

Model-Based Testing Real-Time and Interactive Music Systems

Thesis defended on 11/10/16

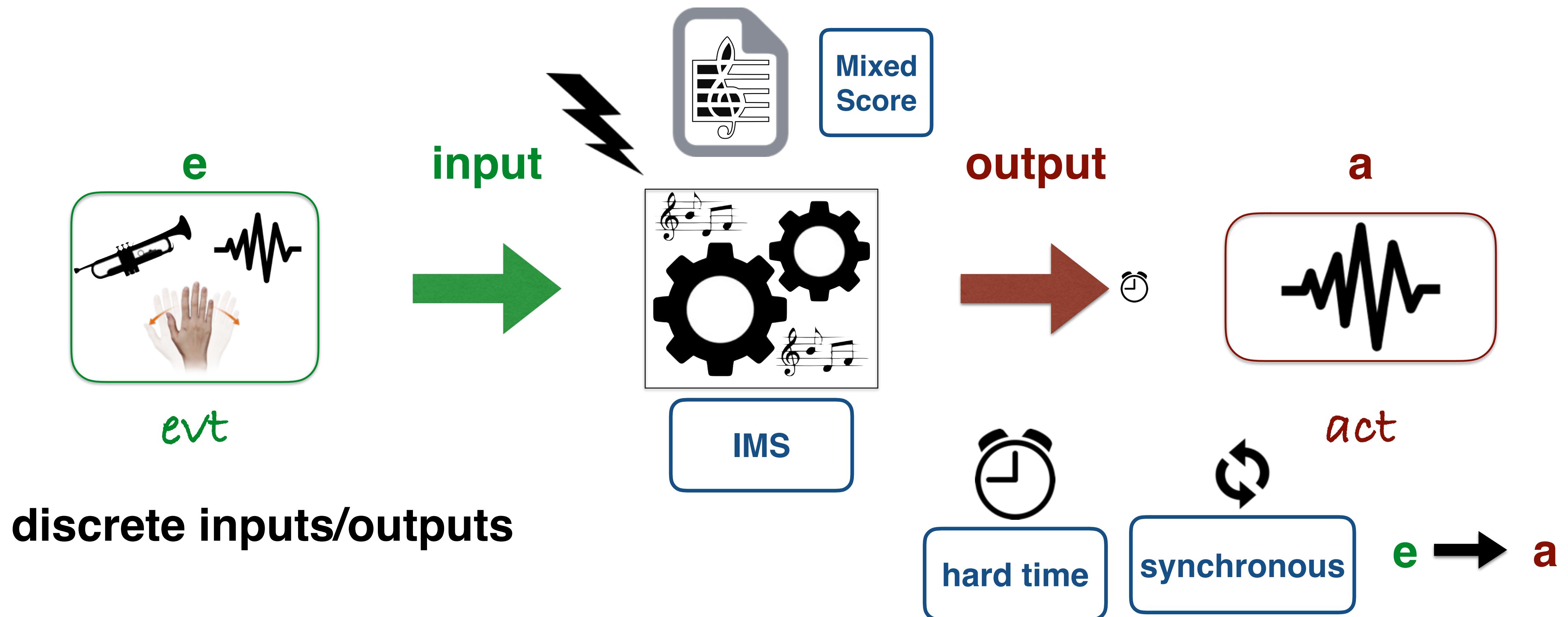
Poncelet Sanchez Clement,
Florent Jacquemard

SYNCHRON 2016

Team: RepMus



Score-Based Interactive Music Systems



Anthèmes 2
pour violon et dispositif électronique (1997)



Mixed Score

Pierre Boulez
(*1925)

*Libre
brusque*
(♩ = 92)

Violon

Spatialization F -11/-18/-18/2.0

Inf. Rev.

Spatialization reverb. time: 60"
F -11/-18/-18/2.0

Sampl. IR

Spatialization MIDI: 93.90.85.84.82.80.79.77.76.75.74
reverb. time: 60"
F -11/-18/-18/2.0

Sampler

Spatialization pizz.
♩ = 93 msec.
MIDI: [74.73.70.69.68.67.66.63.]

MR -4/-12/-24/2.0

batt. (archet normal)
(♩ = 66)

3

Anthèmes 2
pour violon et dispositif électronique (1997)



Mixed Score

Pierre Boulez
(*1925)

**Libre
brusque**
 $\text{♩} = 92$

Violon
Spatialization
F -11/-18/-18/2.0

Inf. Rev.
Spatialization
F -11/-18/-18/2.0

Sampl. IR
Spatialization
F -11/-18/-18/2.0

Sampler
Spatialization
MR -4/-12/-24/2.0

Interpretation
Scored
Sous-objets

Violon
2
 $\text{♩} = 92 \text{ rall.}$
batt. (archet normal)
 $\text{♩} = 66$

Inf. Rev.
reverb. time: 60"
 $\text{♩} = 90 \text{ msec.}$

Sampl. IR
MIDI: 93.90.85.84.82.80.79.77.76.75.74
reverb. time: 60"
 $\text{♩} = 93 \text{ msec.}$
pizz.
MIDI: [74.73.70.69.68.67.66.63.]

Sampler
 $\text{♩} = 93 \text{ msec.}$
pizz.
[74.73.] [74.71.70] [69.70.73.74] [74.73.72.69.68] [67.68.71.72.73.74.] [63.64.67.68.69.70.71.] [74.73.72.71.70.67.66.]

Anthèmes 2
pour violon et dispositif électronique (1997)



Mixed
Score

Pierre Boulez
(*1925)

*Libre
brusque*

Violon

(♩ = 92)

f

F -11-18-18/2.0

Inf. Rev.

reverb. time: 60"

F -11-18-18/2.0

Sampl. IR

MIDI: 93.90.85 84.82.80.79.77.76.75.74

reverb. time: 60"

F -11-18-18/2.0

Sampler

pizz.

pizz.

[74.73.] [74.71.70] [69.70.73.74] [74.73.72.69.68] [67.68.71.72.73.74.] [63.64.67.68.69.70.71.]

MIDI: [74.73.70.69.68.67.66.63.]

MR -4/-12/-24/2.0

Spatialization

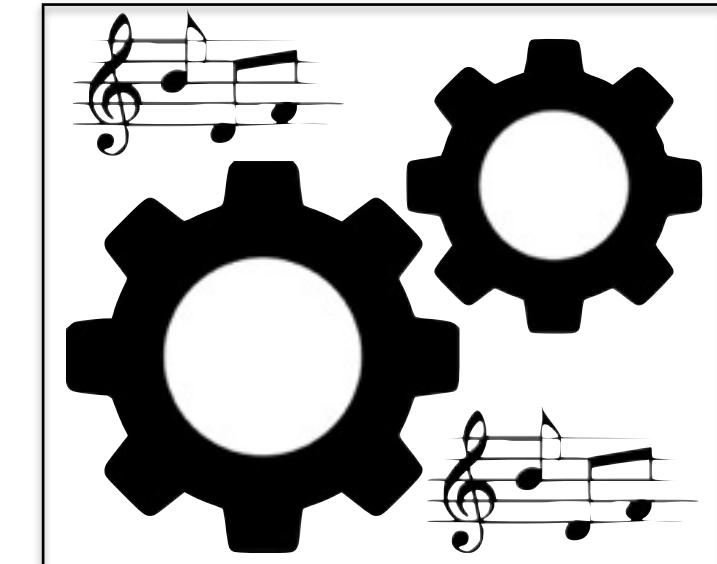
Spatialization

Spatialization

Spatialization

The score page displays a musical score for violin and electronic device. The score is divided into four vertical sections corresponding to the instruments: Violin, Inf. Rev., Sampl. IR, and Sampler. The Violin section includes dynamic markings like *f* and *fff > mf < ff*, and performance instructions like *batt. (archet normal)*. The Inf. Rev. section features a series of numbered circles (1-9) above a line of notes. The Sampl. IR section includes MIDI data and reverb times. The Sampler section contains pizzicato markings and a list of MIDI values. The entire score is framed by a green border at the top and a pink border at the bottom. The title "Anthèmes 2 pour violon et dispositif électronique (1997)" is centered above the score, and the composer's name "Pierre Boulez (*1925)" is in the top right corner.

Interpretation



Anthèmes 2
pour violon et dispositif électronique (1997)



Mixed
Score

Pierre Boulez
(*1925)

*Libre
brusque*

Violon

(♩ = 92)

batt. (archet normal)

(♩ = 66)

f *fff > mf < ff*

Spatialization F -11-18-18/2.0

Inf. Rev.

reverb. time: 60"

Spatialization

F -11-18-18/2.0

♩ = 90 msec.

Sampl. IR

MIDI: 93.90.85.84.82.80.79.77.76.75.74

reverb. time: 60"

Spatialization

F -11-18-18/2.0

Sampler

pizz.

♩ = 93 msec.

pizz.

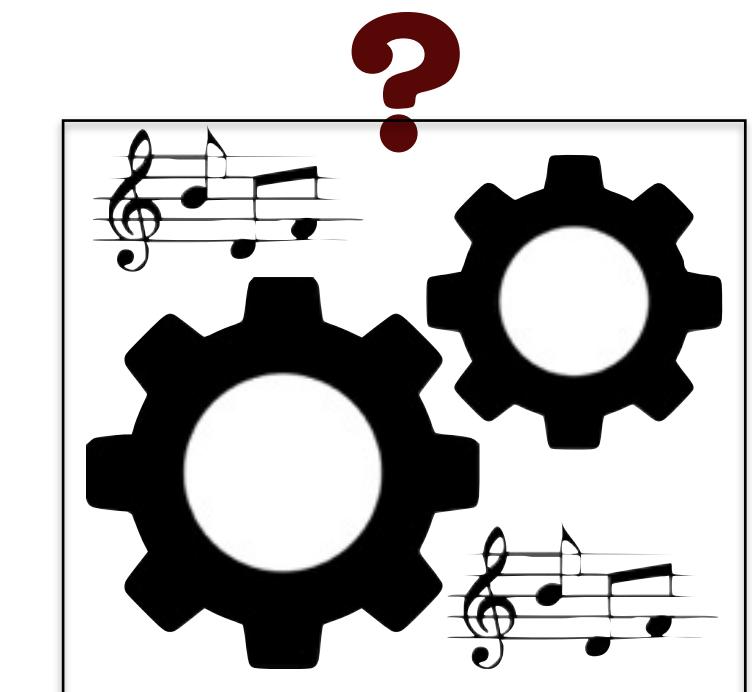
[74.73.] [74.71.70] [69.70.73.74] [74.73.72.69.68] [67.68.71.72.73.74.] [63.64.67.68.69.70.71.] [74.73.72.71.70.67.66.]

Spatialization

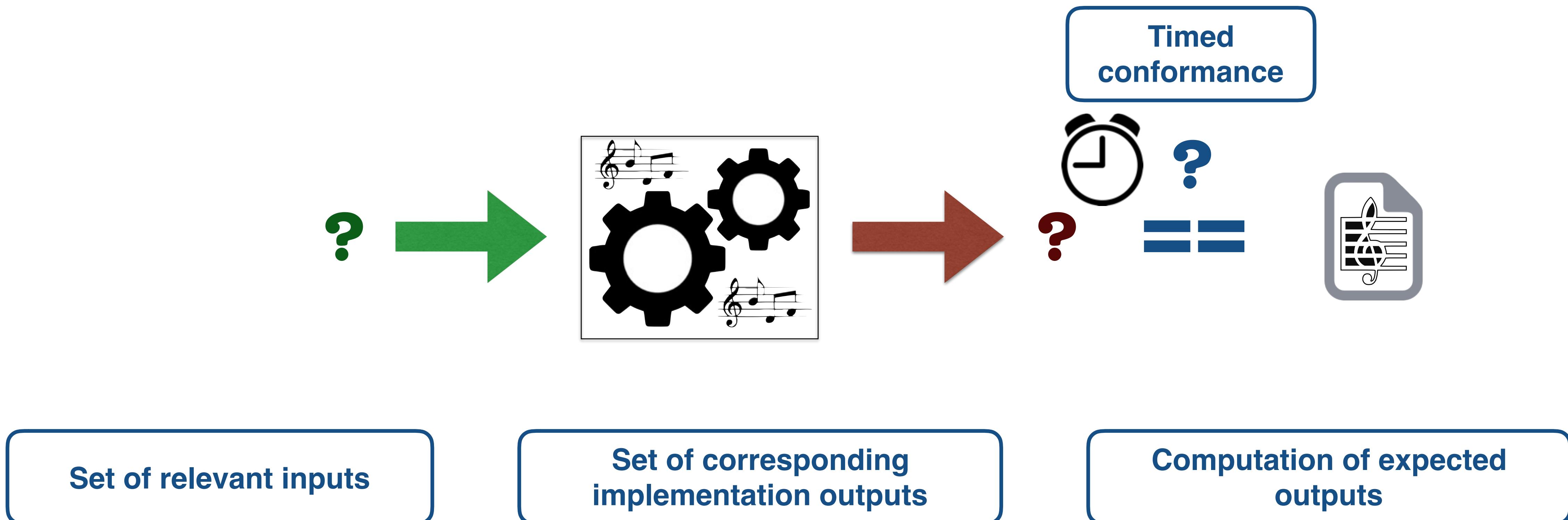
MR -4/-12/-24/2.0

The musical score for Anthèmes 2 by Pierre Boulez is shown in a mixed score format. It includes parts for Violon, Inf. Rev., Sampl. IR, and Sampler. The Violon part features a dynamic range from *f* to *fff* and *ff*. The Inf. Rev. part includes reverberation settings. The Sampl. IR part lists MIDI notes and reverb times. The Sampler part uses pizzicato and specifies note durations and performance times. A red double-headed arrow on the Violon staff indicates a performance range, and three red X marks highlight specific notes. A red arrow points to the *Spatialization* section of the Violon staff.

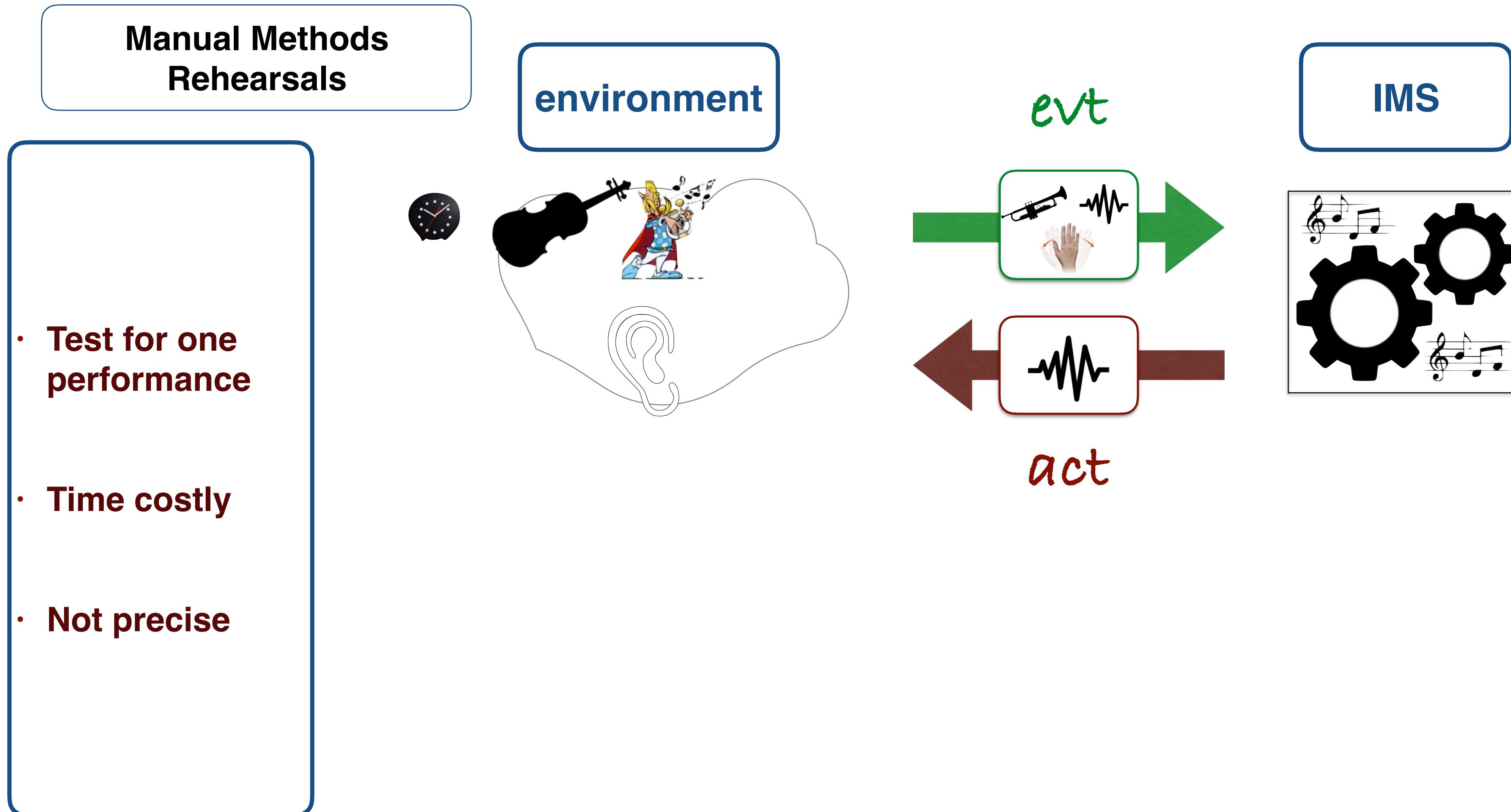
Interpretation



Timed Conformance Testing

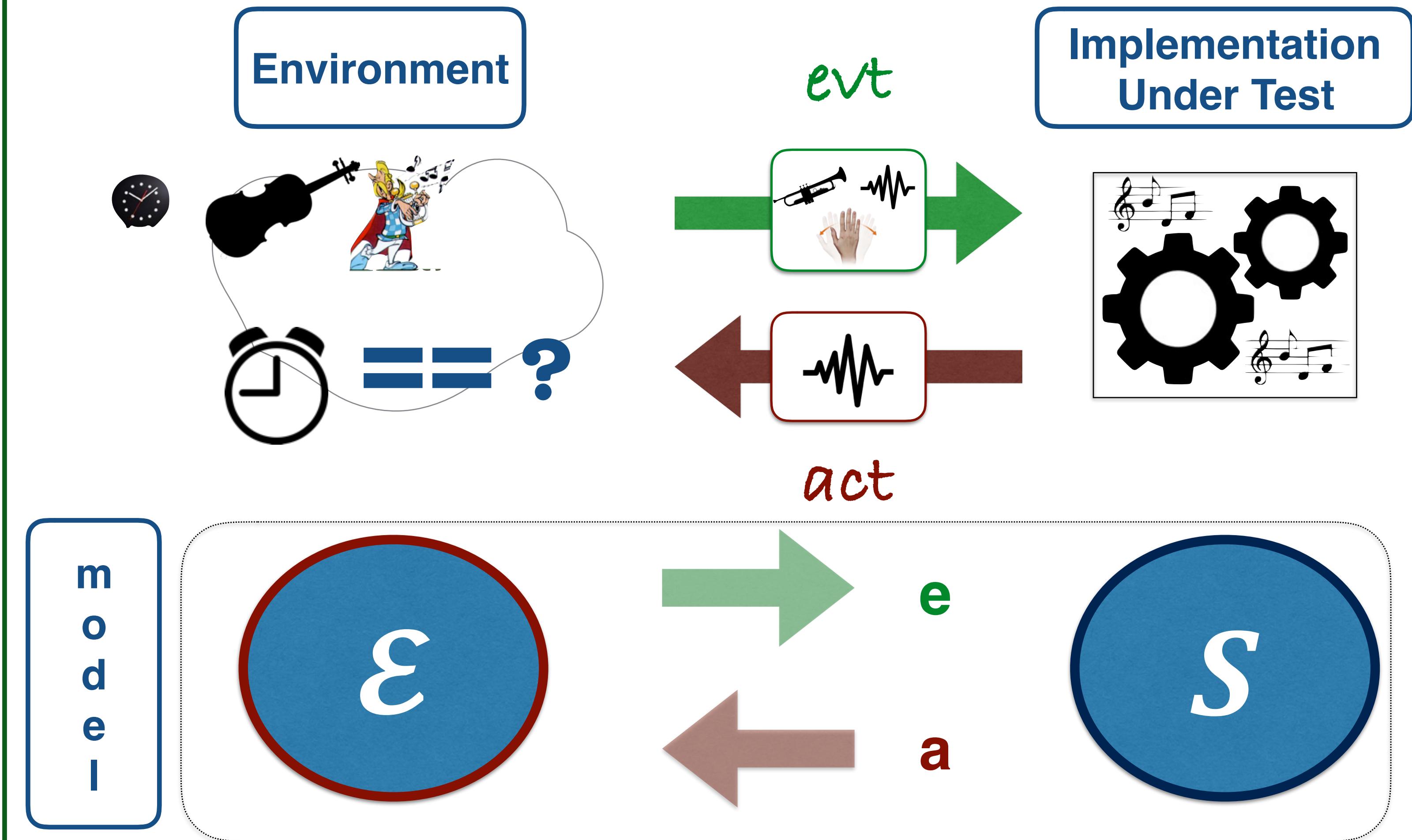


Manual Testing IMS

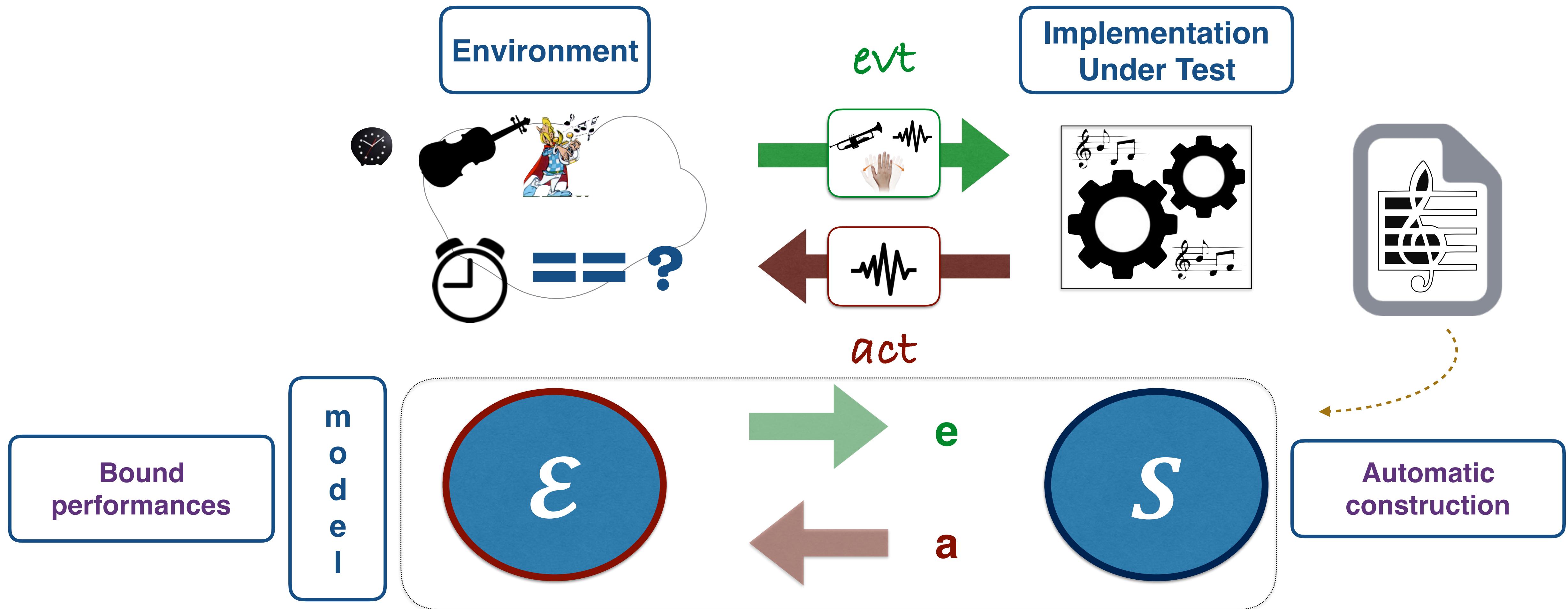


Model-Based Testing IMS

- ‘Exhaustive’ generation
- Fast forward execution (virtual clocks)
- Precise:
 - Automated comparison
 - Formal conformance criteria
 - informative feedbacks

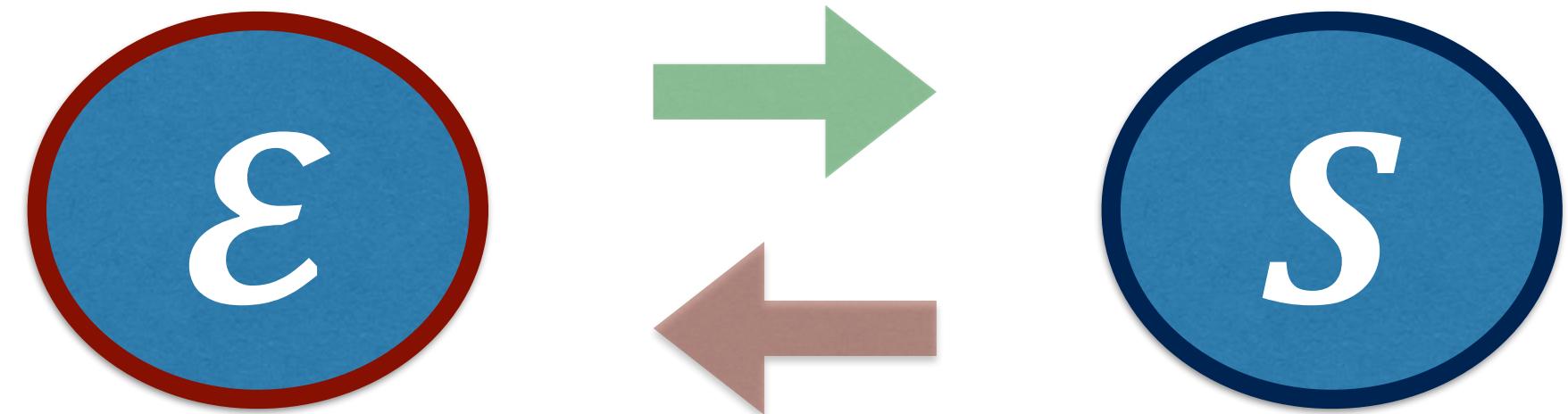


Model-Based Testing IMS



Outline

1.Objectives

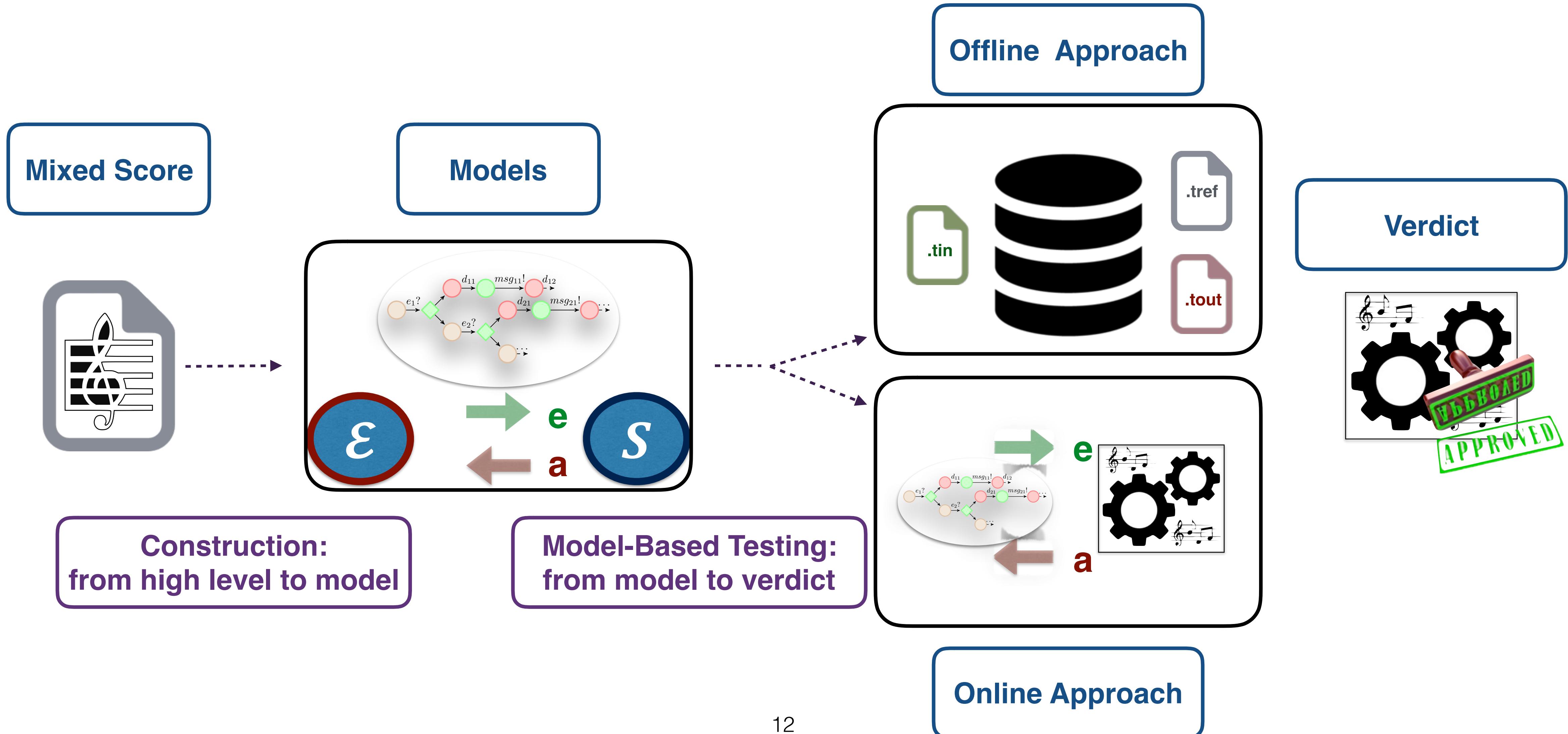


2.Testing Framework



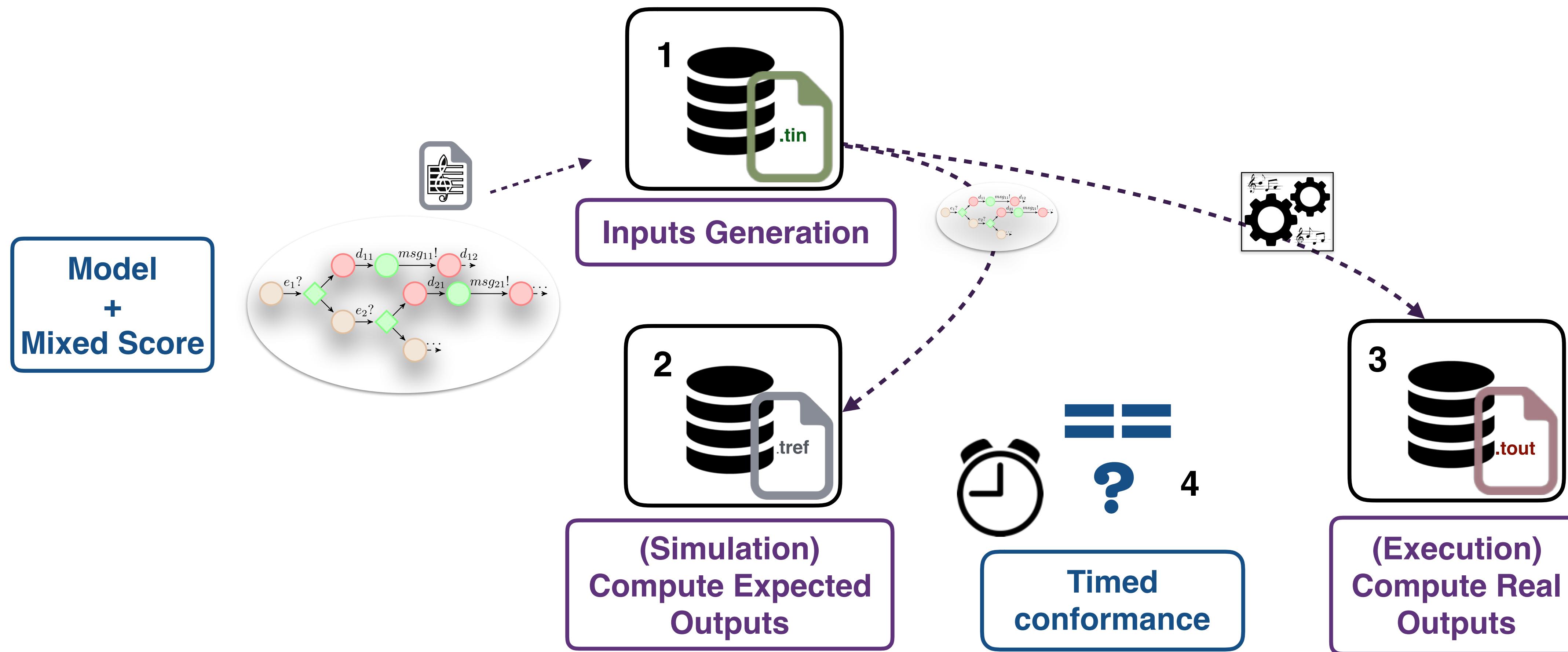
3.Interactive Real-Time Model

Testing Framework Overview



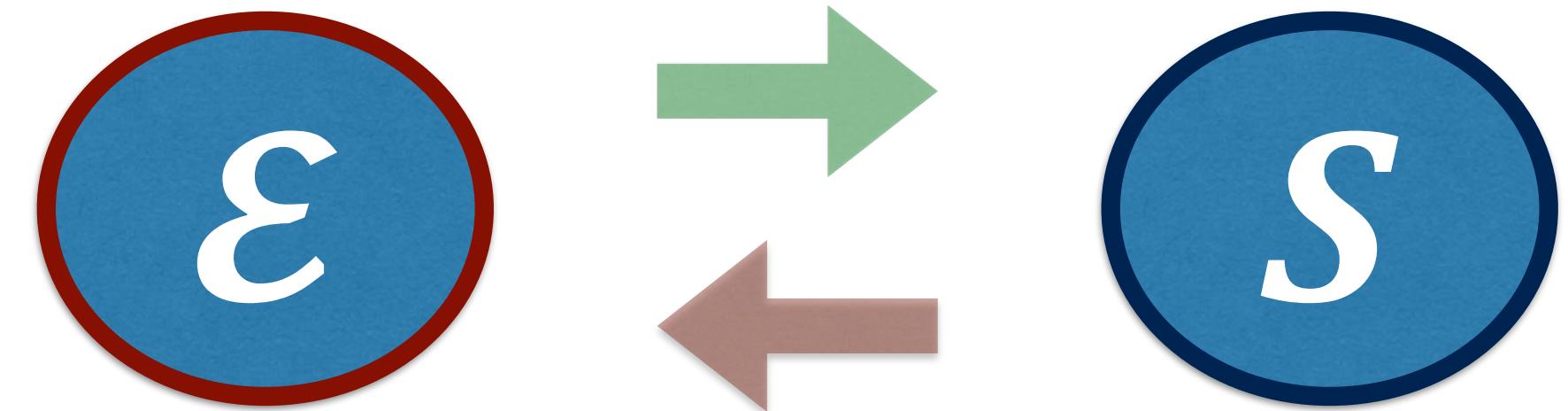


Testing Approaches

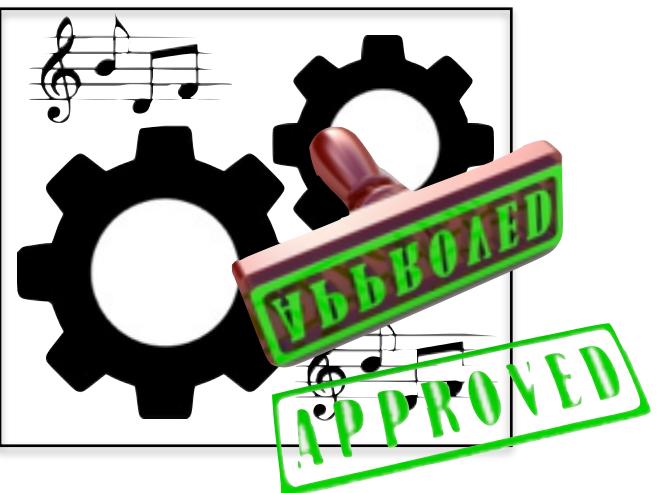


Outline

1. Objectives

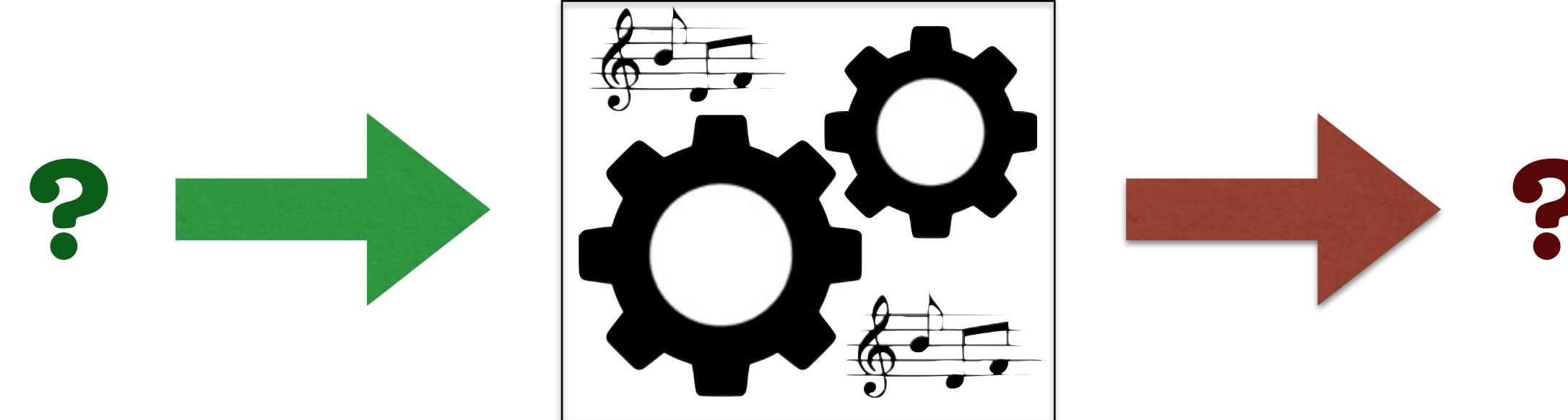


2. Testing Framework



3. Interactive Real-Time Model

Input / Output formalisation



Timed Traces

Timed Input Trace

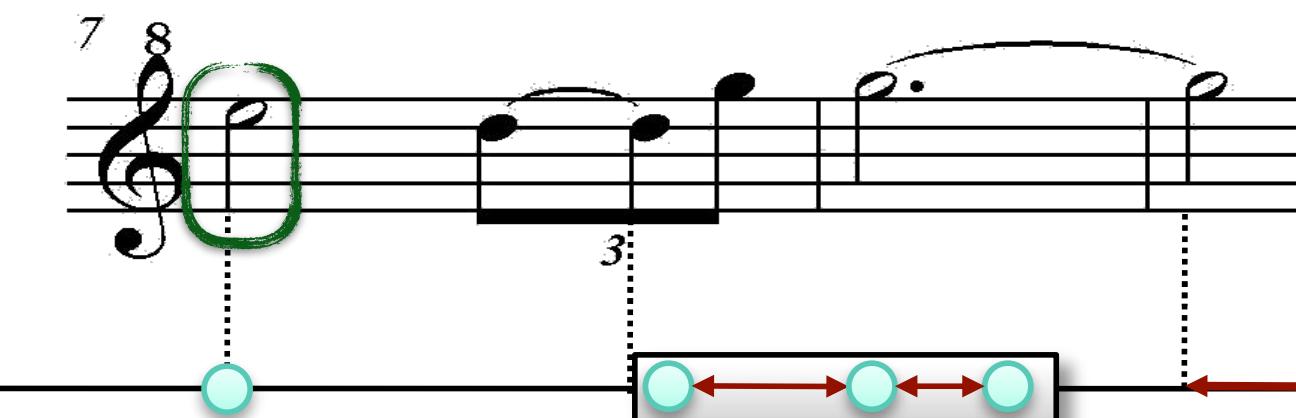
e



tempo:
120bpm

Specified
inputs

$\langle e_1, 0, 120 \rangle$



Definition:

A timed trace is a tuple $\langle s, t, p \rangle$:

s: symbol

t: timestamp in time unit

p: pace in time unit per minute

Timed Traces

Timed Input Trace

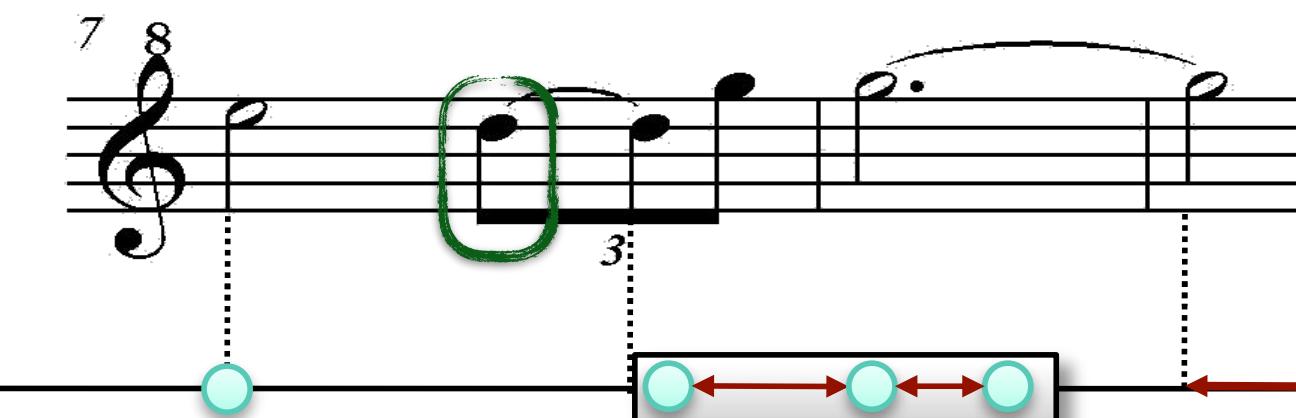
e



tempo:
120bpm

Specified
inputs

$\langle e_1, 0, 120 \rangle \times \langle e_2, 2, 120 \rangle$



Definition:

A timed trace is a tuple $\langle s, t, p \rangle$:

s: symbol

t: timestamp in time unit

p: pace in time unit per minute

Timed Traces

Timed Input Trace

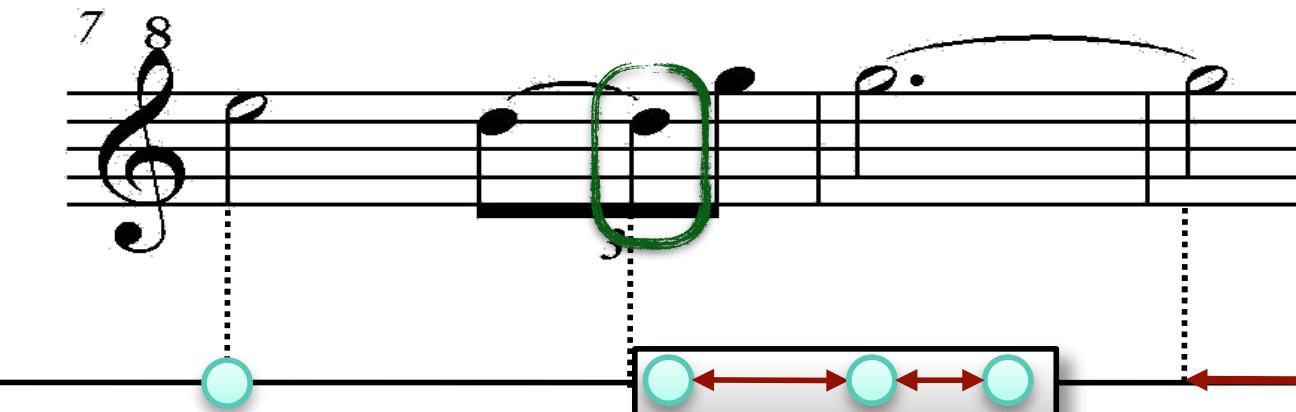
e



tempo:
120bpm

Specified
inputs

$\langle e_1, 0, 120 \rangle \times \langle e_2, 2, 120 \rangle \times \boxed{e_3, 2.33, 120}$



Definition:

A timed trace is a tuple $\langle s, t, p \rangle$:

s: symbol

t: timestamp in time unit

p: pace in time unit per minute

Timed Input Trace



tempo:
120bpm

Specified
inputs

$\langle e_1, 0, 120 \times e_2, 2, 120 \times e_3, 2.33, 120 \times e_4, 2.66, 120 \times e_5, 3, 120 \times e_6, 6, 120 \rangle$

$\langle e_1, 0, 120 \times e_2, 2, 120 \rangle ! \langle e_4, 2.66, 120 \times e_5, 3, 120 \times e_6, 6, 120 \rangle$

$\langle e_1, 0, 120 \times e_2, 1.9, 120 \rangle \langle e_4, 2.76, 120 \times e_5, 3.2, 120 \times e_6, 5.9, 120 \rangle$

$\langle e_1, 0, 119 \times e_2, 1.9, 80.9 \rangle \langle e_4, 2.76, 114 \times e_5, 3.2, 115.3 \times e_6, 5.9, 119 \rangle$

Timed Traces

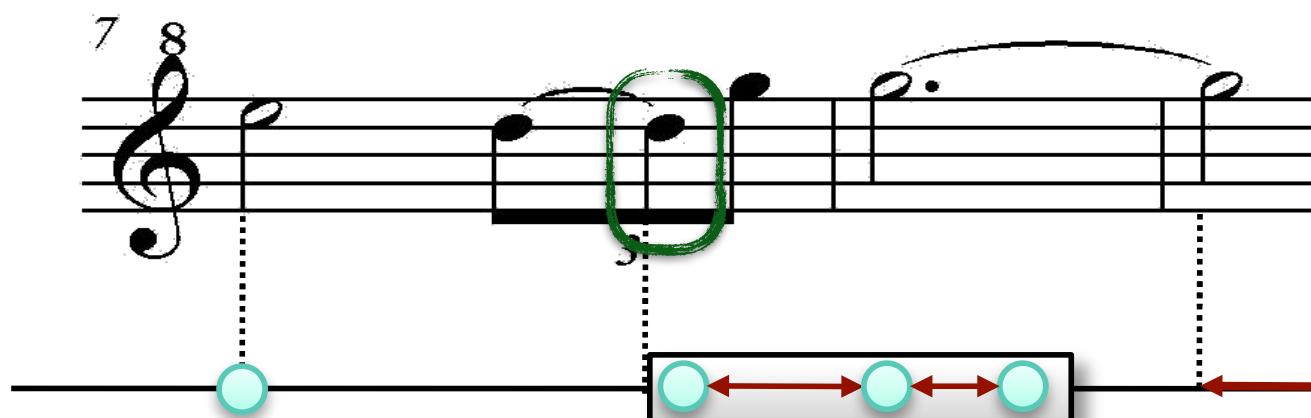
Definition:

A timed trace is a tuple $\langle s, t, p \rangle$:

s: symbol

t: timestamp in time unit

p: pace in time unit per minute



errors

Interpretation



variations

Timed Traces

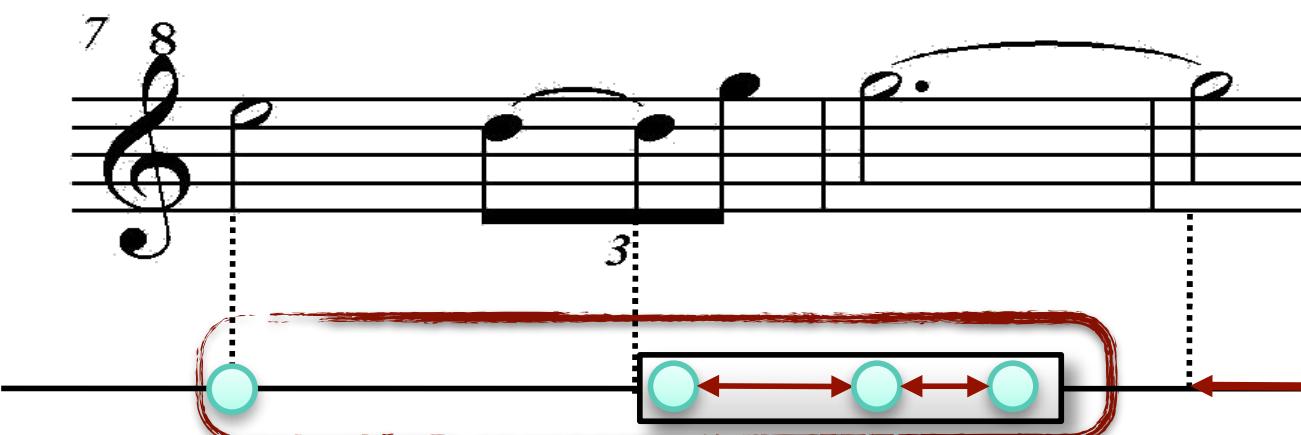
Timed Input Trace



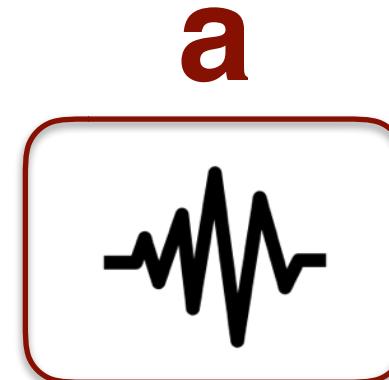
tempo:
120bpm

Specified
inputs

$\langle e_1, 0, 120 \times e_2, 2, 120 \times e_3, 2.33, 120 \times e_4, 2.66, 120 \times e_5, 3, 120 \times e_6, 6, 120 \rangle$



Timed Output Trace



Expected
trace

$\langle a_1, 0, 60 \times a_2, 2.66, 60 \times a_3, 3, 60 \rangle$

$\langle e_1, 0, 120 \times e_2, 2, 120 \rangle ! \langle e_4, 2.66, 120 \times e_5, 3, 120 \times e_6, 6, 120 \rangle$

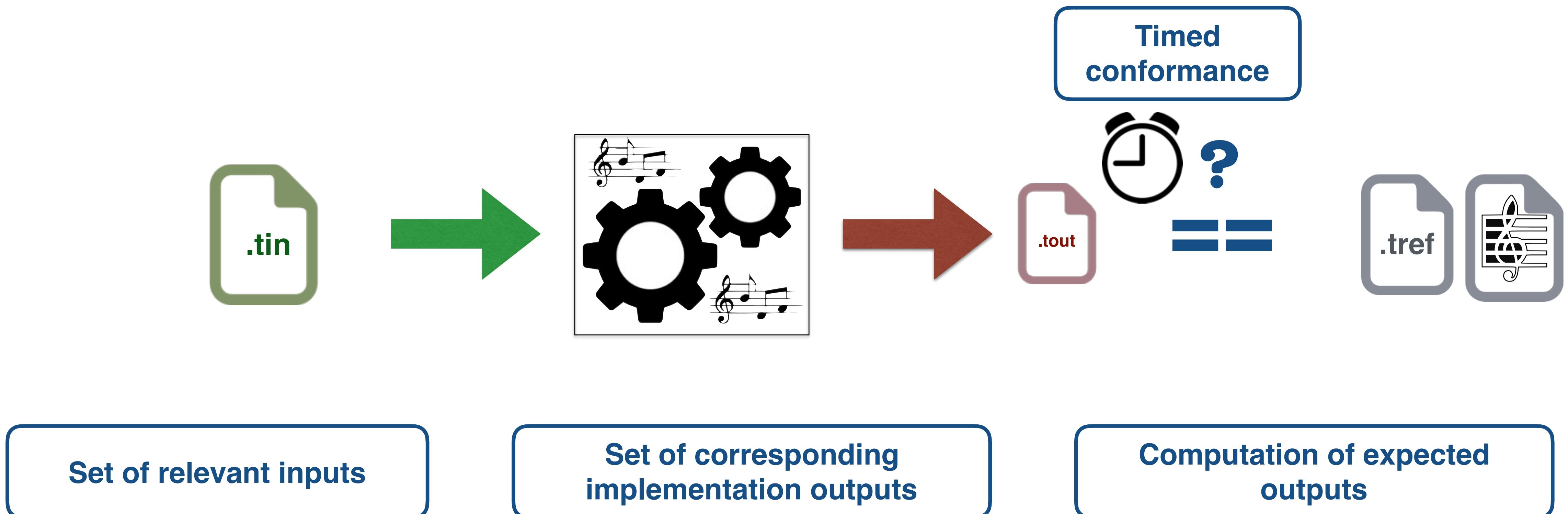
$\langle e_1, 0, 120 \times e_2, 1.9, 120 \rangle \langle e_4, 2.76, 120 \times e_5, 3.2, 120 \times e_6, 5.9, 120 \rangle$

$\langle e_1, 0, 119 \times e_2, 1.9, 80.9 \rangle \quad \langle e_4, 2.76, 114 \times e_5, 3.2, 115.3 \times e_6, 5.9, 119 \rangle$

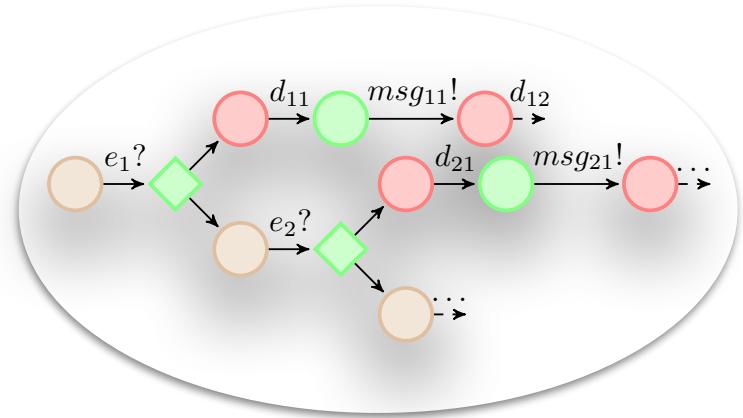


?

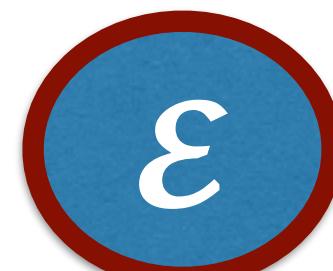
Timed Conformance Testing



Models



Environment Model



Model = E + S

e
a



System Model

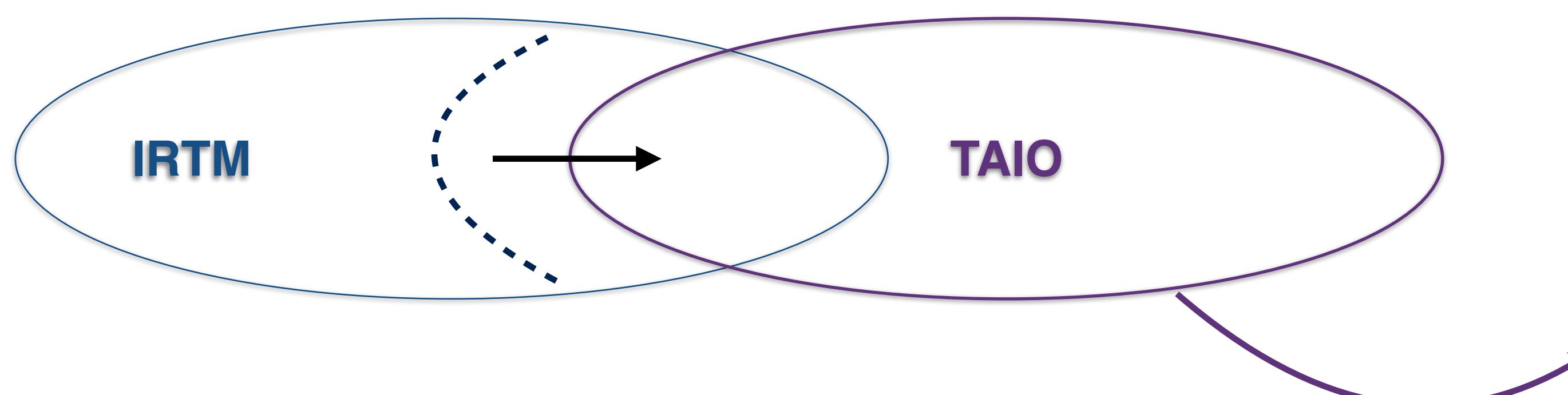
Bound performances

Compute expected output

Interactive Real-Time Model

Timed Automata with Input-Output

TA aspects
Synchronous aspects



IRTM

TAIO

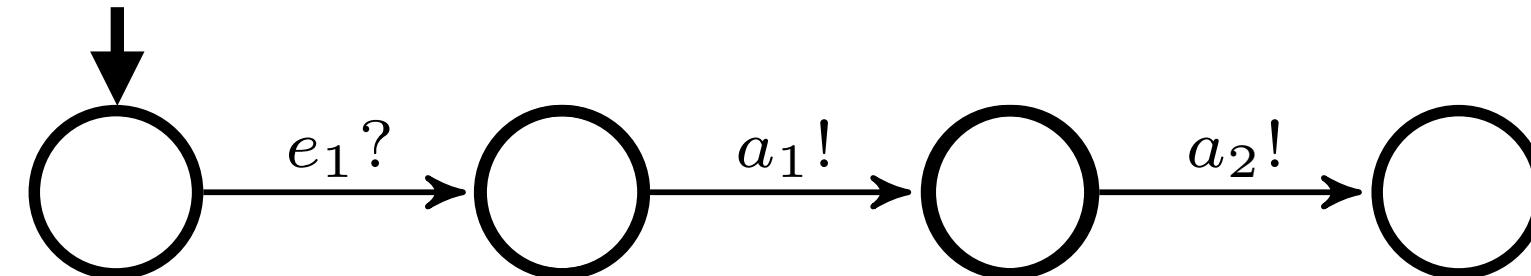
model-checking /
decidability

Labelled Transition System

System Specification

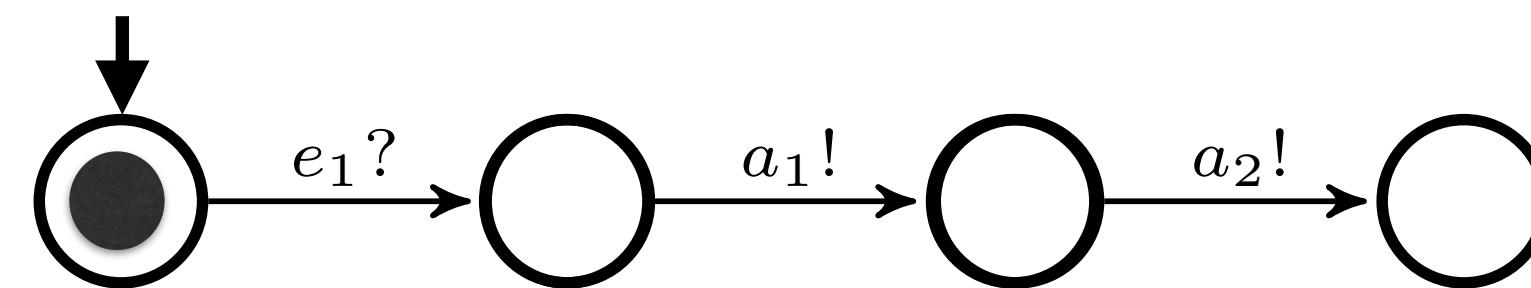
Input/Output

e a



Labelled Transition System

Simulation



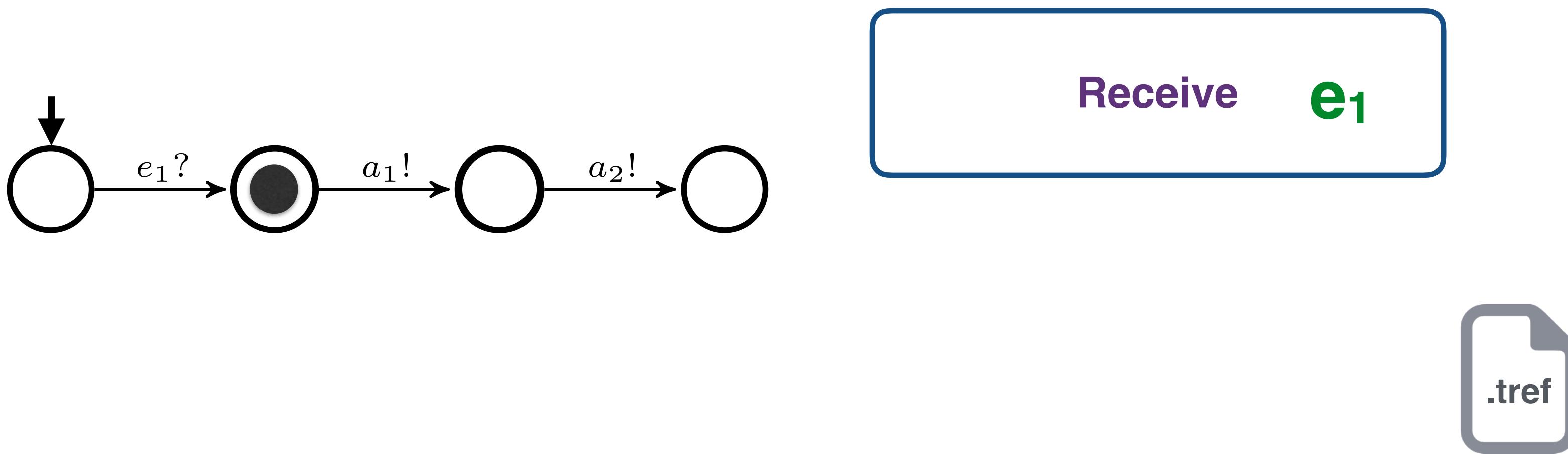
Jan Tretmans.
Model Based Testing with Labelled Transition Systems.
Formal Methods and Testing, an outcome of the FORTEST.



M. Timmer, E. Brinksma and M. Stoelinga.
Model Based Testing.
Software and Systems Safety - Specification and Verification.

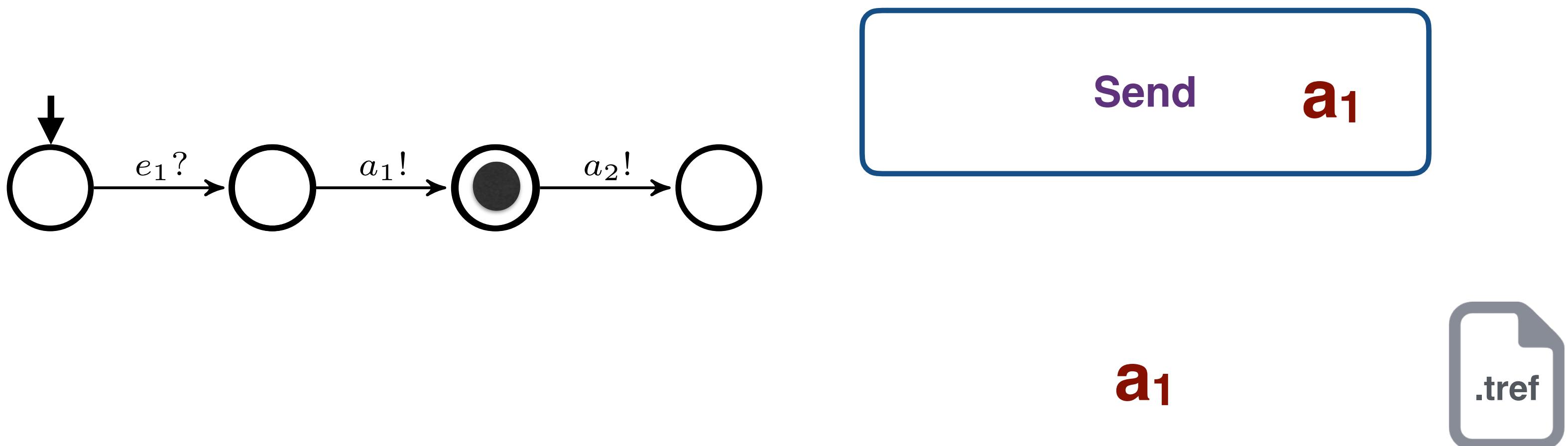
Labelled Transition System

Simulation



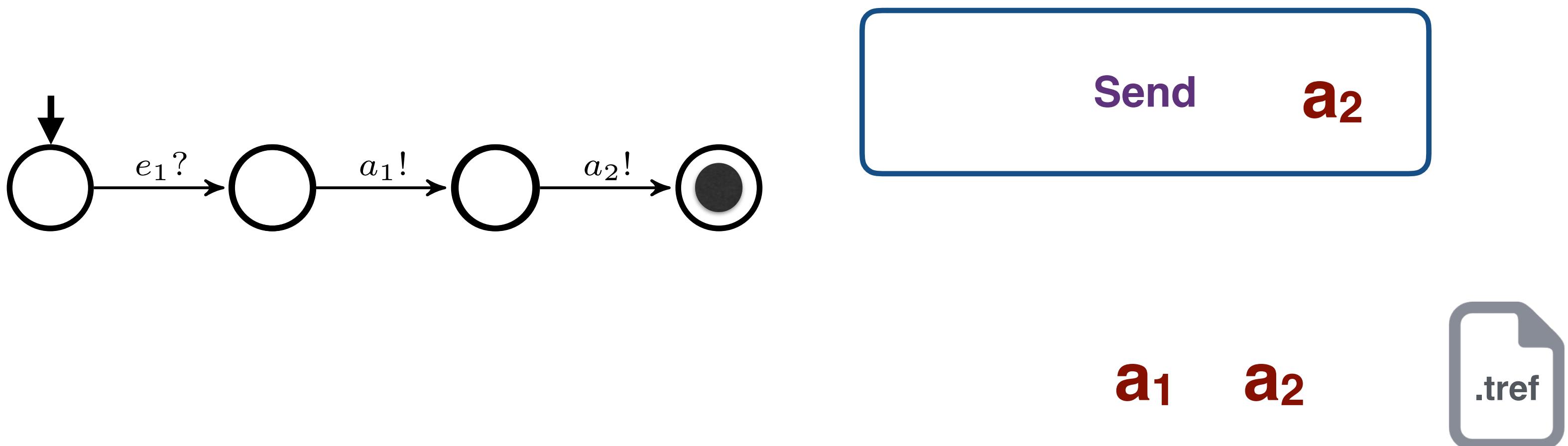
Labelled Transition System

Simulation



Labelled Transition System

Simulation



Timed Automata with Input-Output

System Specification

Time

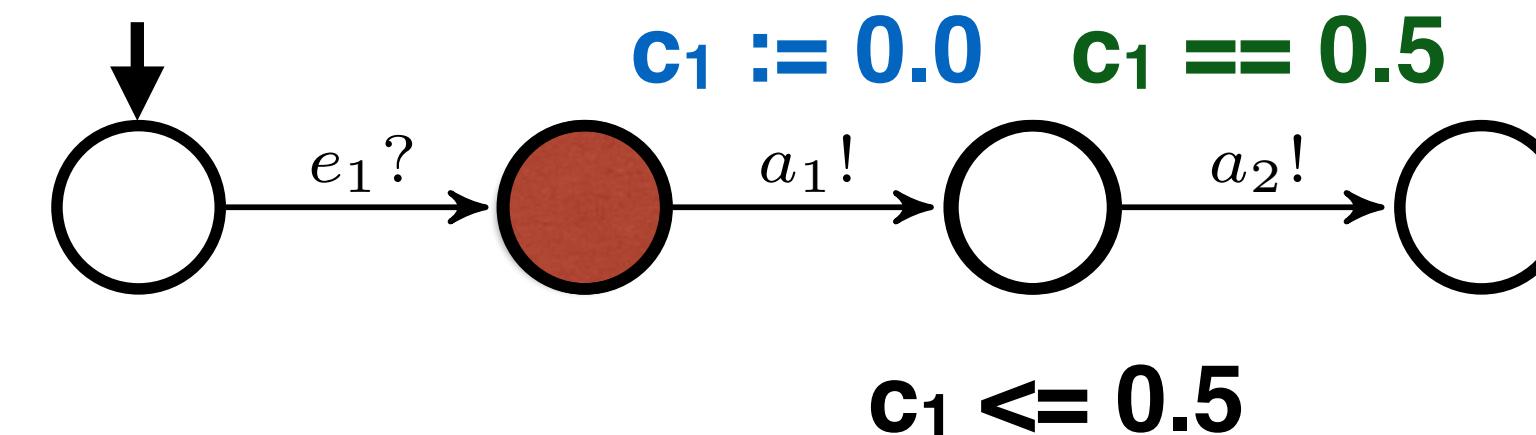


clock value: $C_i = \mathbb{R}_+$.

Finite set of clocks
valued on reels

Abstract Time

Same rate

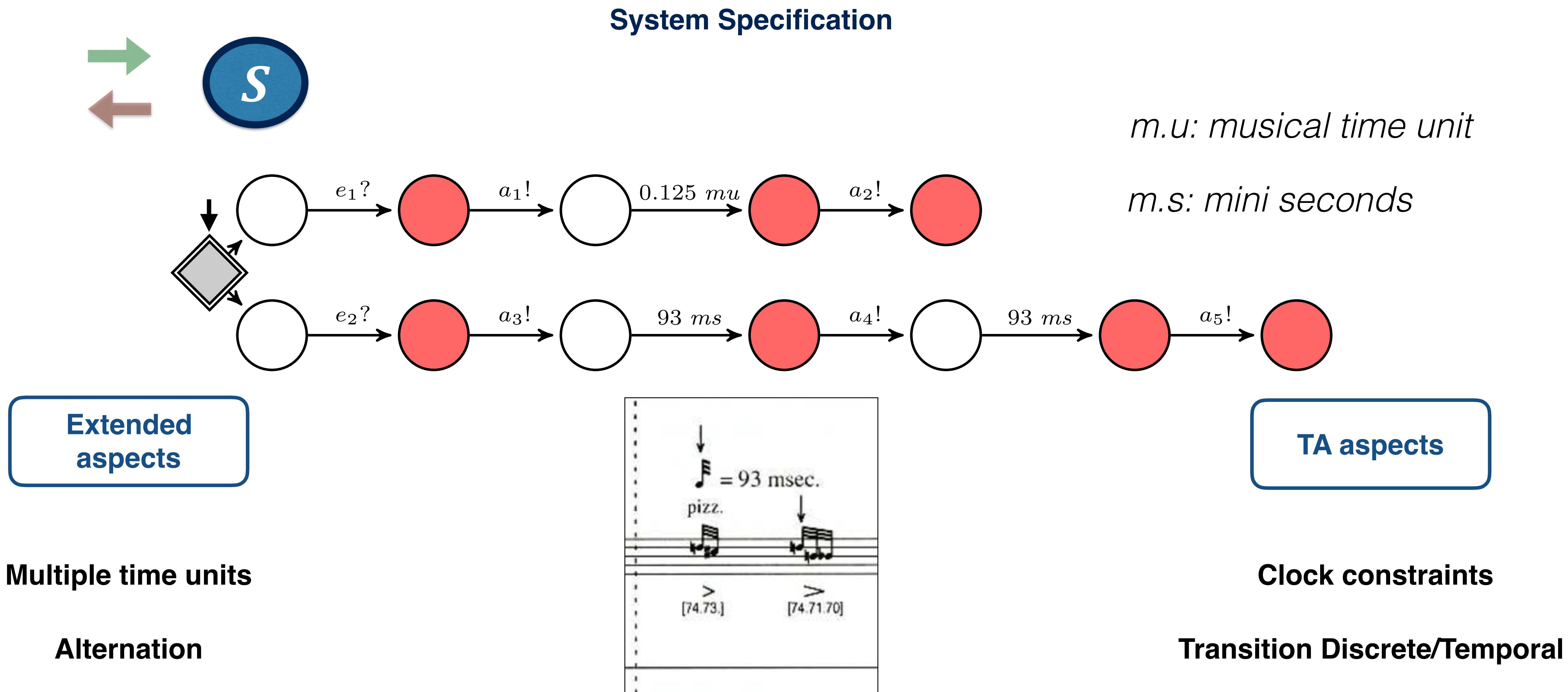


Urgent locations

Restricted with
guards and **invariants**

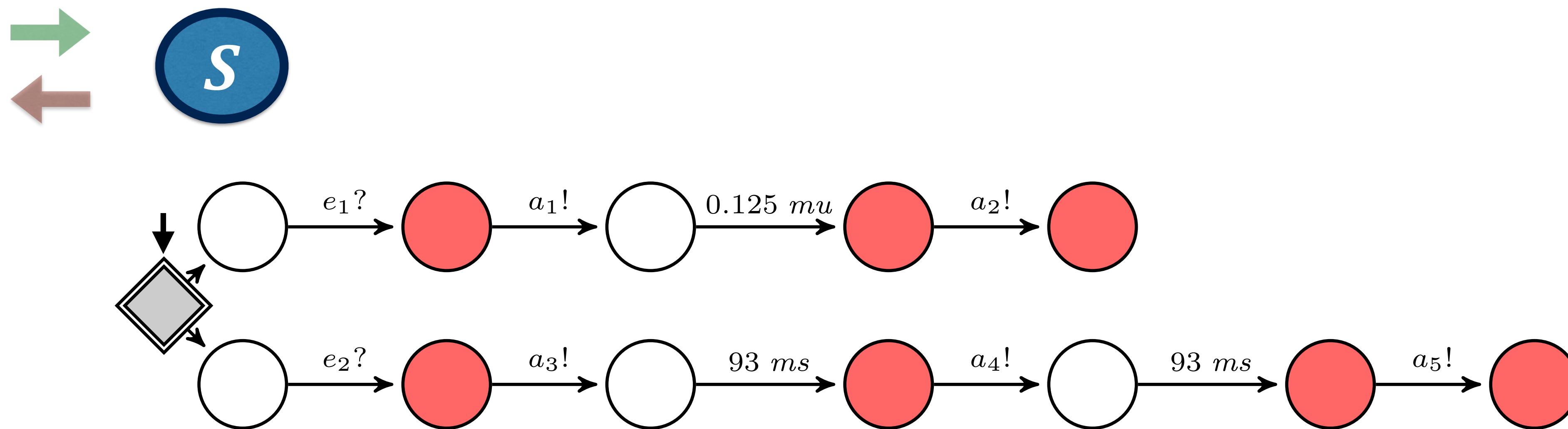
Reset with **affections**

Interactive Real-Time Model (IRTM)



IRTM: System Model

Synchronous aspects



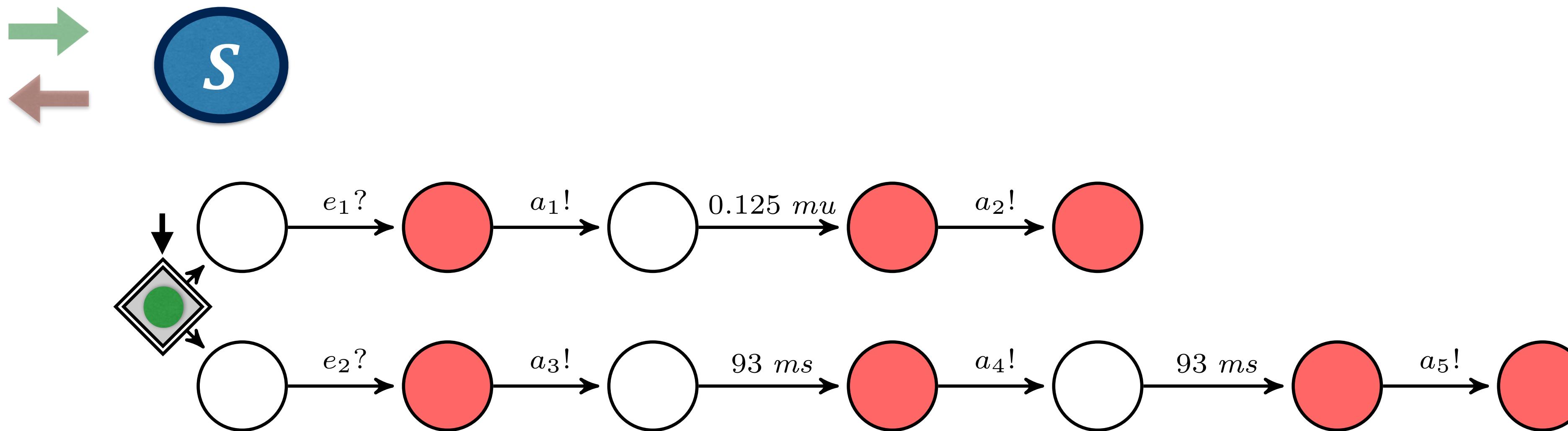
Dense time

State: $\langle t, n \rangle [\text{controls}] \{ \text{symbols} \}$

control: $C_i = \mathbb{R}_+$

IRTM: System Model

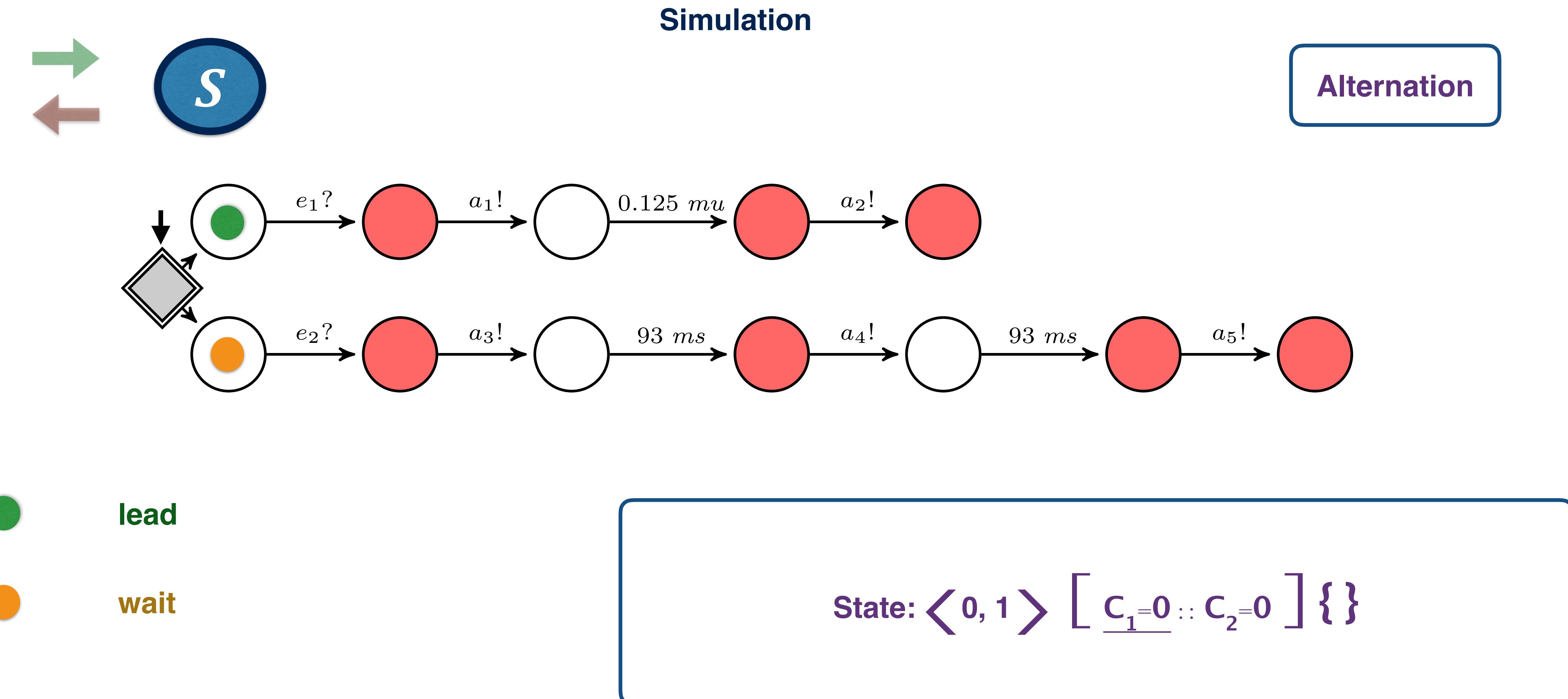
Simulation



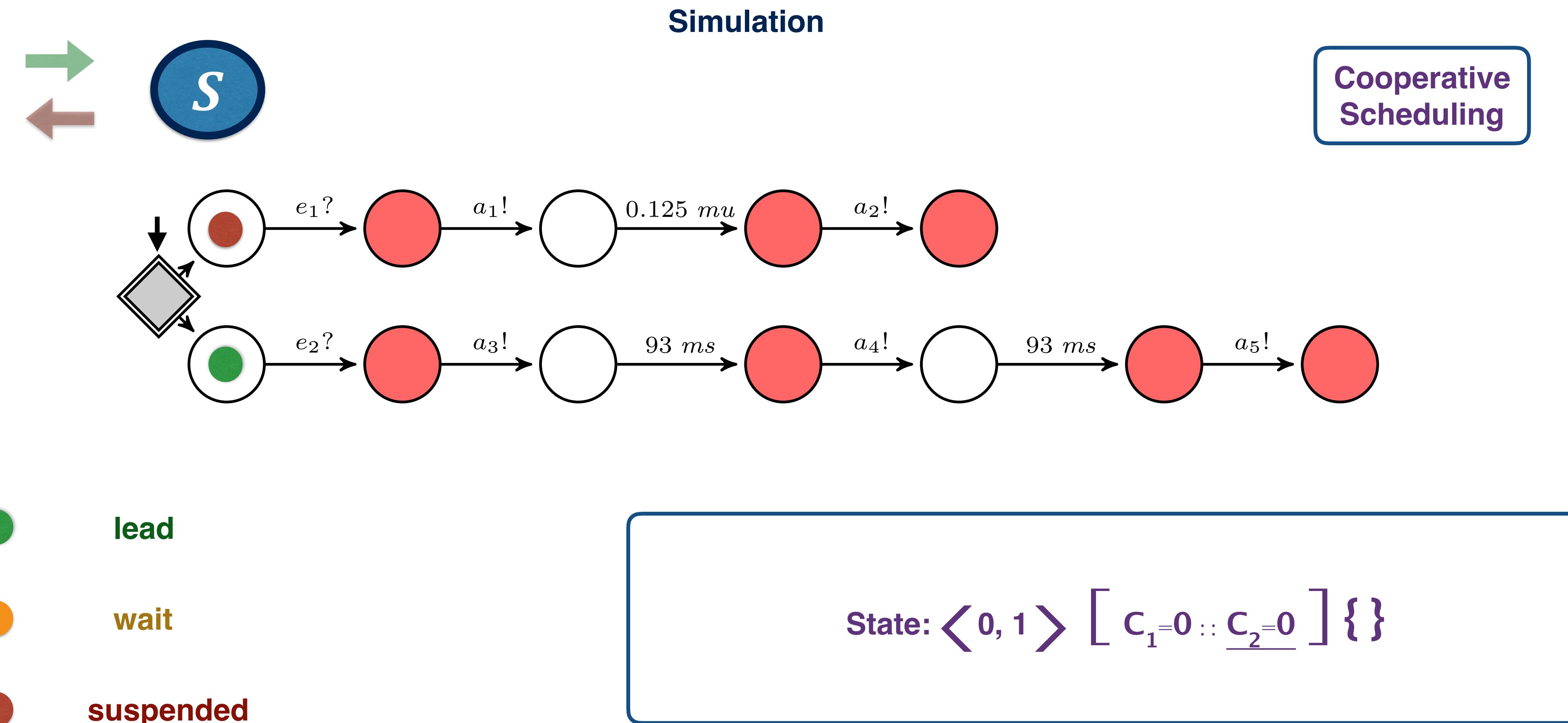
lead

State: $\langle 0, 0 \rangle [\underline{c1:0}] \{ \}$

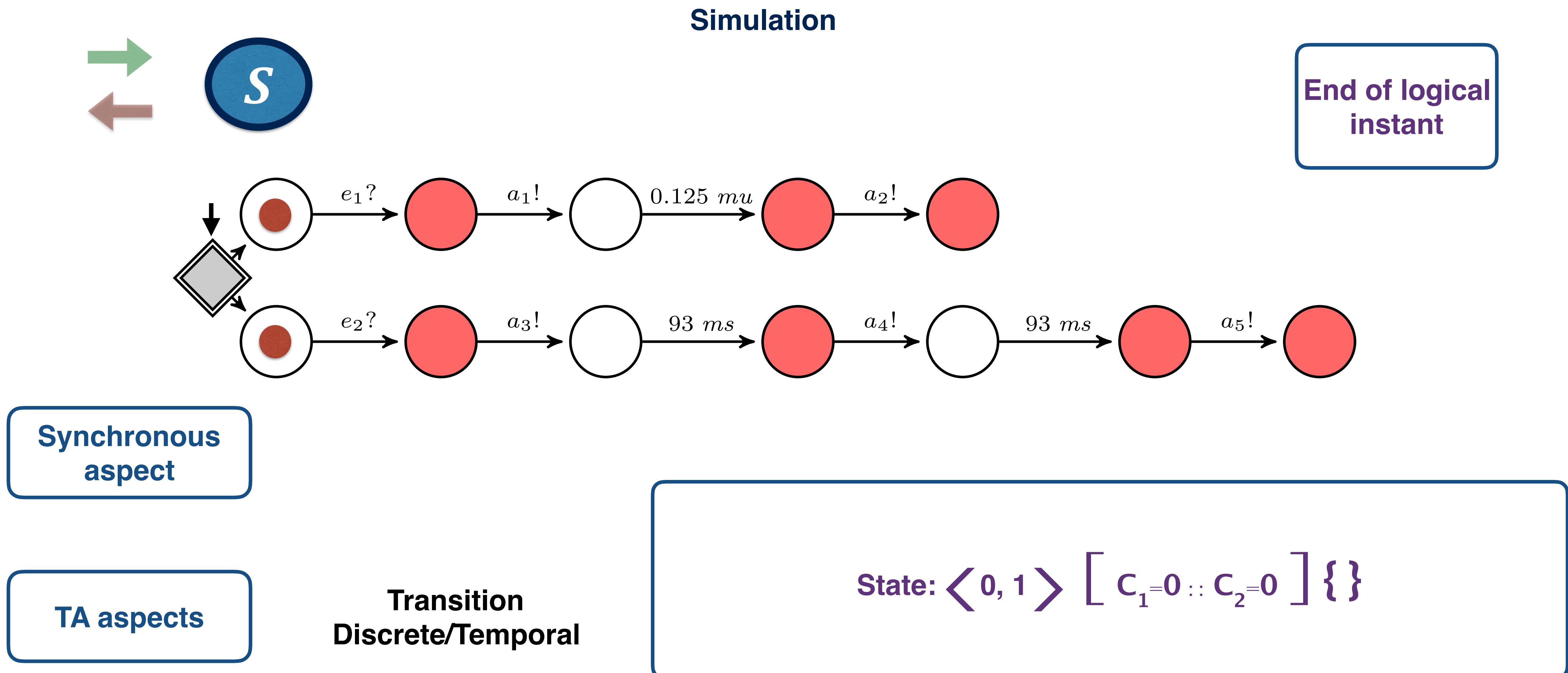
IRTM: System Model



IRTM: System Model

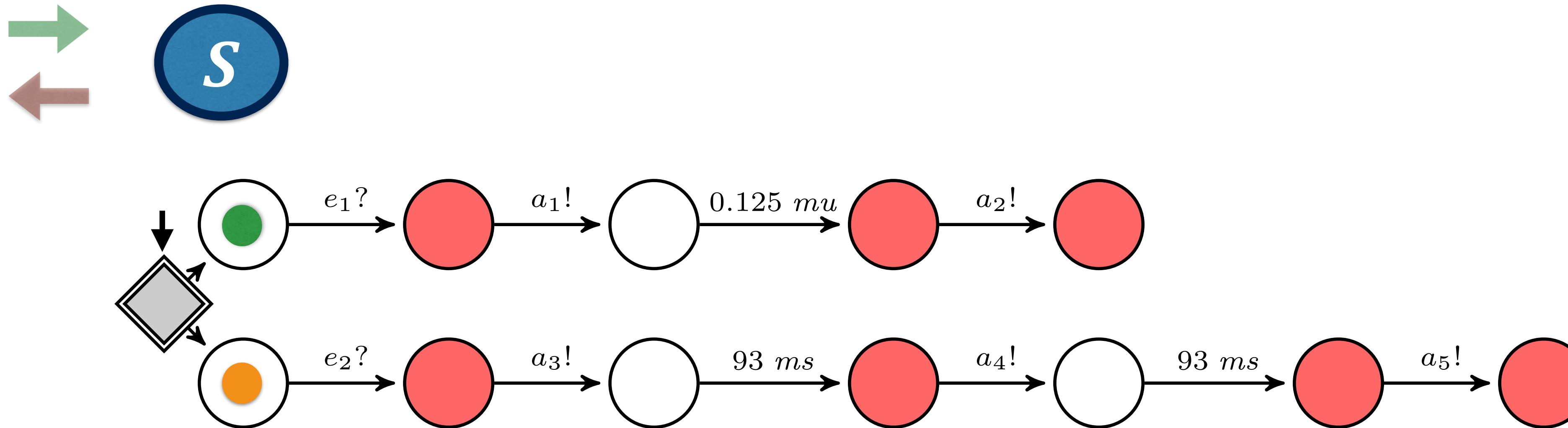


IRTM: System Model



IRTM: System Model

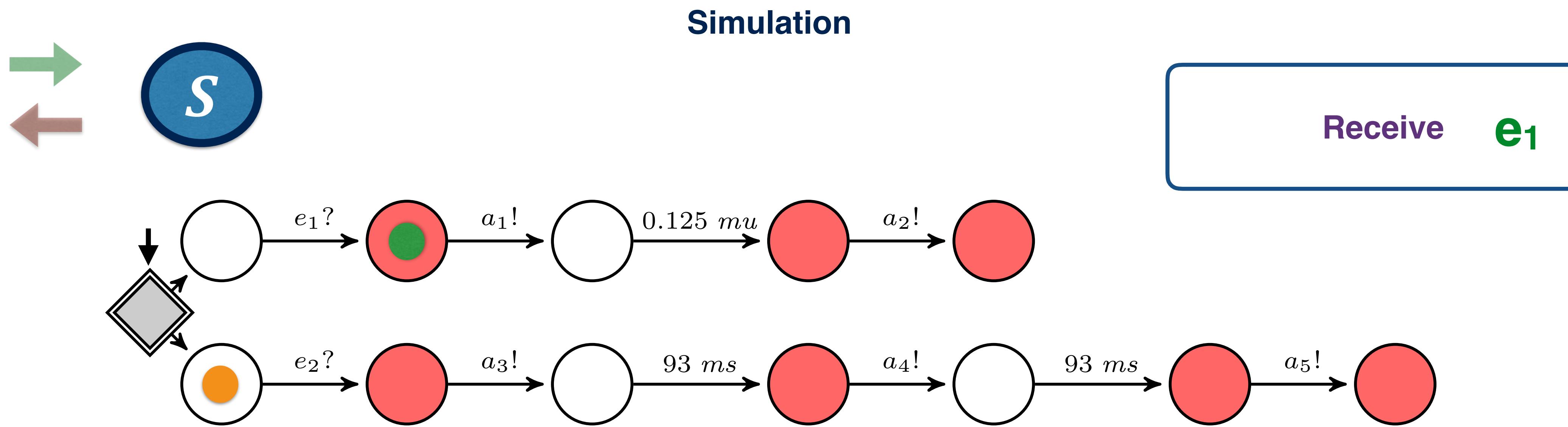
Simulation



.tin → $\langle e_1, 0, 184 \rangle$

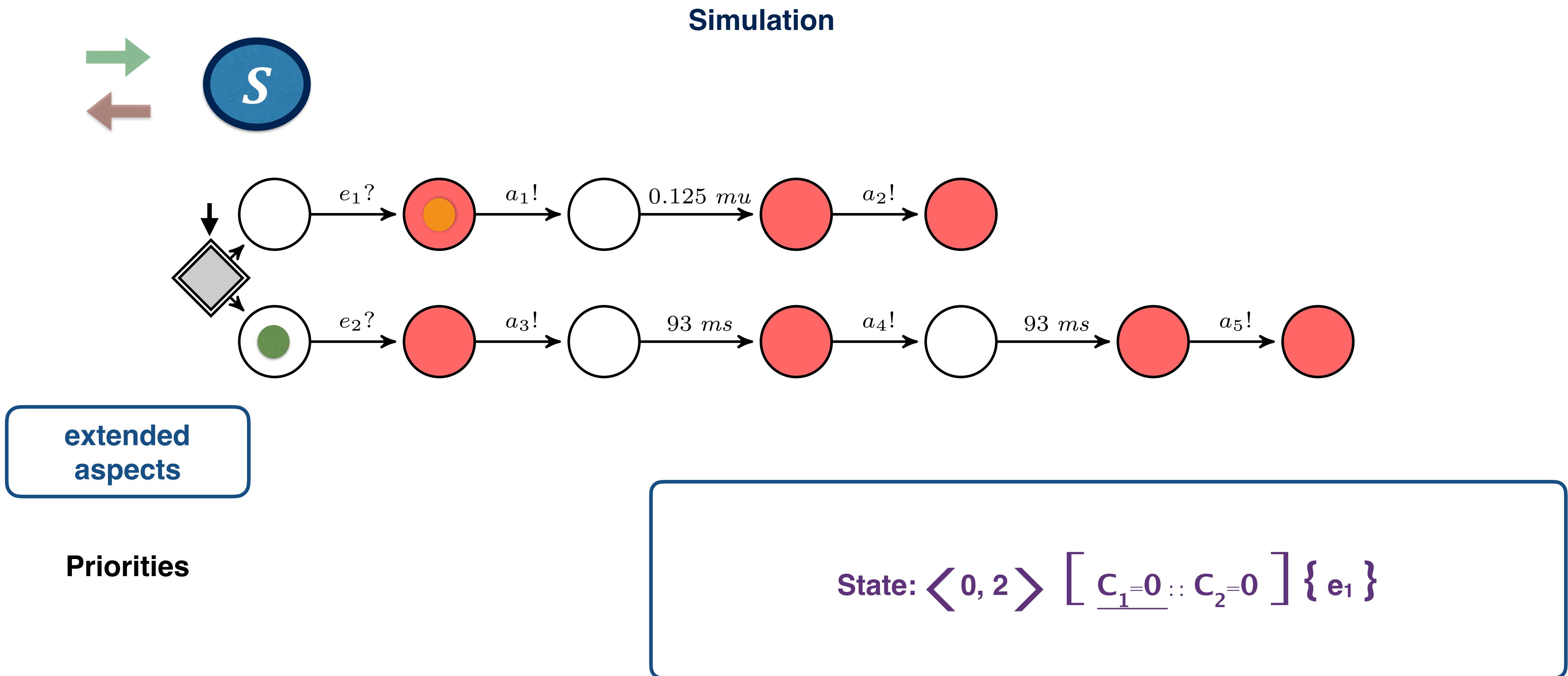
State: $\langle 0, 1 \rangle [c_1=0 :: c_2=0] \{ e_1 \}$

IRTM: System Model

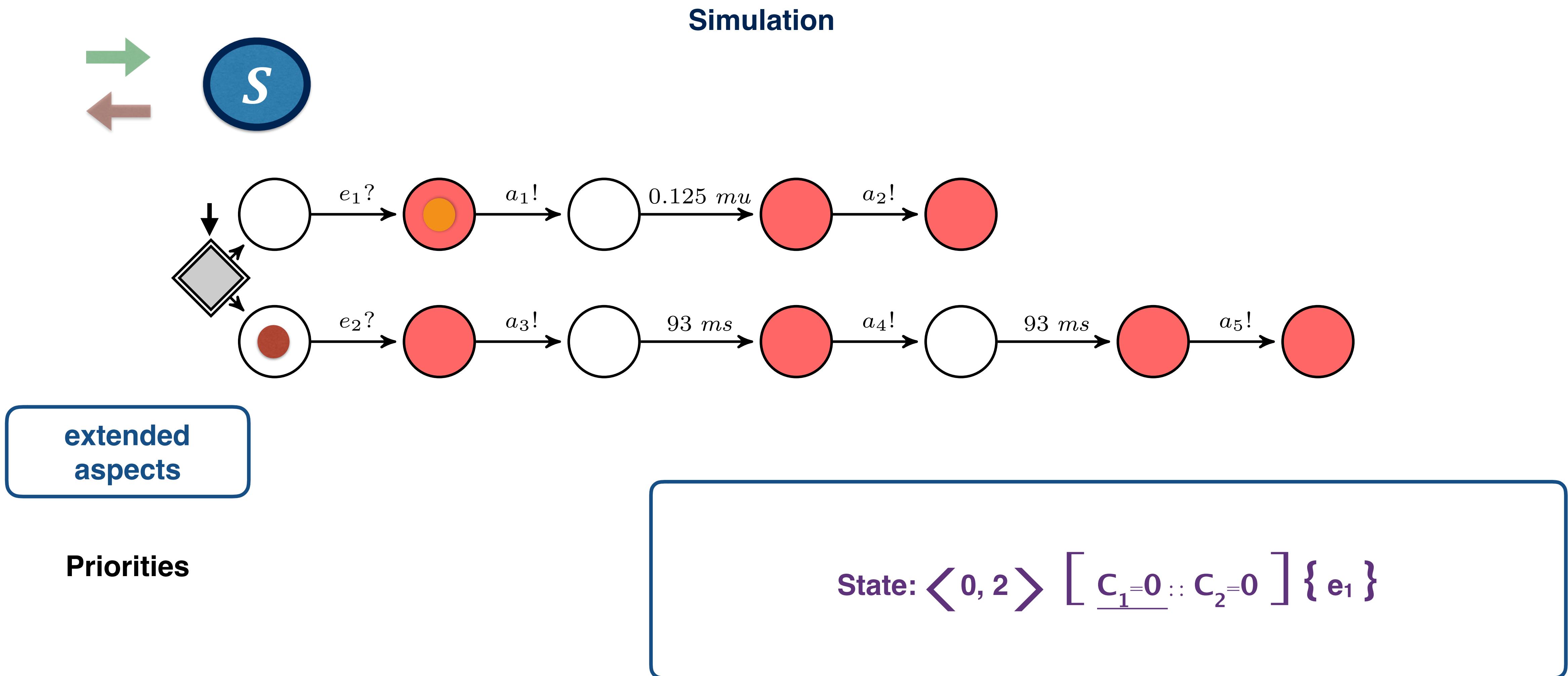


State: $\langle 0, 2 \rangle [\underline{c_1=0} :: c_2=0] \{ e_1 \}$

IRTM: System Model

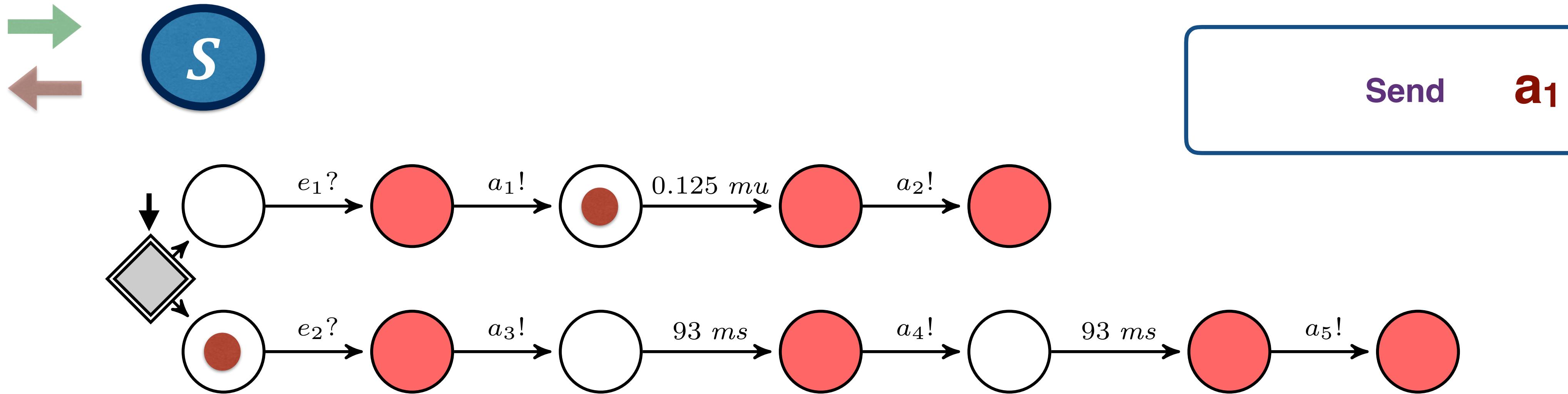


IRTM: System Model



IRTM: System Model

Simulation

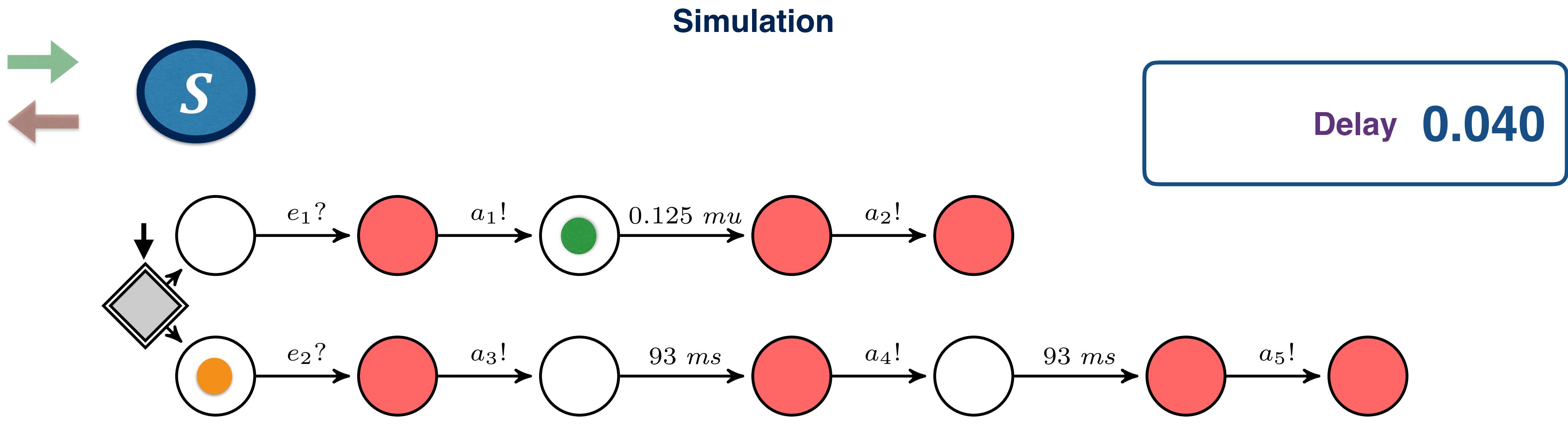


State: $\langle 0, 3 \rangle [\underline{c_1=0} :: c_2=0] \{ e_1 \}$



$\langle a_1, 0 \rangle$

IRTM: System Model

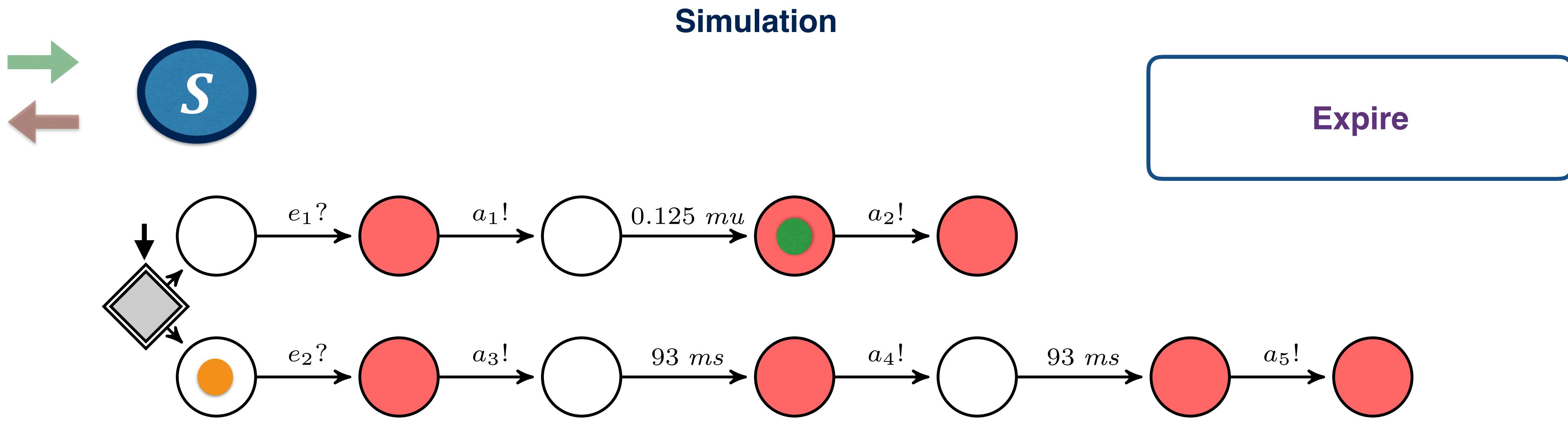


State: $\langle 0.040, 0 \rangle \left[\underline{C_1=0.040 :: C_2=0.040} \right] \{ \}$



$\langle a_1, 0 \rangle$

IRTM: System Model

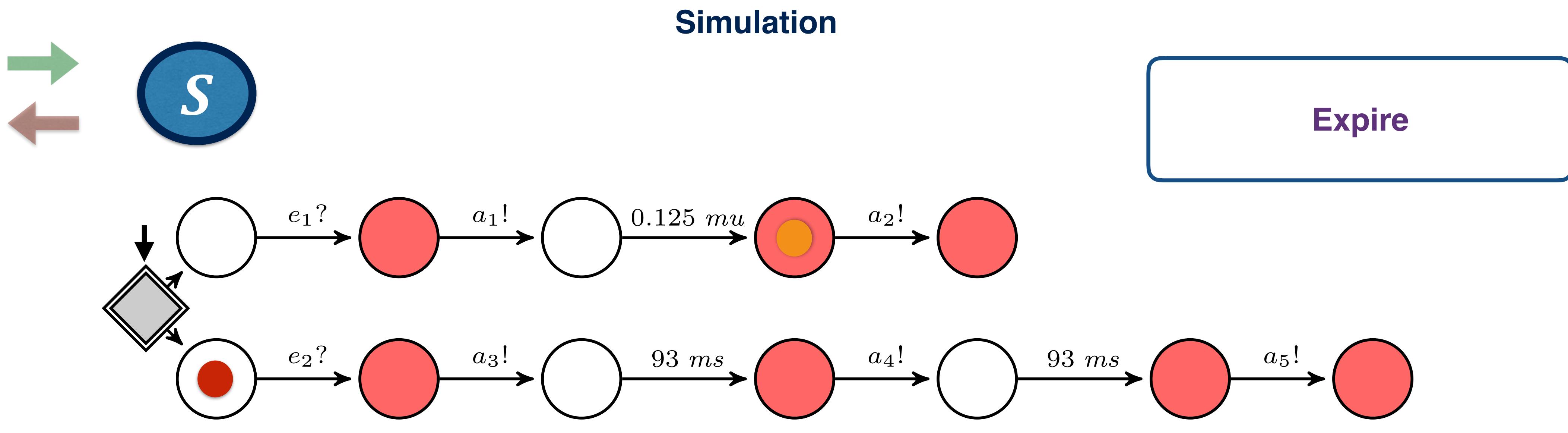


State: $\langle 0.040, 1 \rangle [\underline{c_1=0} :: c_2=0.040] \{ \}$



$\langle a_1, 0 \rangle$

IRTM: System Model

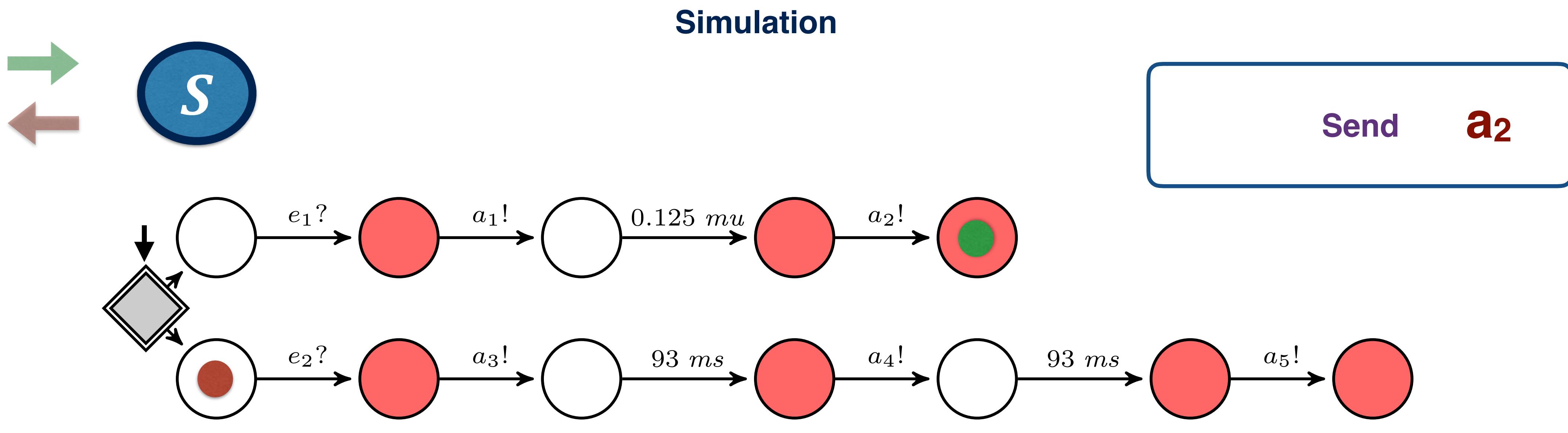


State: $\langle 0.040, 1 \rangle [\underline{c_1=0} :: c_2=0.040] \{ \}$



$\langle a_1, 0 \rangle$

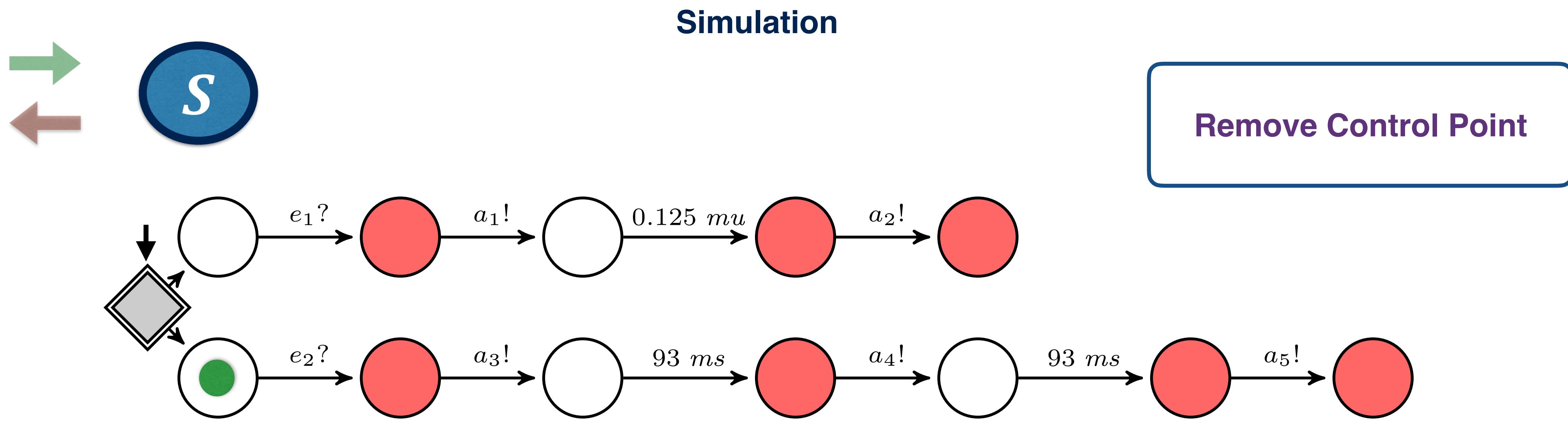
IRTM: System Model



$\langle a_1, 0 \times a_2, 0.040 \rangle$

State: $\langle 0.040, 2 \rangle [\underline{c_1=0} :: c_2=0.040] \{ \}$

IRTM: System Model



Remove Control Point

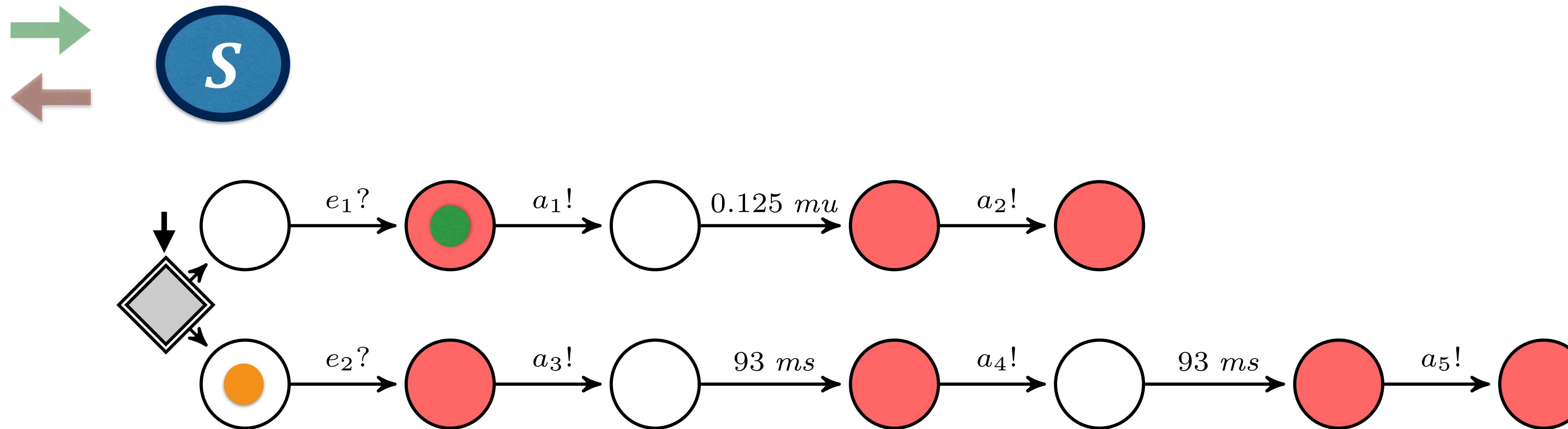
State: $\langle 0.040, 3 \rangle [\underline{c_2=0.040}] \{ \}$



$\langle a_1, 0 \times a_2, 0.040 \rangle$

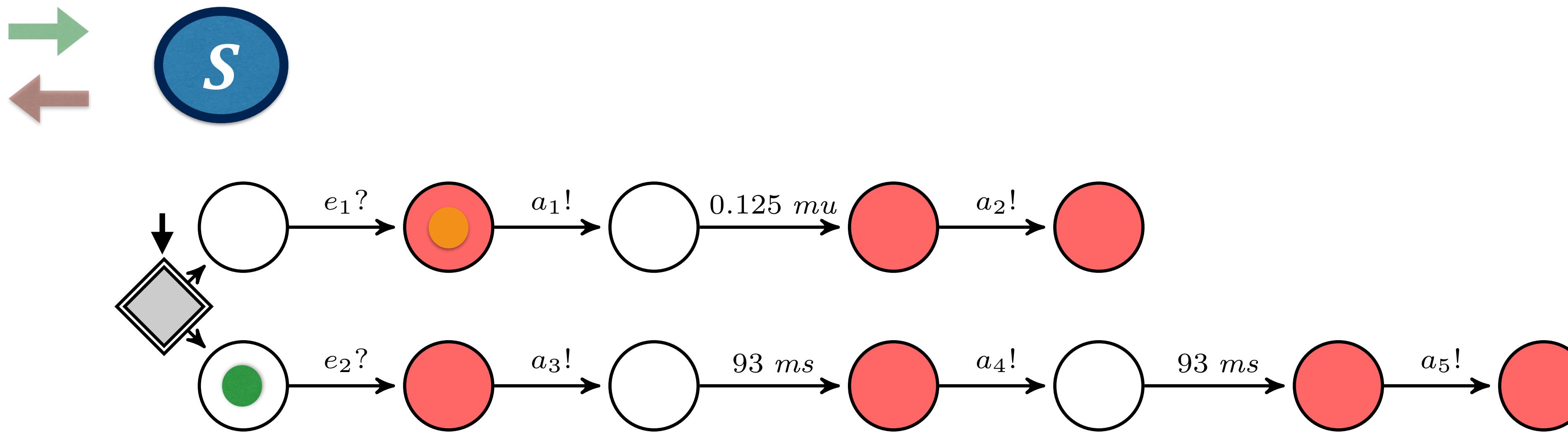
IRTM: System Model

Simulation



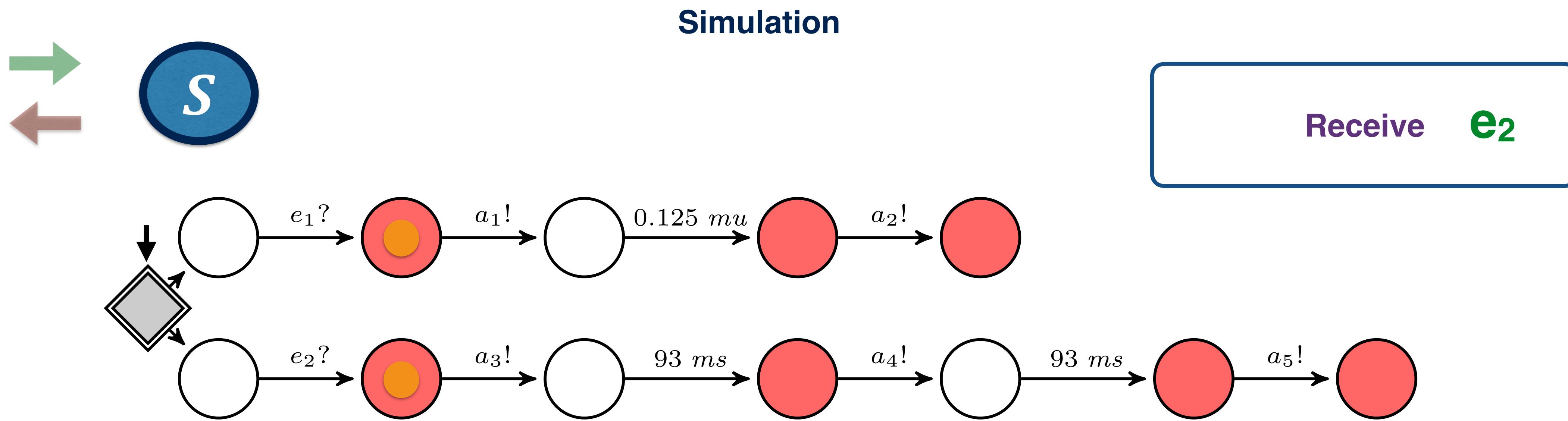
IRTM: System Model

Simulation



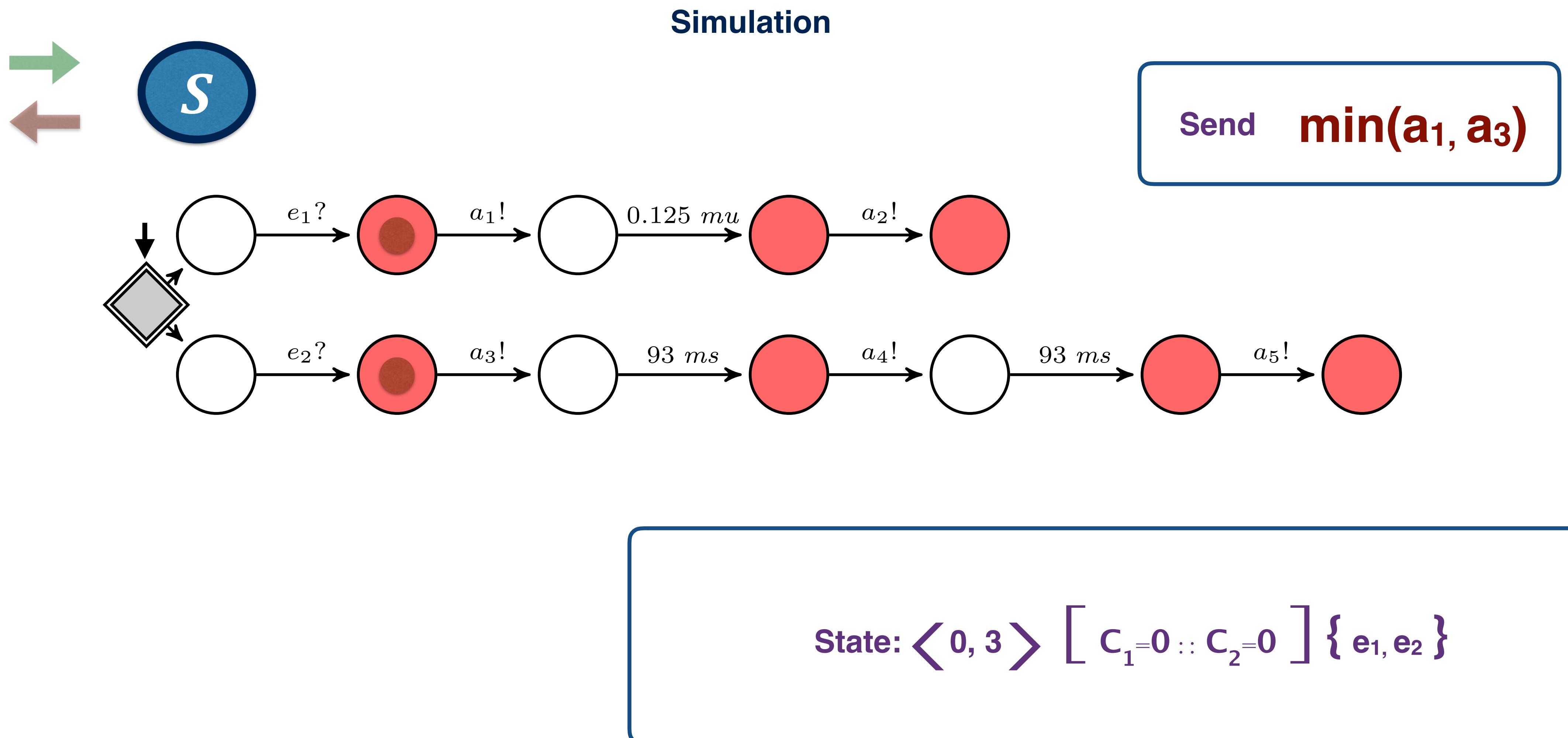
State: $\langle 0, 2 \rangle [c_1=0 :: \underline{c_2=0}] \{ e_1, e_2 \}$

IRTM: System Model

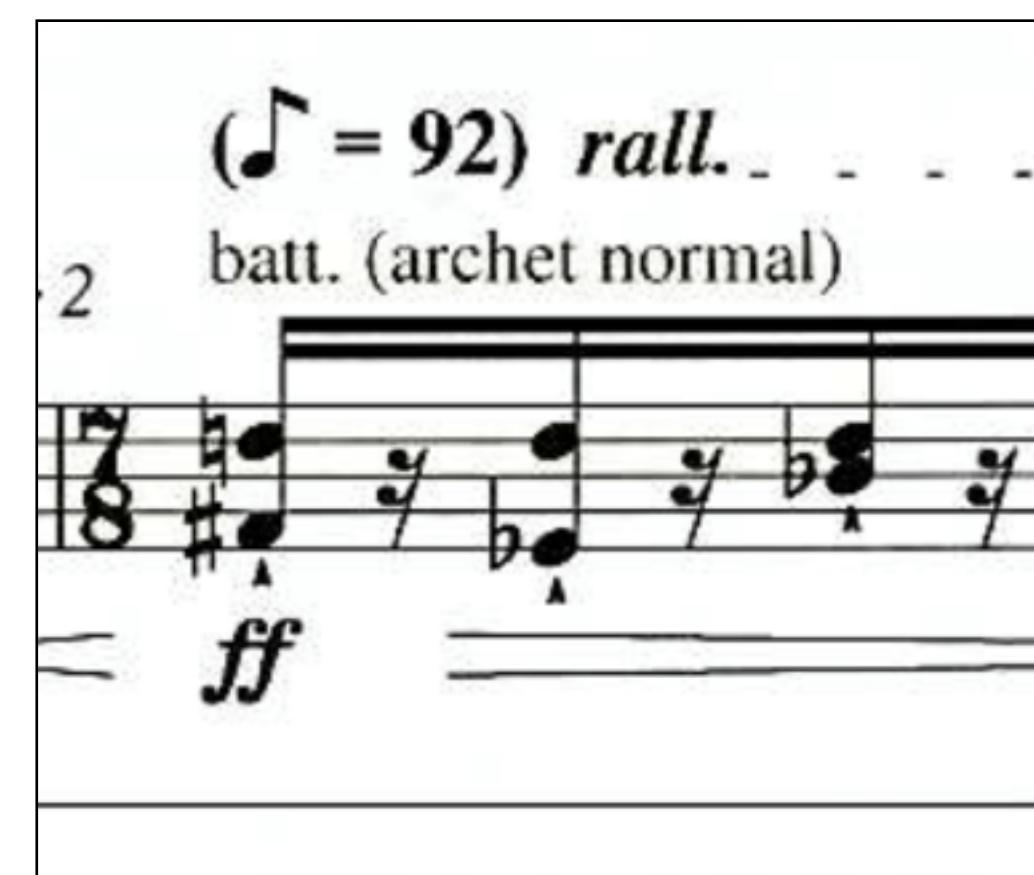
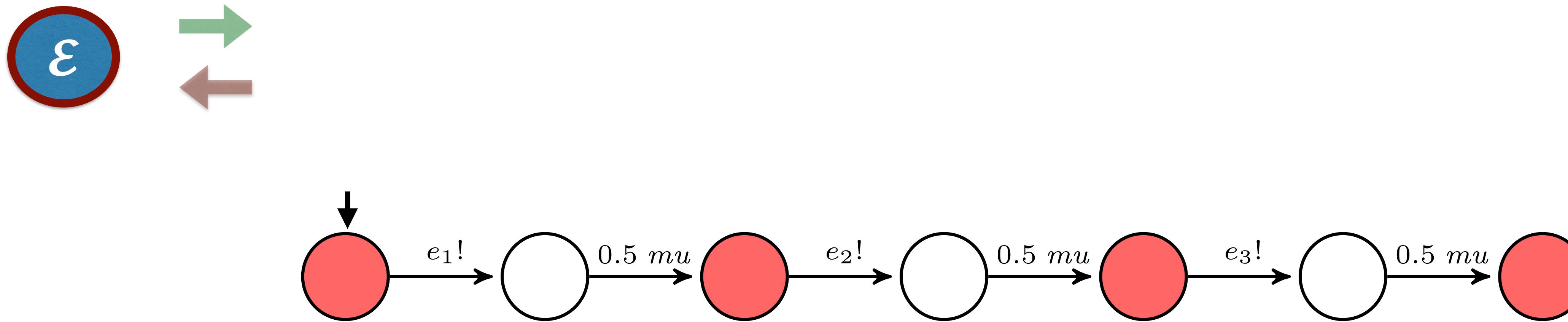


State: $\langle 0, 3 \rangle [c_1=0 :: c_2=0] \{ e_1, e_2 \}$

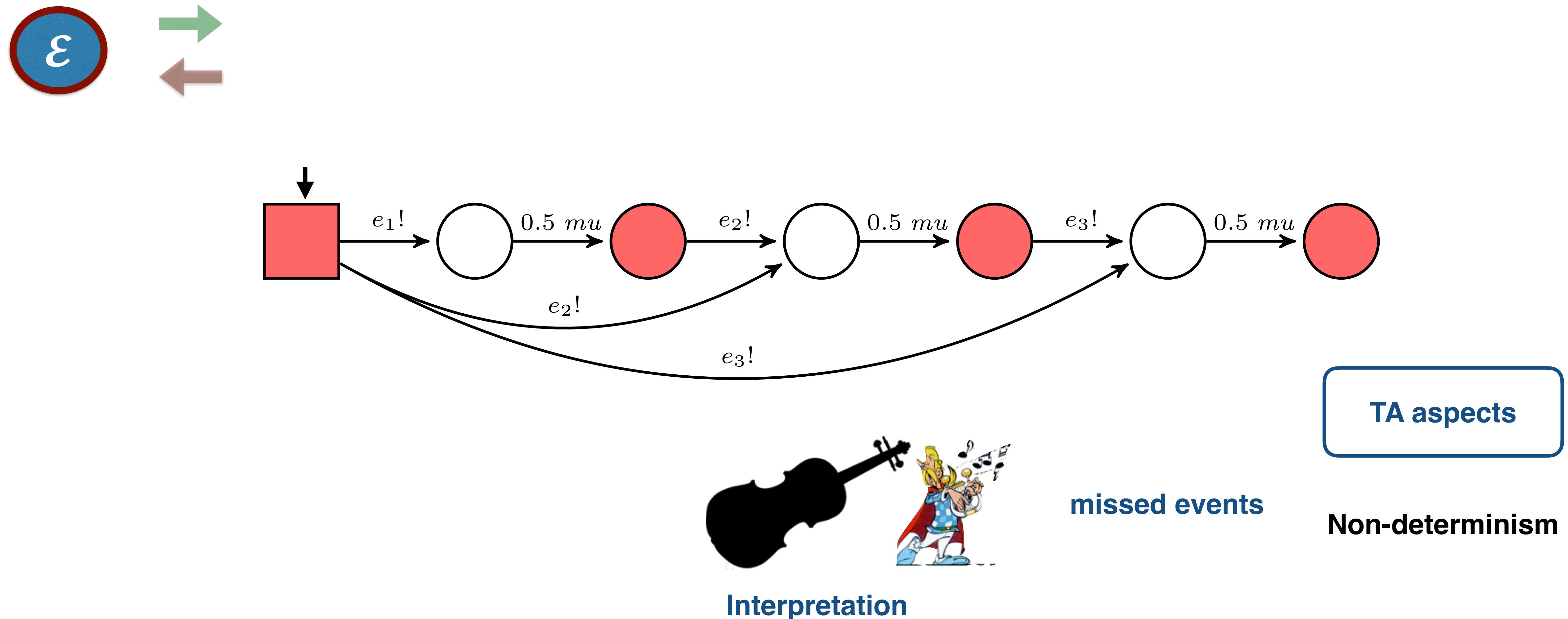
IRTM: System Model



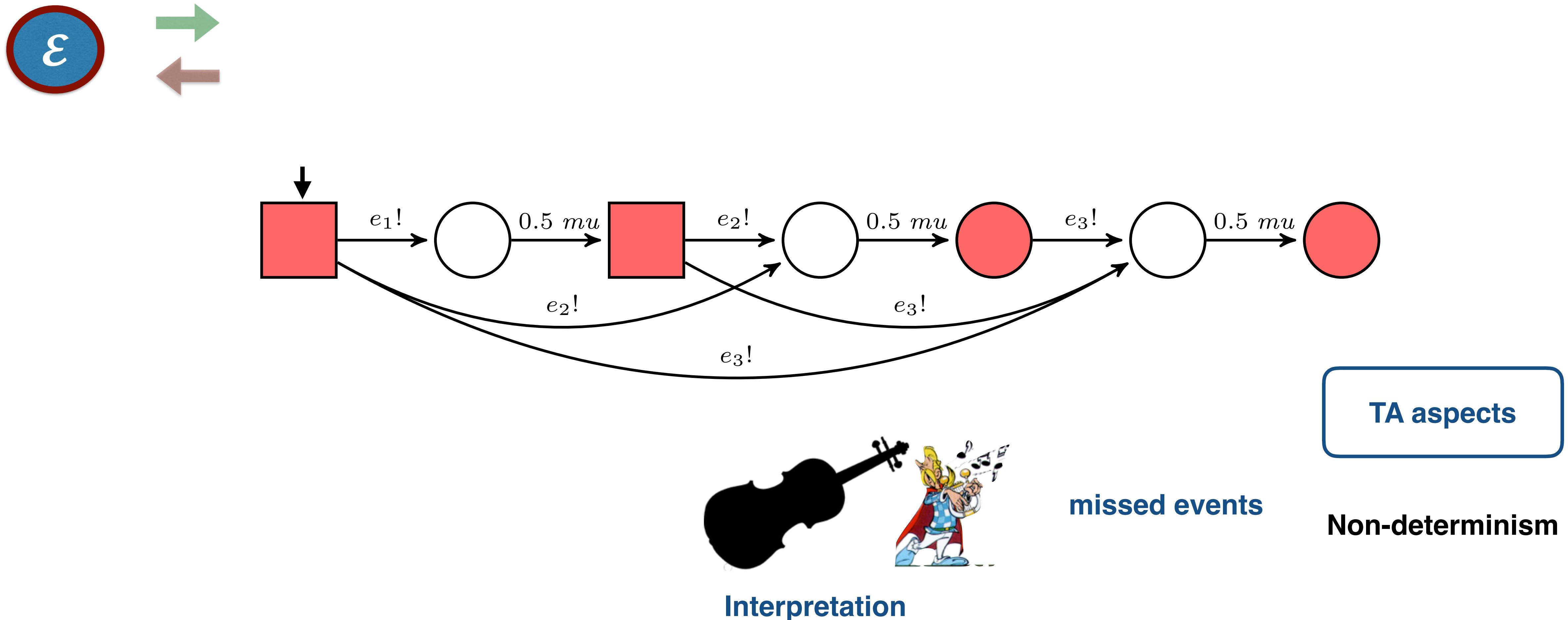
IRTM: Environment Model



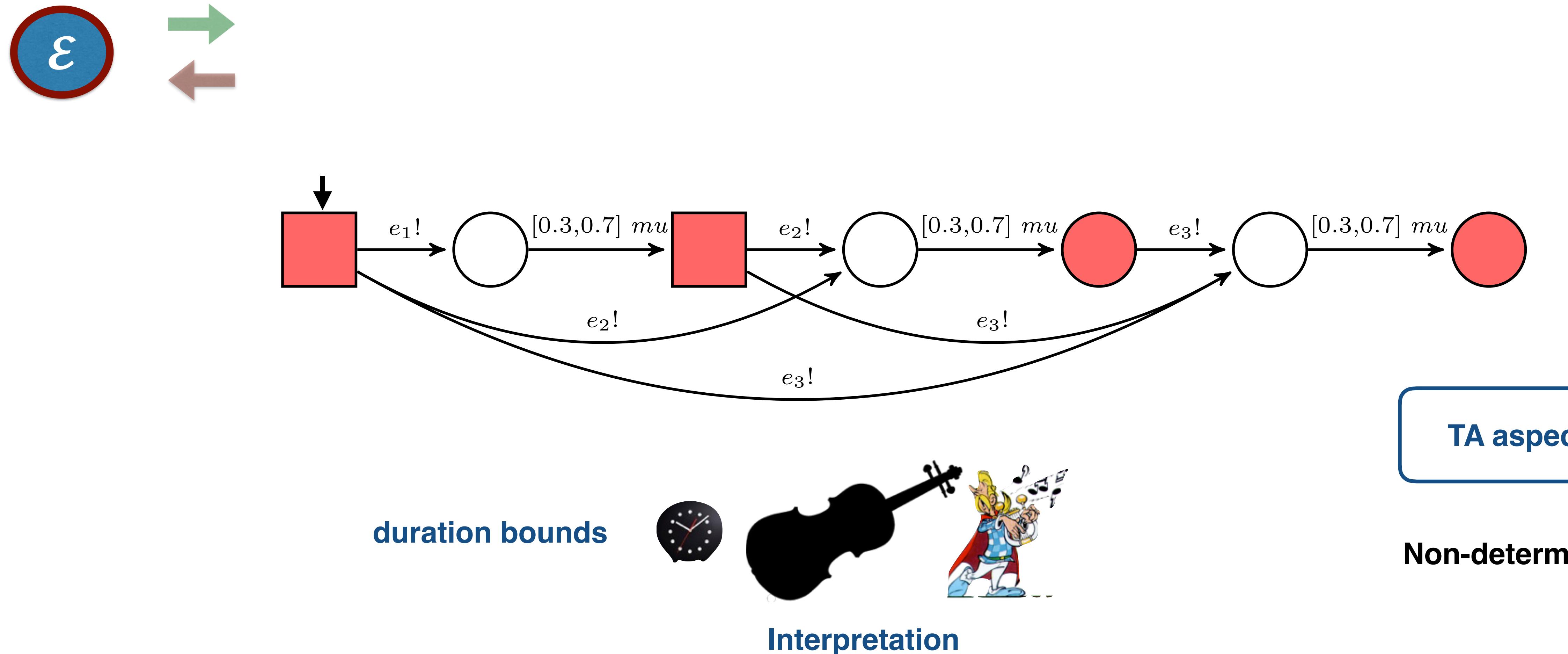
Non-Determinism: missed events



Non-Determinism: missed events



Non-Determinism: duration variation

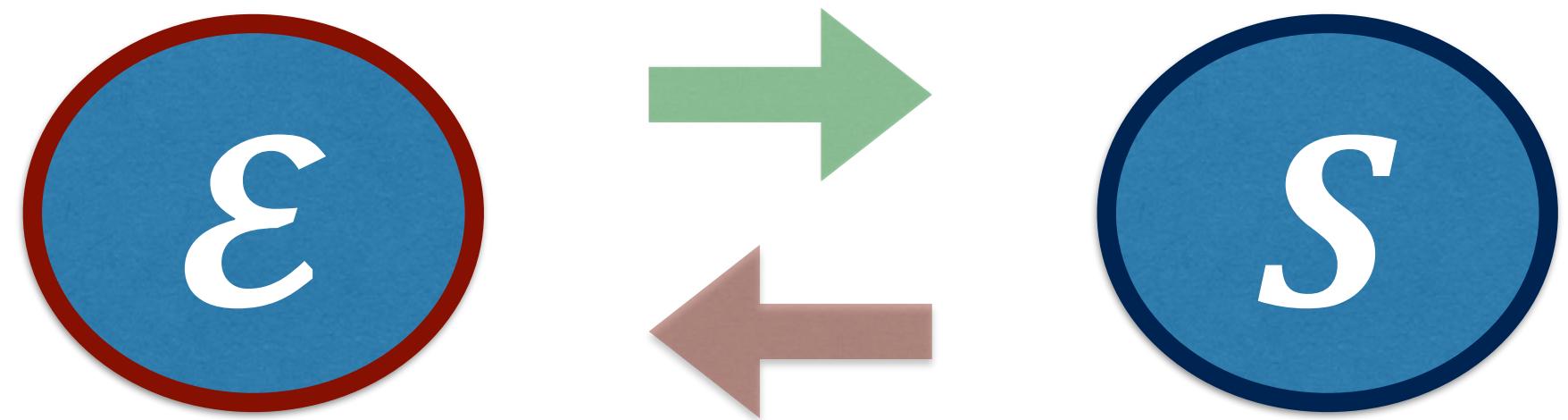


Outline

1.Objectives



2.Interactive Real-Time Model



3.Testing Framework

Contribution

Publications

Poncelet, Jacquemard.
Model-Based Testing for Building Reliable Realtime Interactive Music Systems. Science of Computer Programming (SCP, 2016).

Burloiu, Cont, Poncelet. A visual framework for dynamic mixed music notation.
Journal of New Music Research (JNMR, 2016).

C. Poncelet, F. Jacquemard.
An automatic test framework for interactive music systems.
Journal of New Music Research (JNMR), 2016.

Poncelet, Jacquemard.
Model Based Testing of an Interactive Music System. 30th ACM/SIGAPP Symposium Computing (ACM SAC, 2015).

C. Poncelet, F. Jacquemard.
Test Methods for Score-Based Interactive Music Systems.
ICMC - SMS, 2014.

journals

conferences



Developments

Application to Antescofo + Regression tests

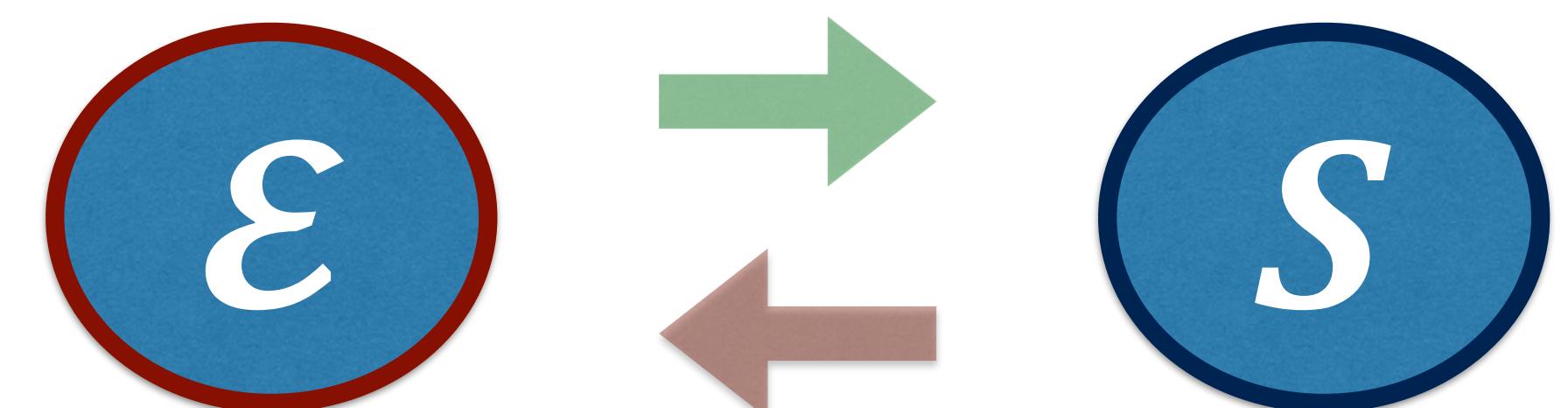
front-end compiler of AntescofoDSL (C++, 13.000 loc).

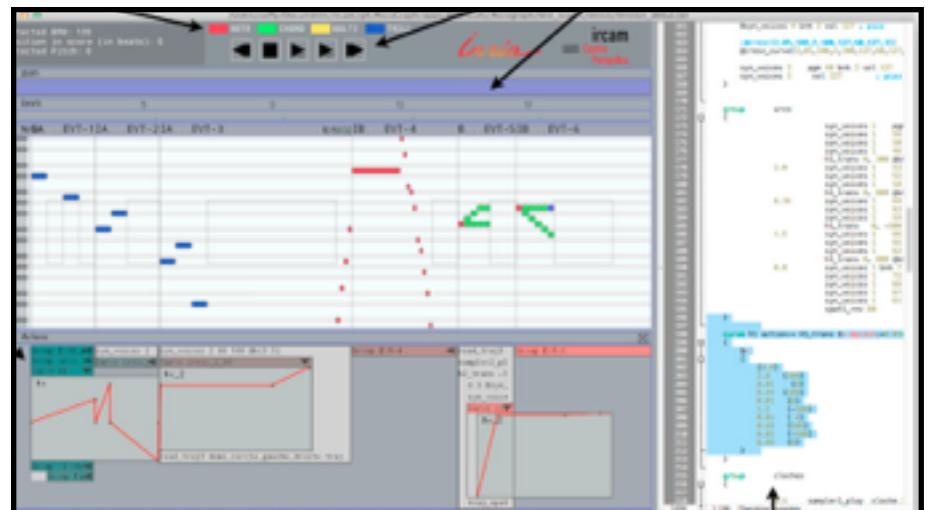
Antescofo adaptors (C++).

~ 20 Scripts for test execution (Perl).

Conformance and trace manager (C++, 4.000 loc).

Virtual Machine (C++, 3.000 loc).





Perspectives

Applications:

- Visual tool for improving framework uses
 - A debug environment with Ascograph
- Application to other IMS (or timed-cyber systems)

Testing Framework:

- Improve Fuzz Testing
 - White-fuzzing Guided-Random (DART)
- Specify a concrete specification language
 - Based on a *Given-When-Then* like paradigm (Gherkin)

Interactive Real-Time Model:

- Translate IRTM into Hybrid Automata
 - add constraints on tempo
- Translate IRTM into Stochastic Automata
 - Improve the input generation

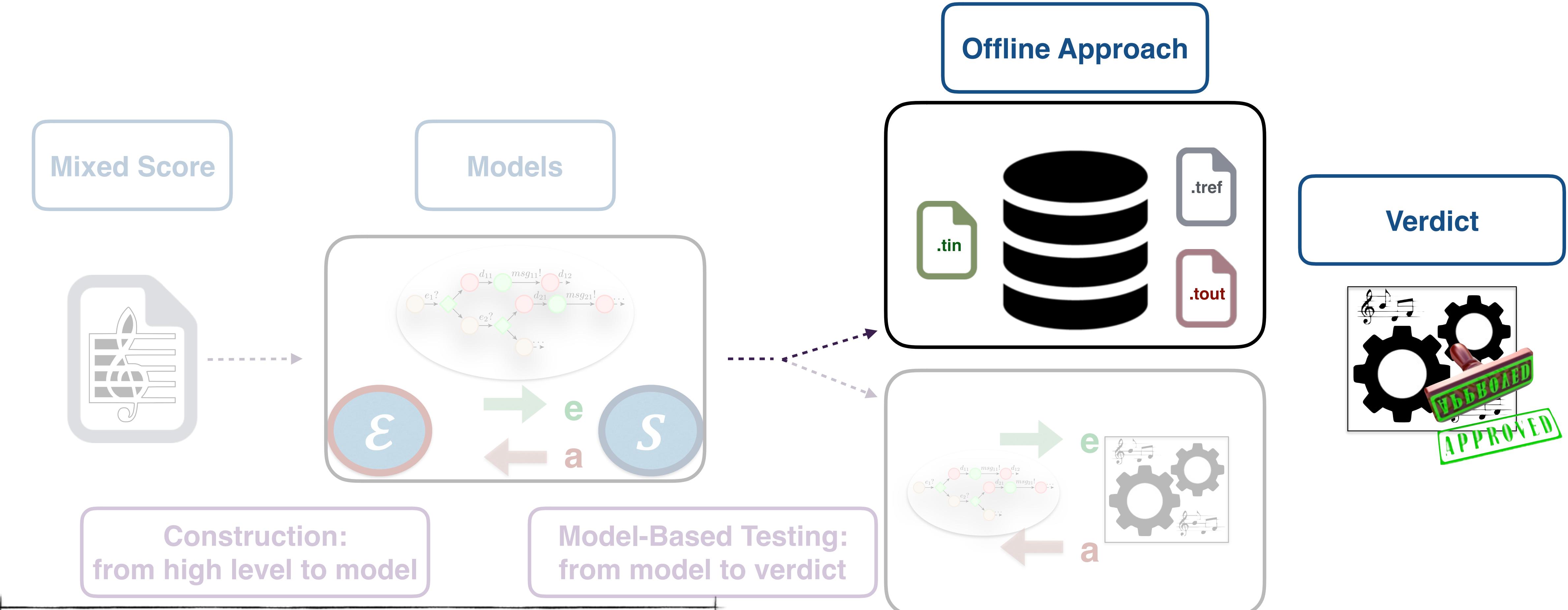
Other Applications:

- Static Analysis of Mixed Score
- Verification of properties

pc7:TestOffline poncelet\$



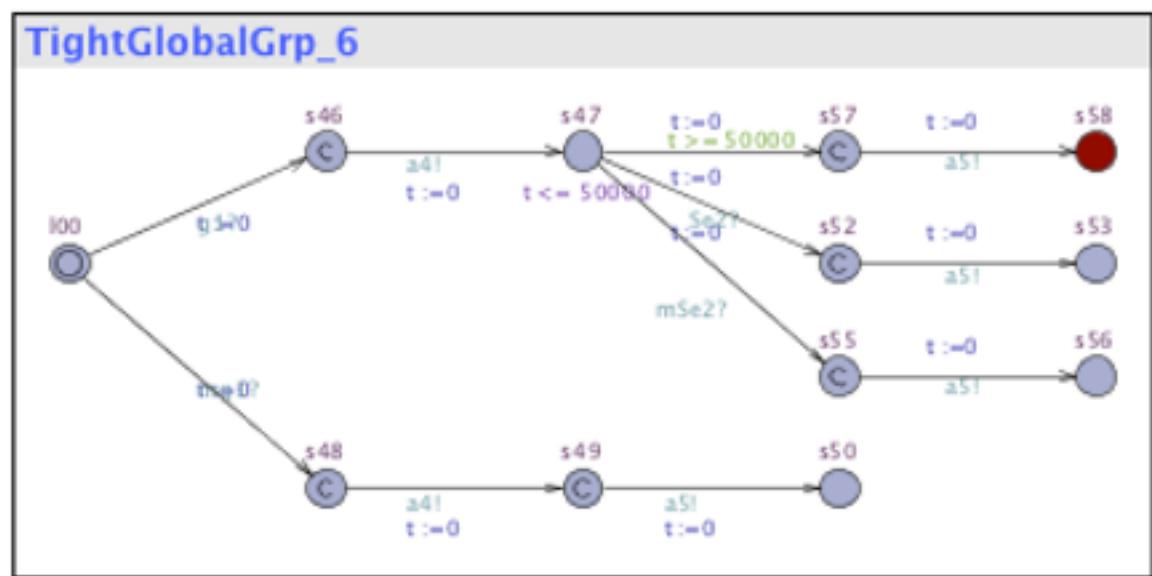
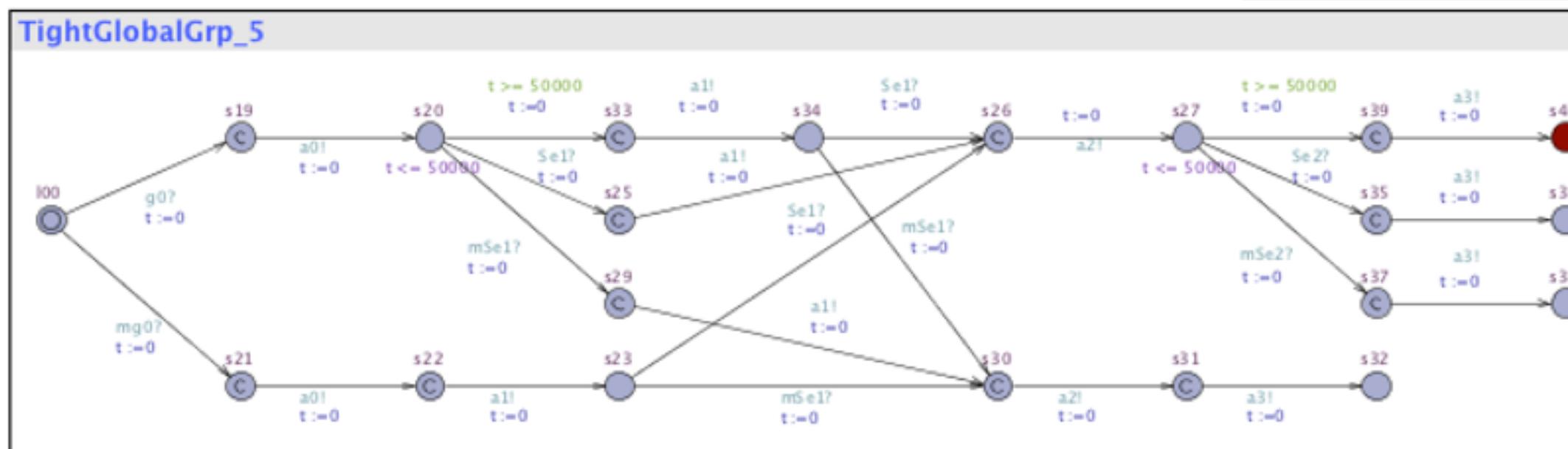
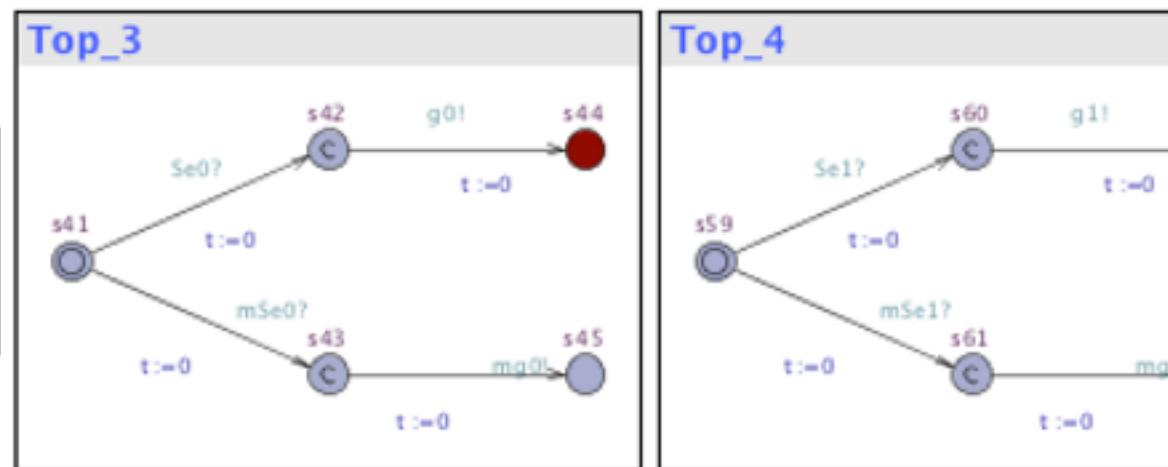
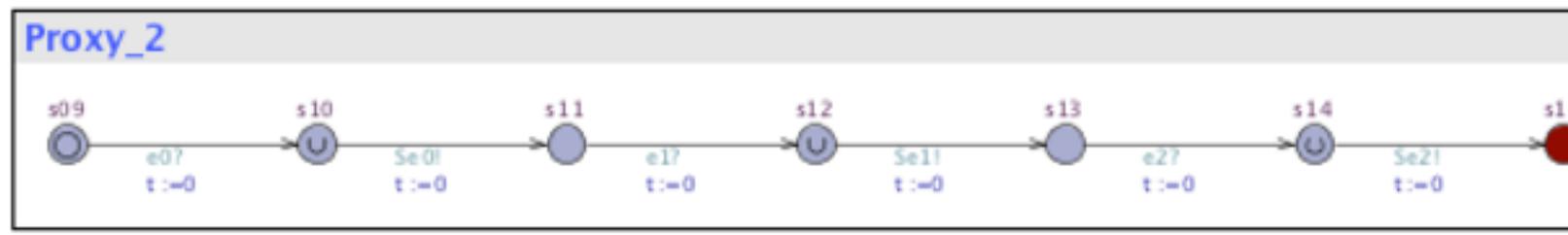
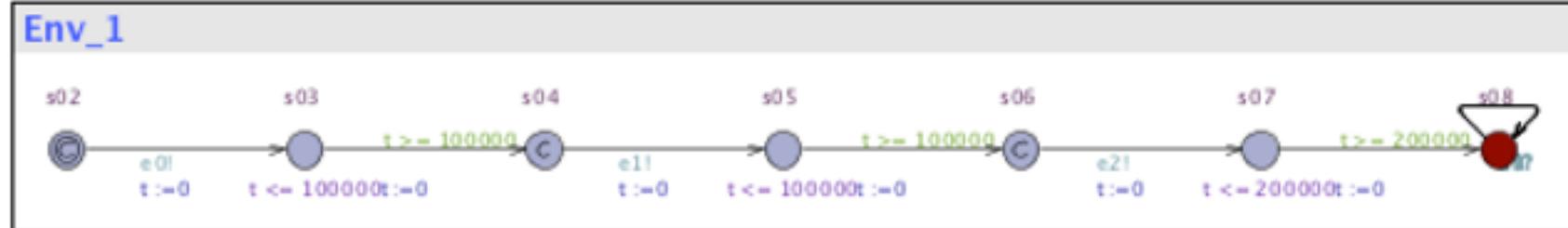
Testing Framework Overview





Uppaal

Translation:
from IRTM into TA



Build
Simulate
Verify

IRTM

TA

under restrictions

A. David, K.G. Larsen, S. Li, M. Mikucionis, B. Nielsen.
Testing real-time systems under uncertainty. FMCO'10.

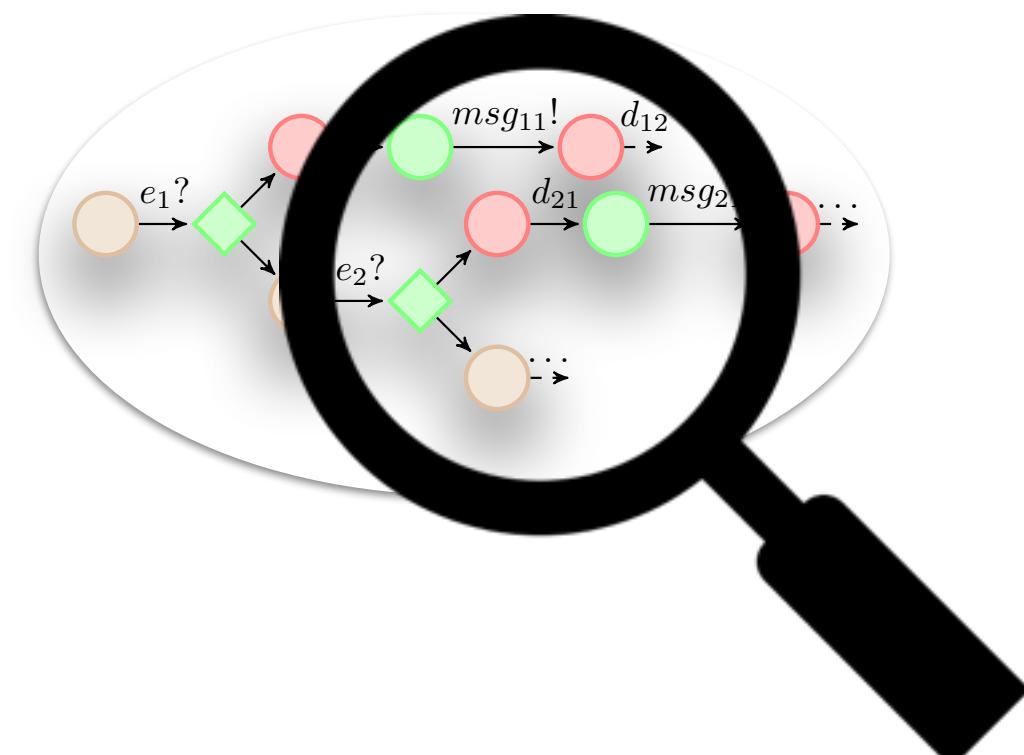
Covering Input Generation



& CoVer

- **Covering generation**
- **Existing Tools**

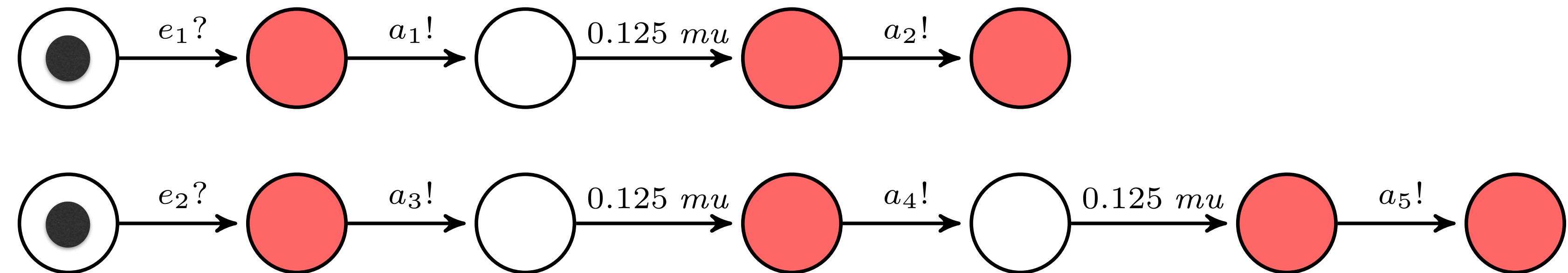
- **Translation into Timed Automata**
- **Generates lowest durations**



covering
queries

observers

Location/Transition/Path



C. Poncelet, F. Jaquemard.

Test Methods for Score-Based Interactive Music Systems.

ICMC - SMS, 2014.

Blom, Hessel, Jonsson, Peterson.

Specifying and Generating Test Cases Using Observer Automata.

FATES'04.

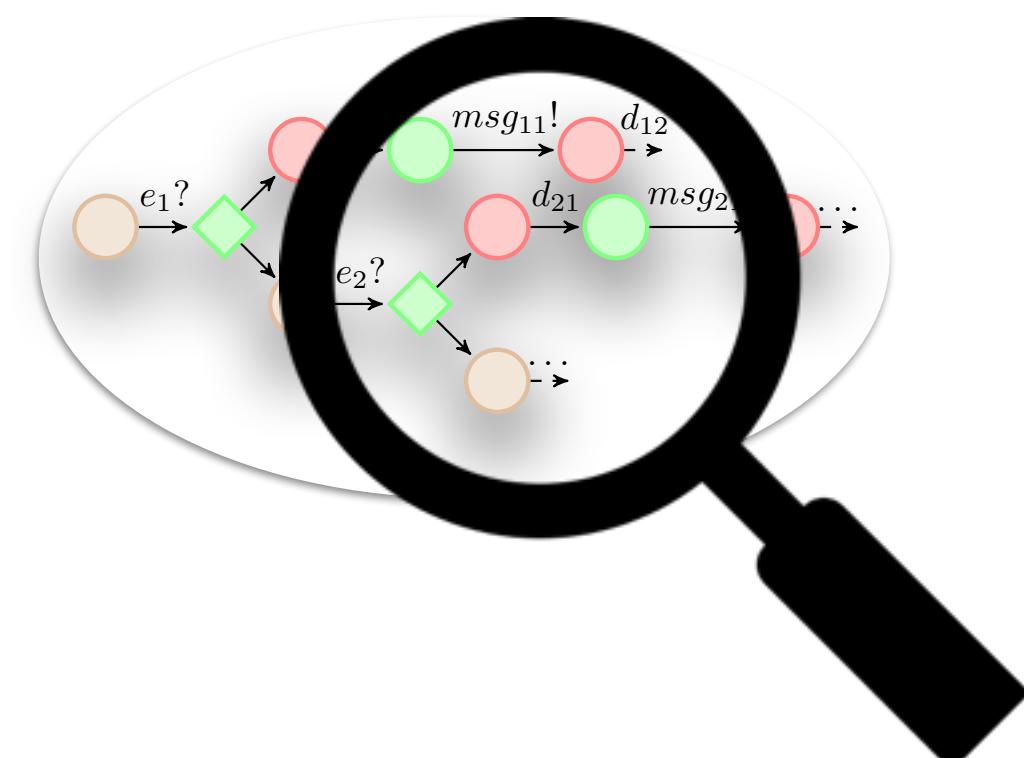
Covering Input Generation



& CoVer

- **Covering generation**
- **Existing Tools**

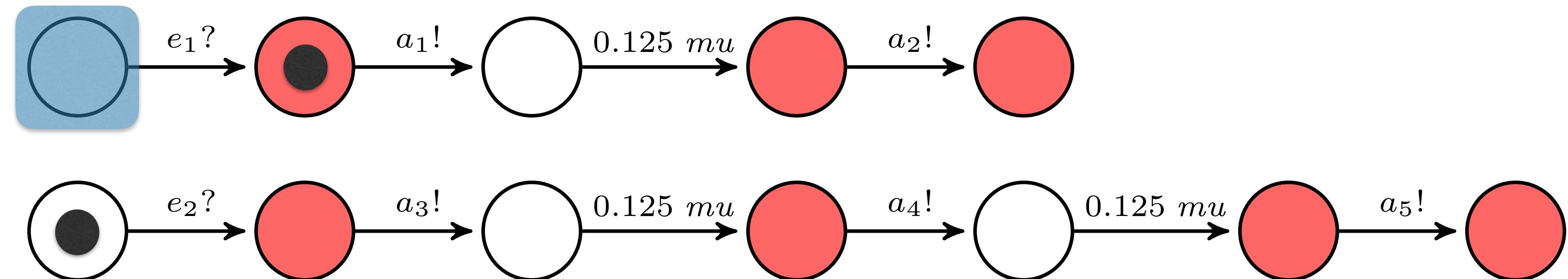
- **Translation into Timed Automata**
- **Generates lowest durations**



covering
queries

observers

Location/Transition/Path



Blom, Hessel, Jonsson, Peterson.
Specifying and Generating Test Cases Using Observer Automata.
FATES'04.

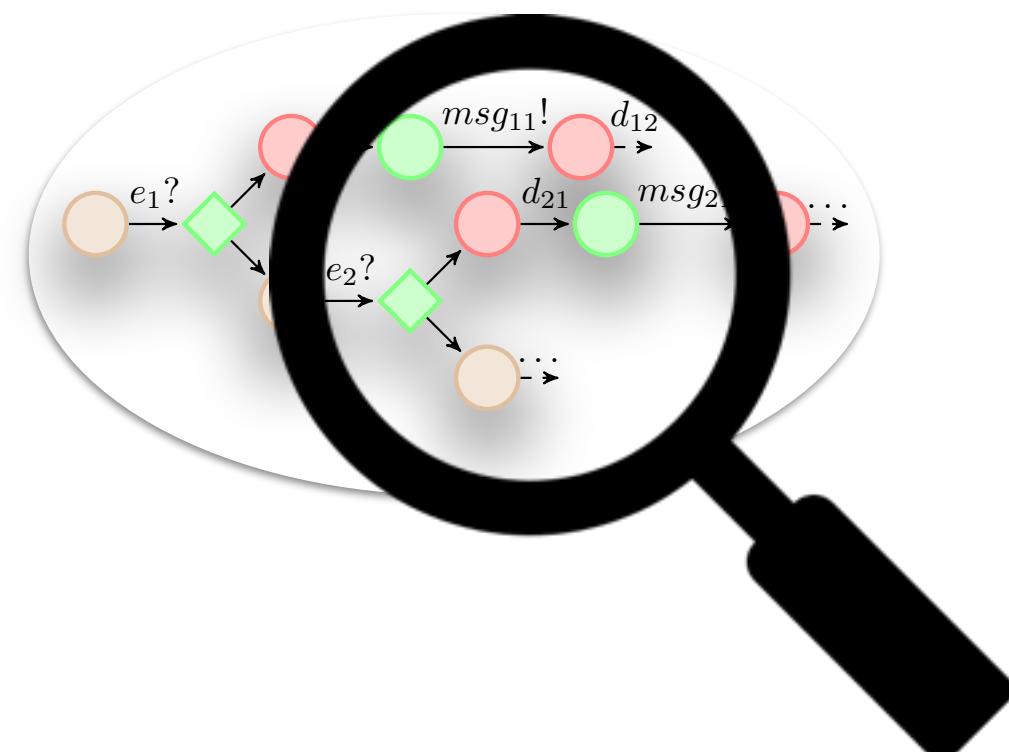
Covering Input Generation



& CoVer

- Covering generation
- Existing Tools

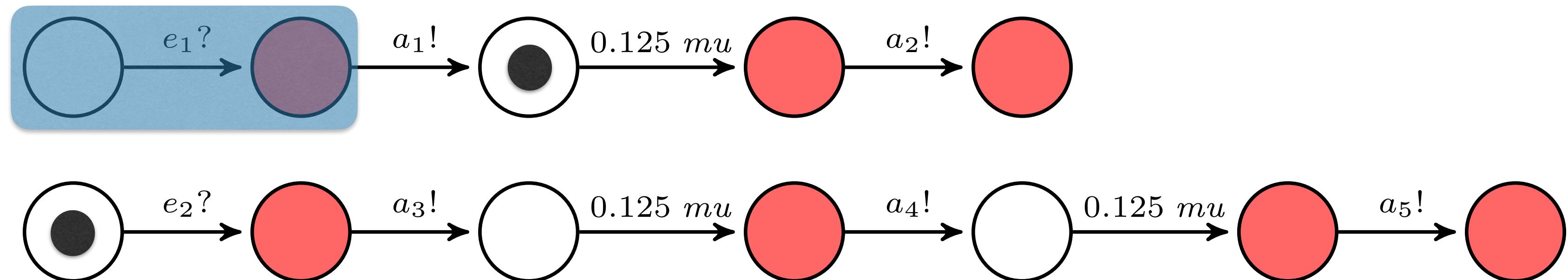
- Translation into Timed Automata
- Generates lowest durations



covering
queries

observers

Location/Transition/Path



Blom, Hessel, Jonsson, Peterson.
Specifying and Generating Test Cases Using Observer Automata.
FATES'04.

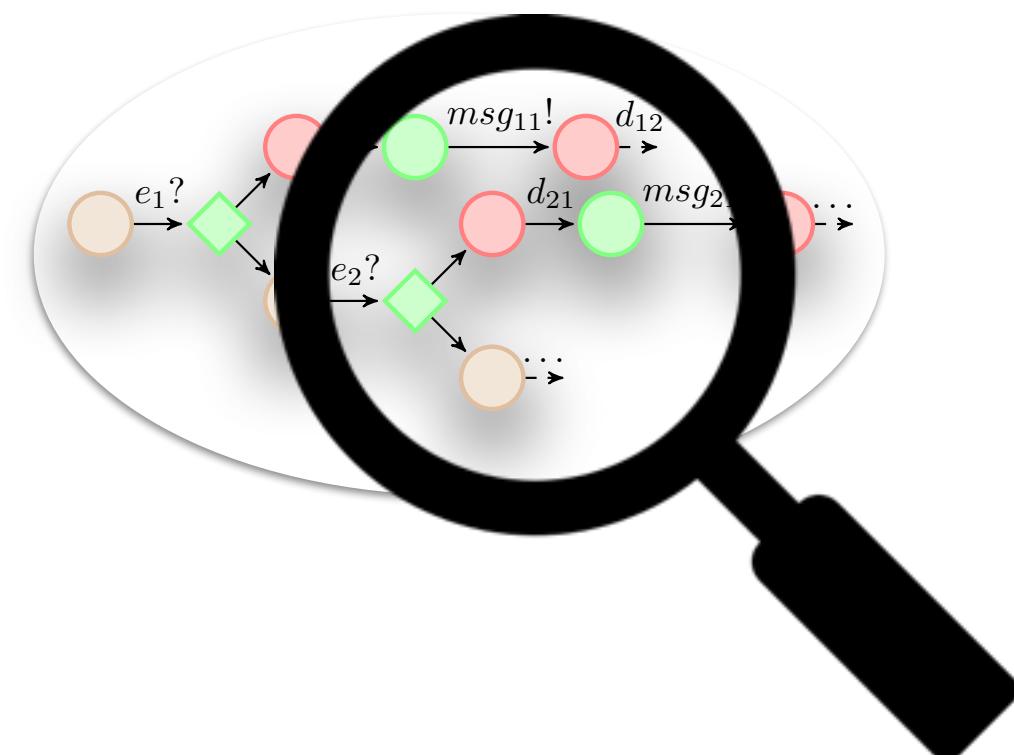
Covering Input Generation



& CoVer

- **Covering generation**
- **Existing Tools**

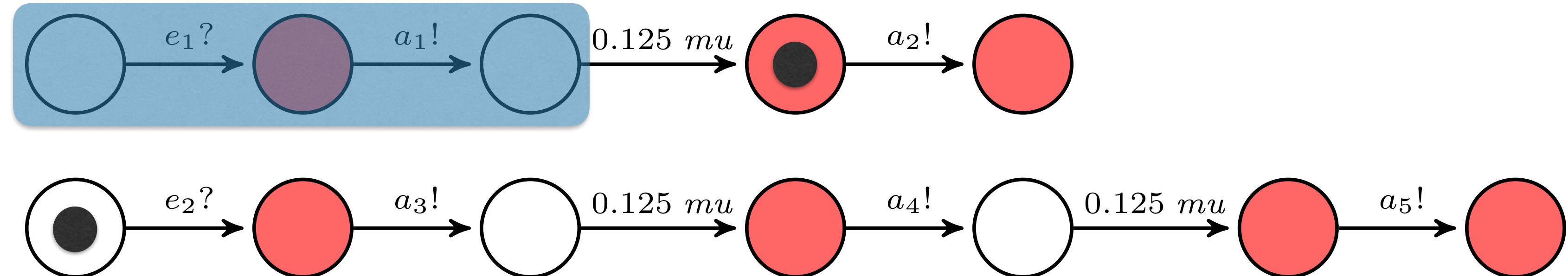
- **Translation into Timed Automata**
- **Generates lowest durations**



covering
queries

observers

Location/Transition/Path



Blom, Hessel, Jonsson, Peterson.
Specifying and Generating Test Cases Using Observer Automata.
FATES'04.

Random

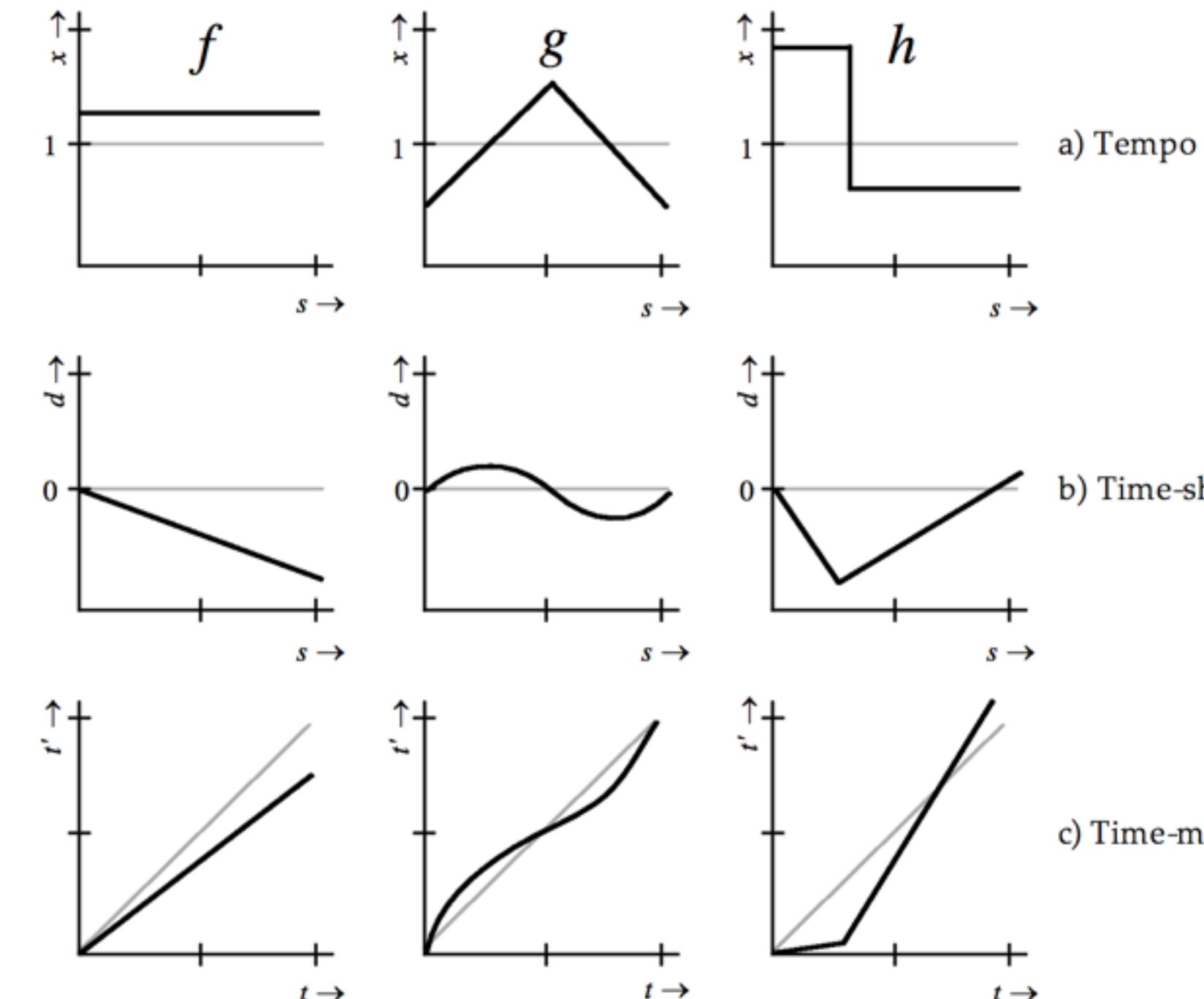
Time Functions
(TIF)

- Musically relevant
- No translation

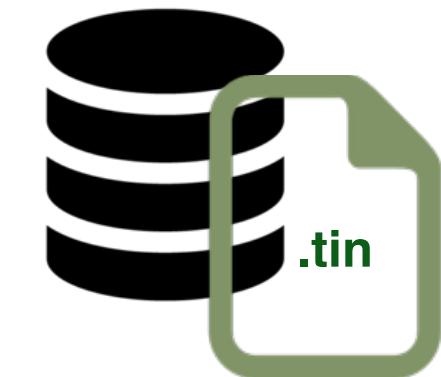
• No coverage guarantee



Fuzz Generation



reference
trace

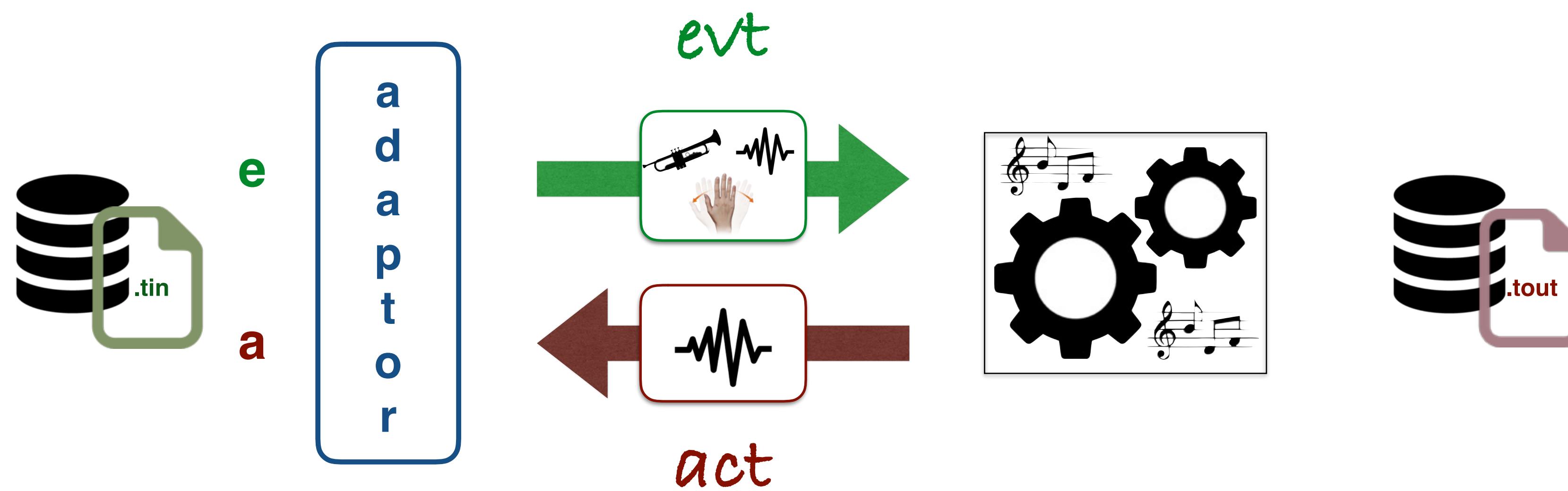


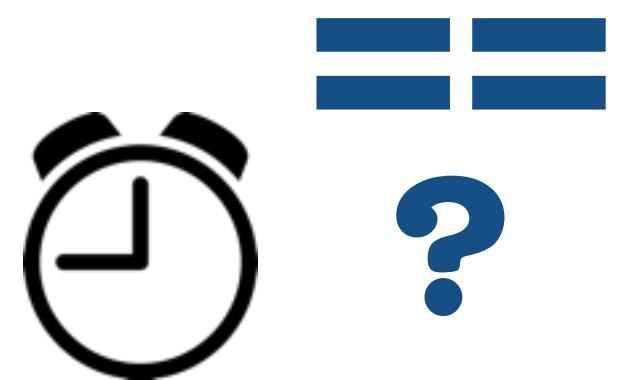
Interpretation = local shift and global tempo changes

Henkjan Honing.

From Time to Time: The Representation of Timing and Tempo. Computer Music Journal. 2001.

Execution





Timed Conformance

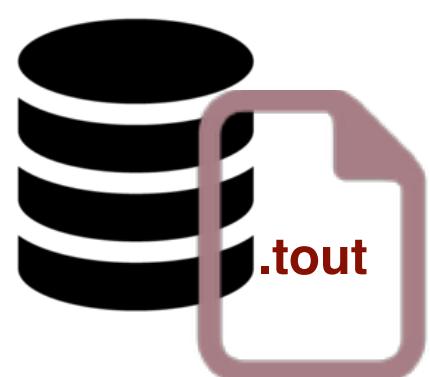
Definition:

Timed conformance:

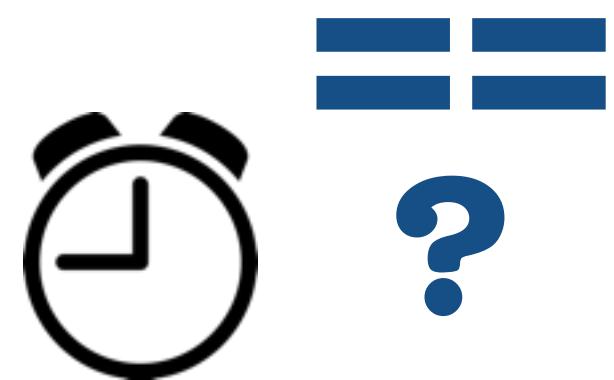
Set inclusion of real timed output traces
into the expected timed output traces


$$\langle a_1, 0 \times a_2, 0.040 \times a_3, 0.080 \rangle$$

Expected Trace


$$\langle a_1, 0 \times a_2, 0.040 \times a_3, 0.080 \rangle$$

Real Trace



Timed Conformance

Definition:

Timed conformance:

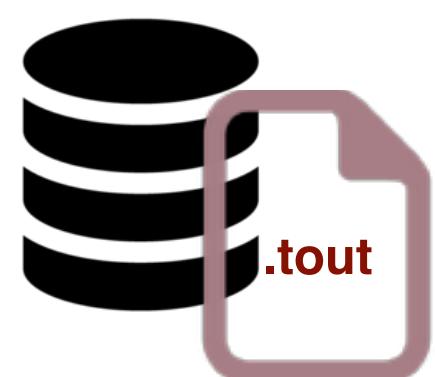
Set inclusion of real timed output traces
into the expected timed output traces

Missed actions



$\langle a_1, 0 \rangle \times a_2, 0.040 \times a_3, 0.080 \rangle$

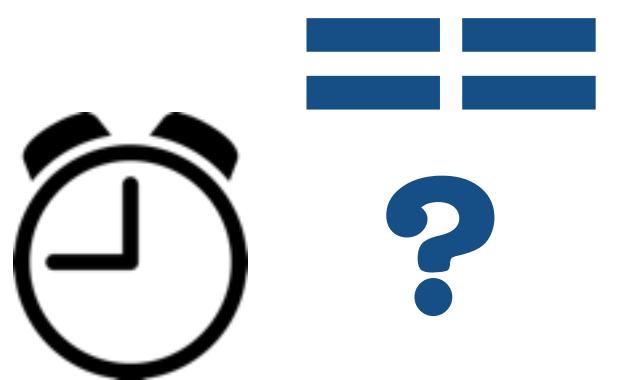
Expected Trace



$\langle a_1, 0 \rangle$

$\langle a_3, 0.080 \rangle$

Real Trace



Timed Conformance

Definition:

Timed conformance:

Set inclusion of real timed output traces
into the expected timed output traces

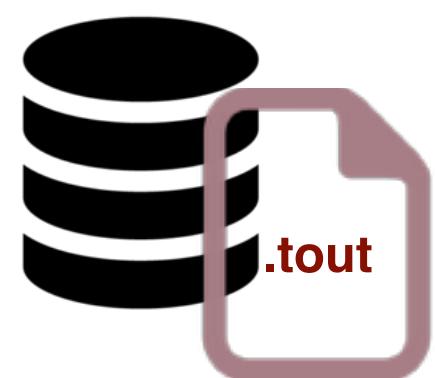
Unexpected actions



$\langle a_1, 0 \rangle$

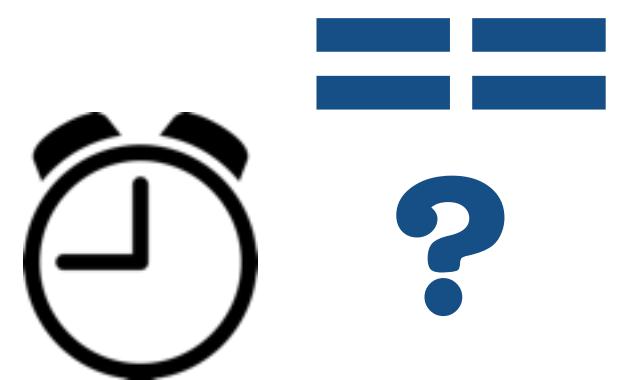
$\langle a_3, 0.080 \rangle$

Expected Trace



$\langle a_1, 0 \rangle \times a_2, 0.040 \times a_3, 0.080 \rangle$

Real Trace



Timed Conformance

Definition:

Timed conformance:

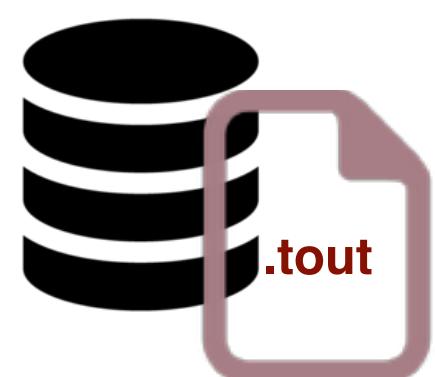
Set inclusion of real timed output traces
into the expected timed output traces

$\Delta > \epsilon$



$\langle a_1, 0 \times a_2, 0.040 \times a_3, 0.080 \rangle$

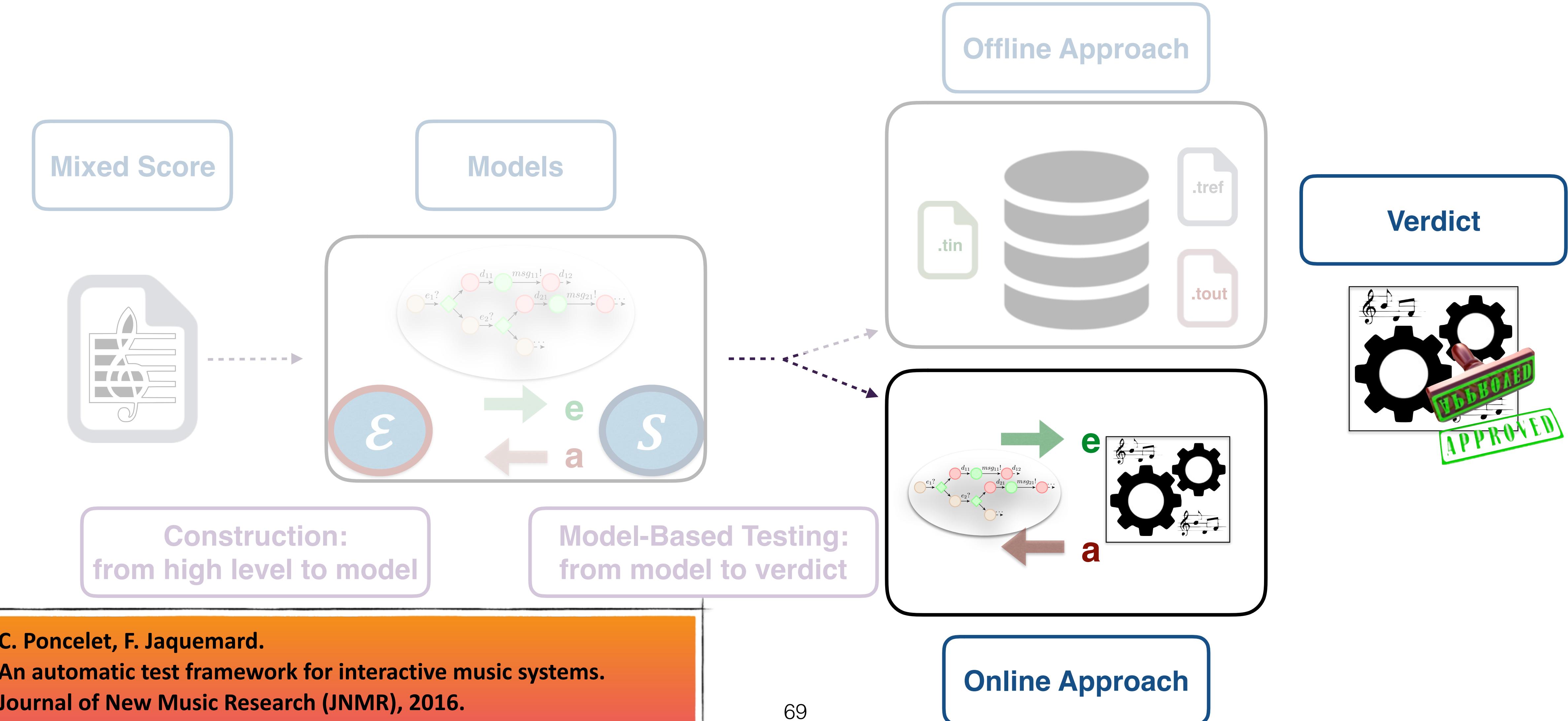
Expected Trace



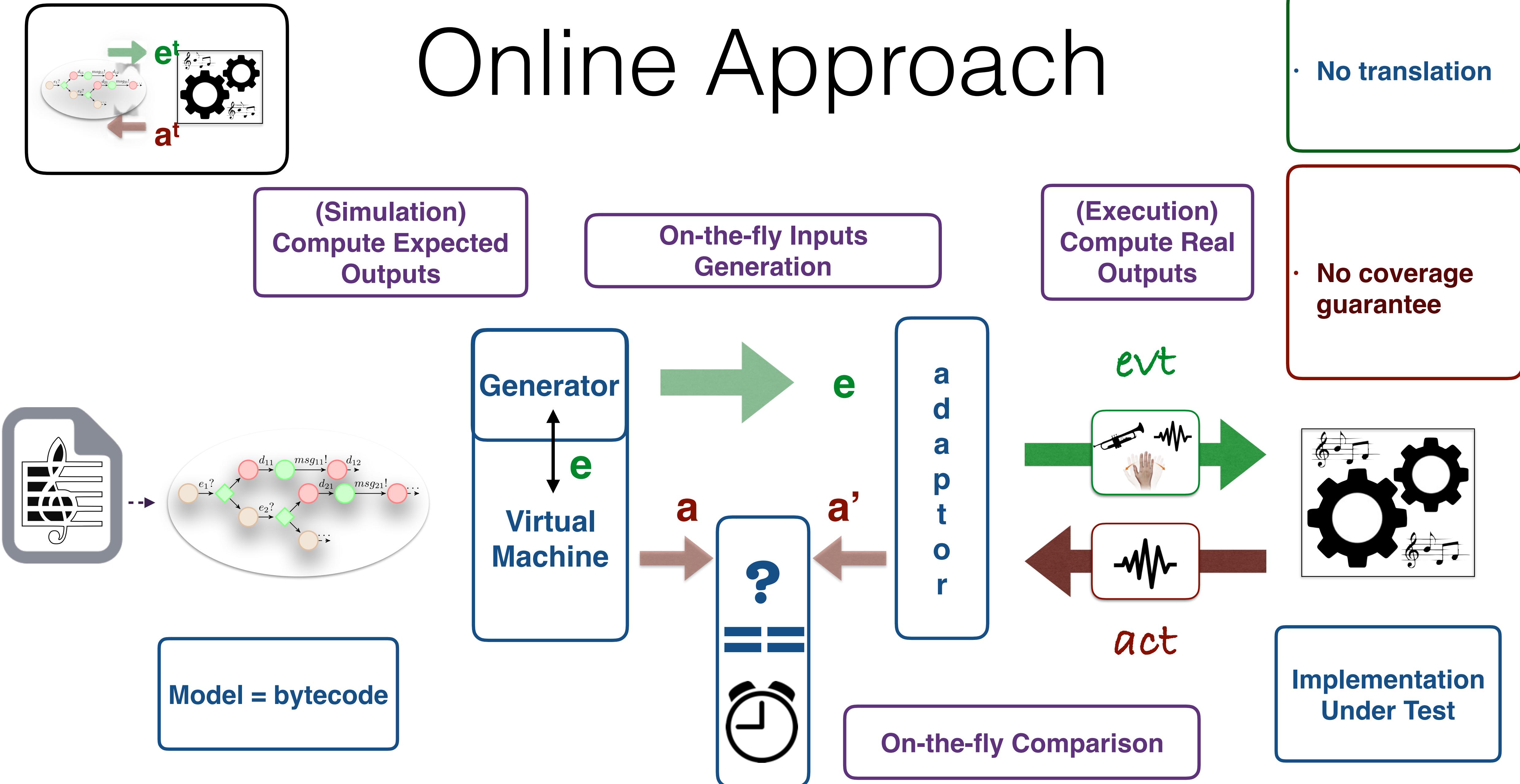
$\langle a_1, 0 \times a_2, 0.040 \times a_3, 0.090 \rangle$

Real Trace

Testing Framework Overview



Online Approach

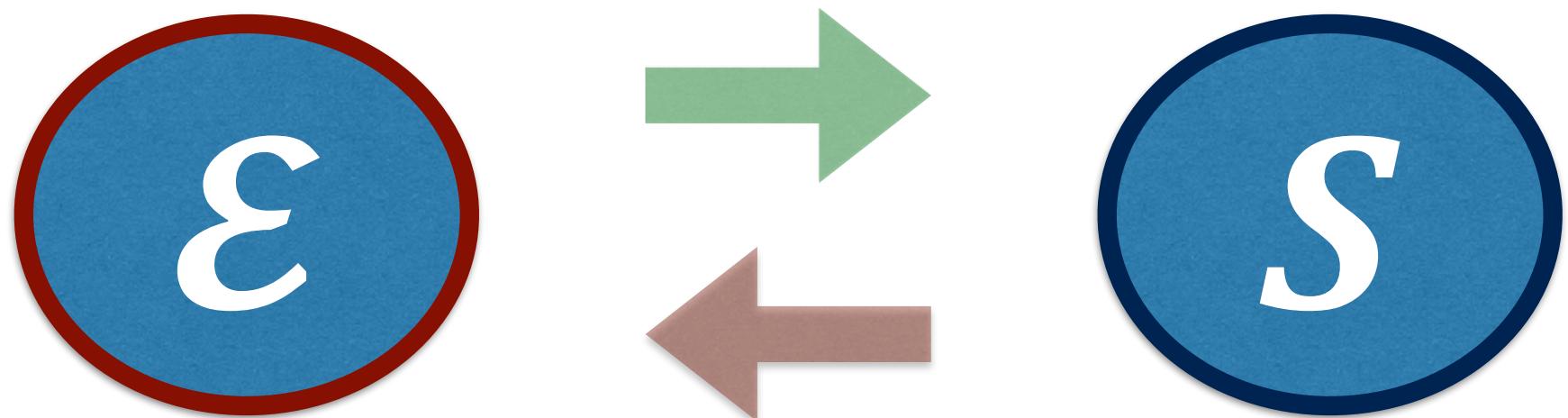


Outline

1. Objectives

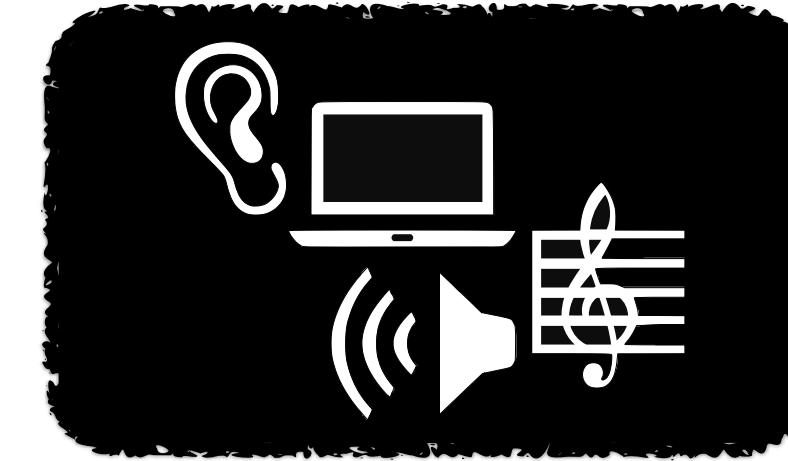


2. Interactive Real-Time Model



3. Testing Framework

4. Application to Antescofo



Antescofo

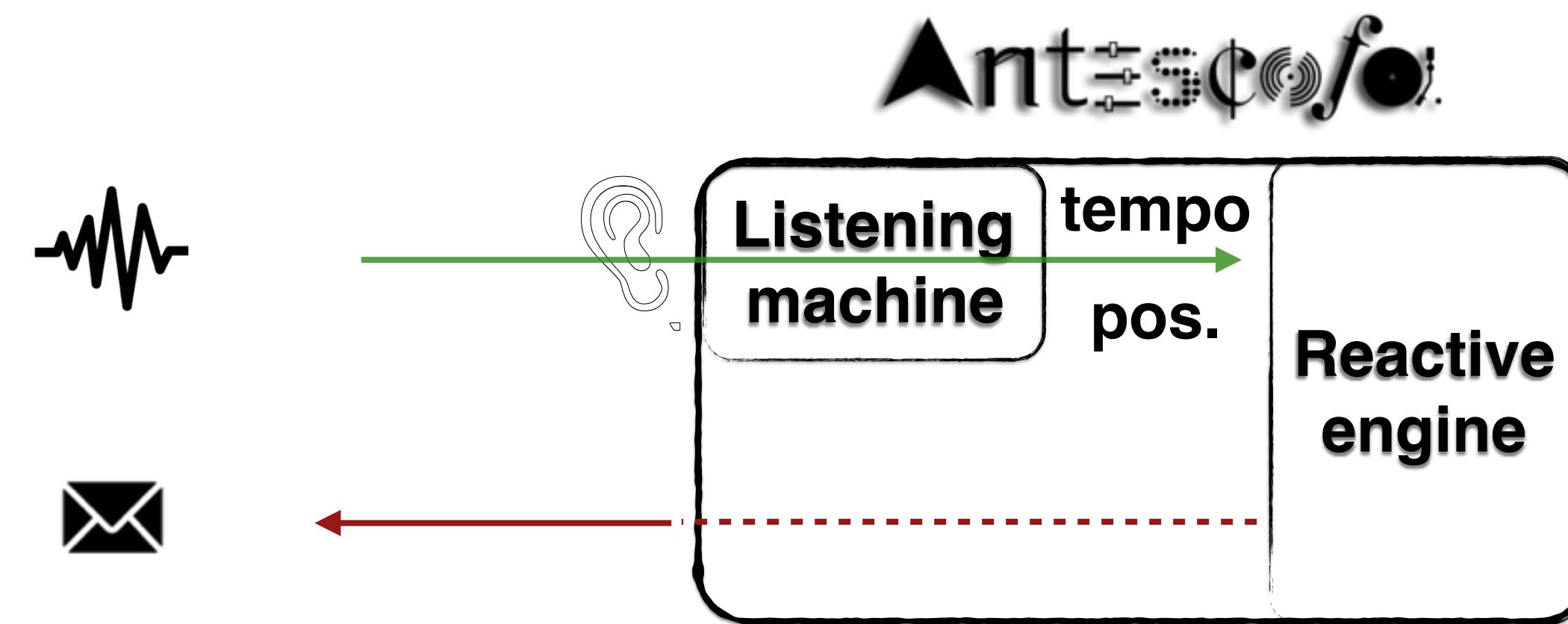
Application to Antescofo



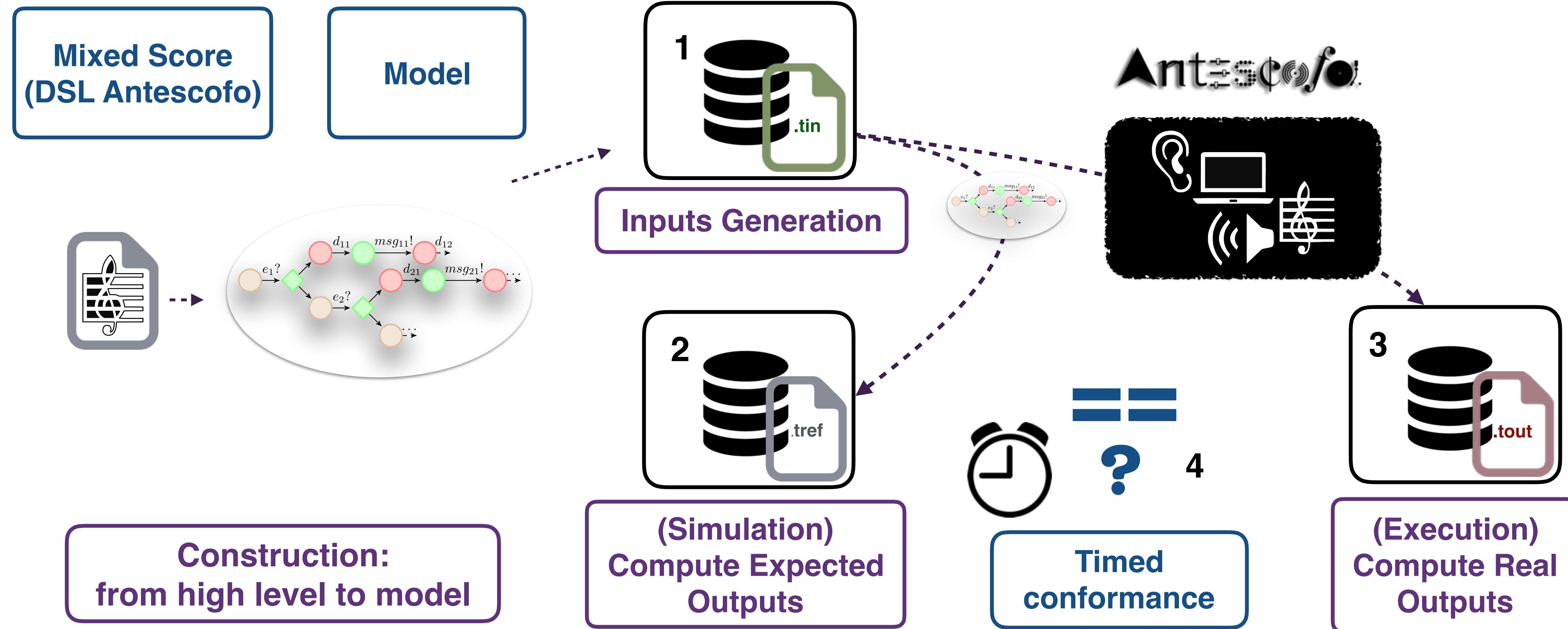
Antescofo



Antescofo



Offline Approaches application

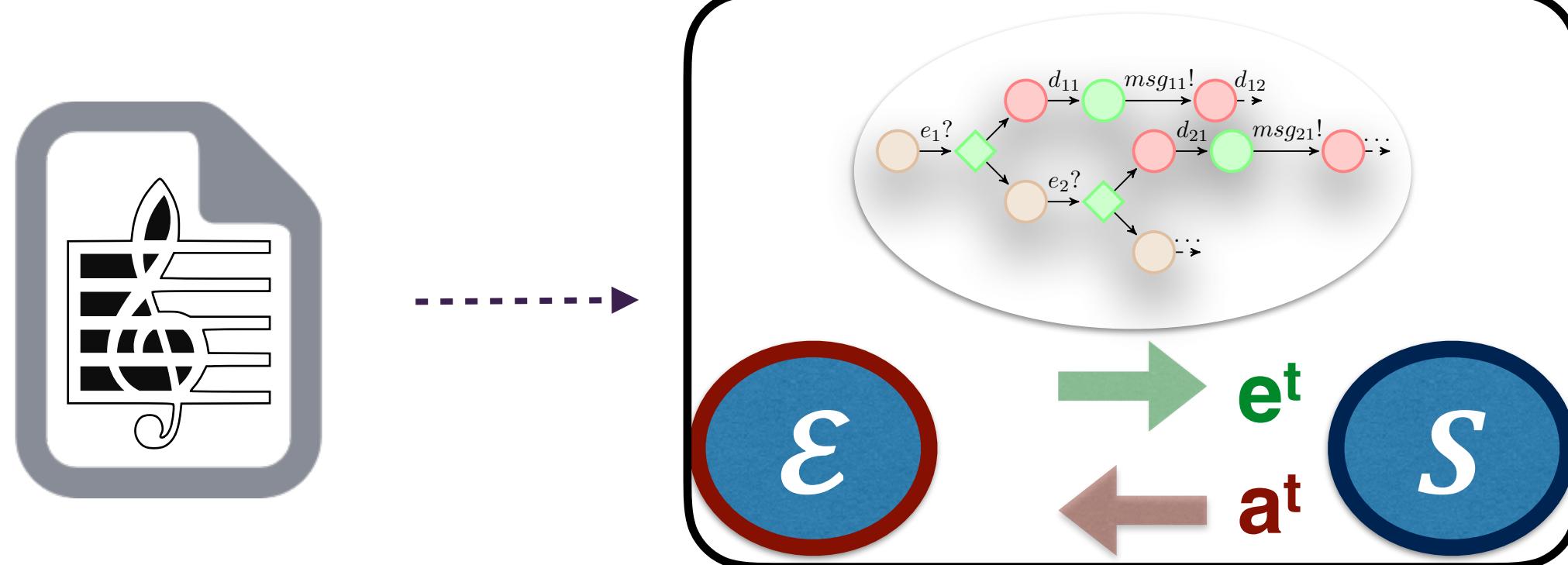


Construction:
from high level to model

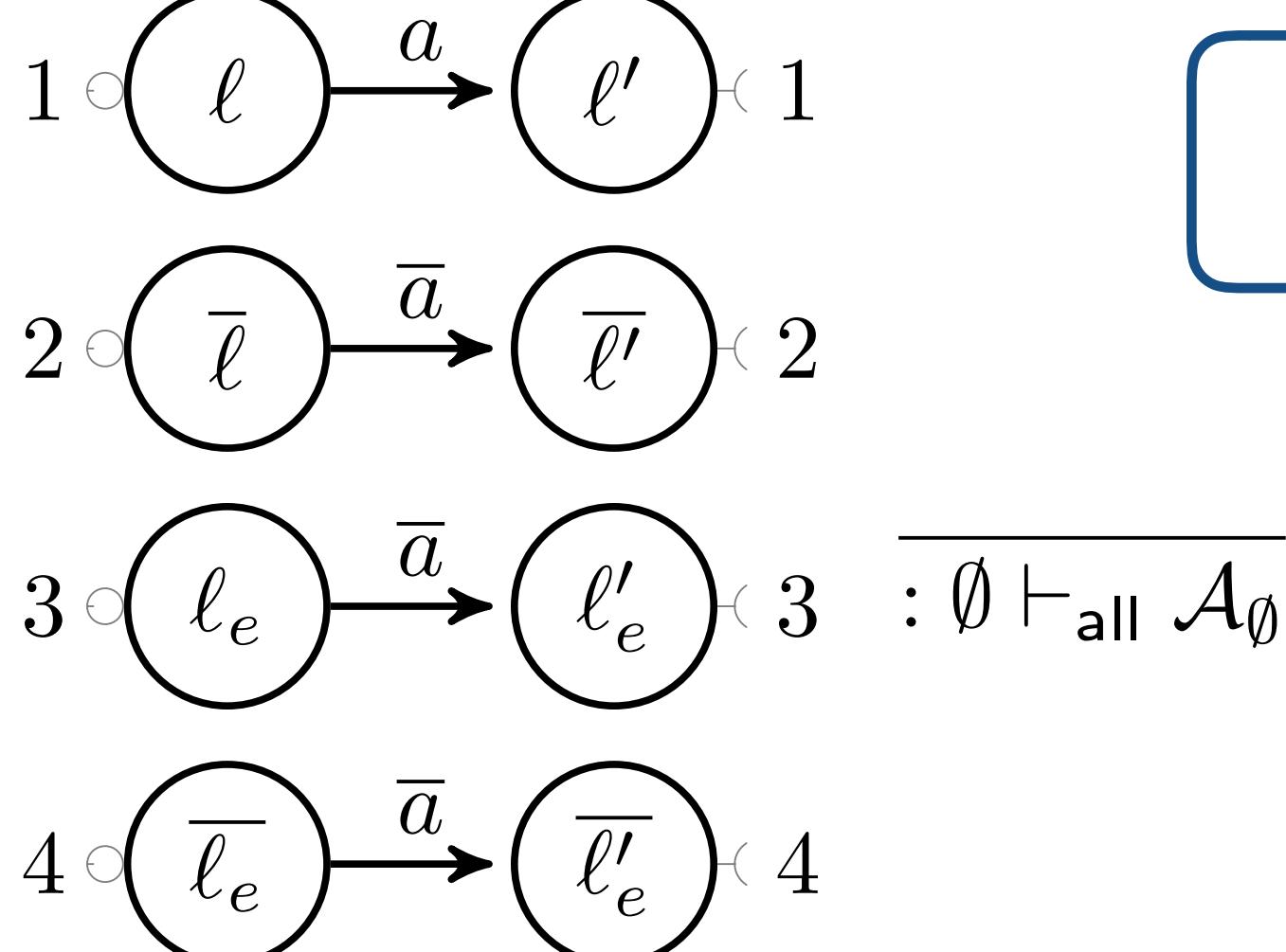
Construction

Automatic

**Domain Specific
Language
Antescofo**



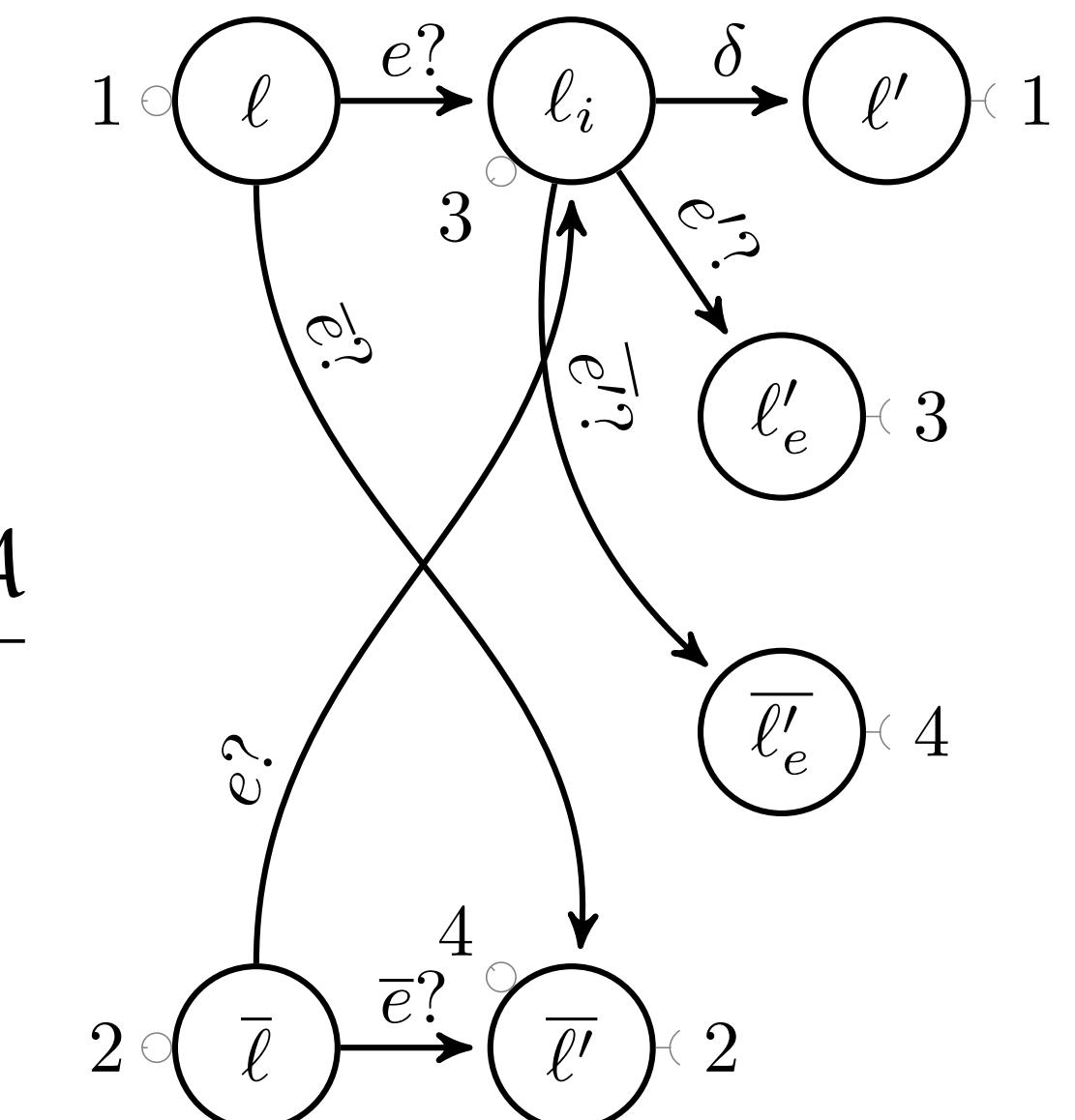
**Interactive Real-Time
Model**



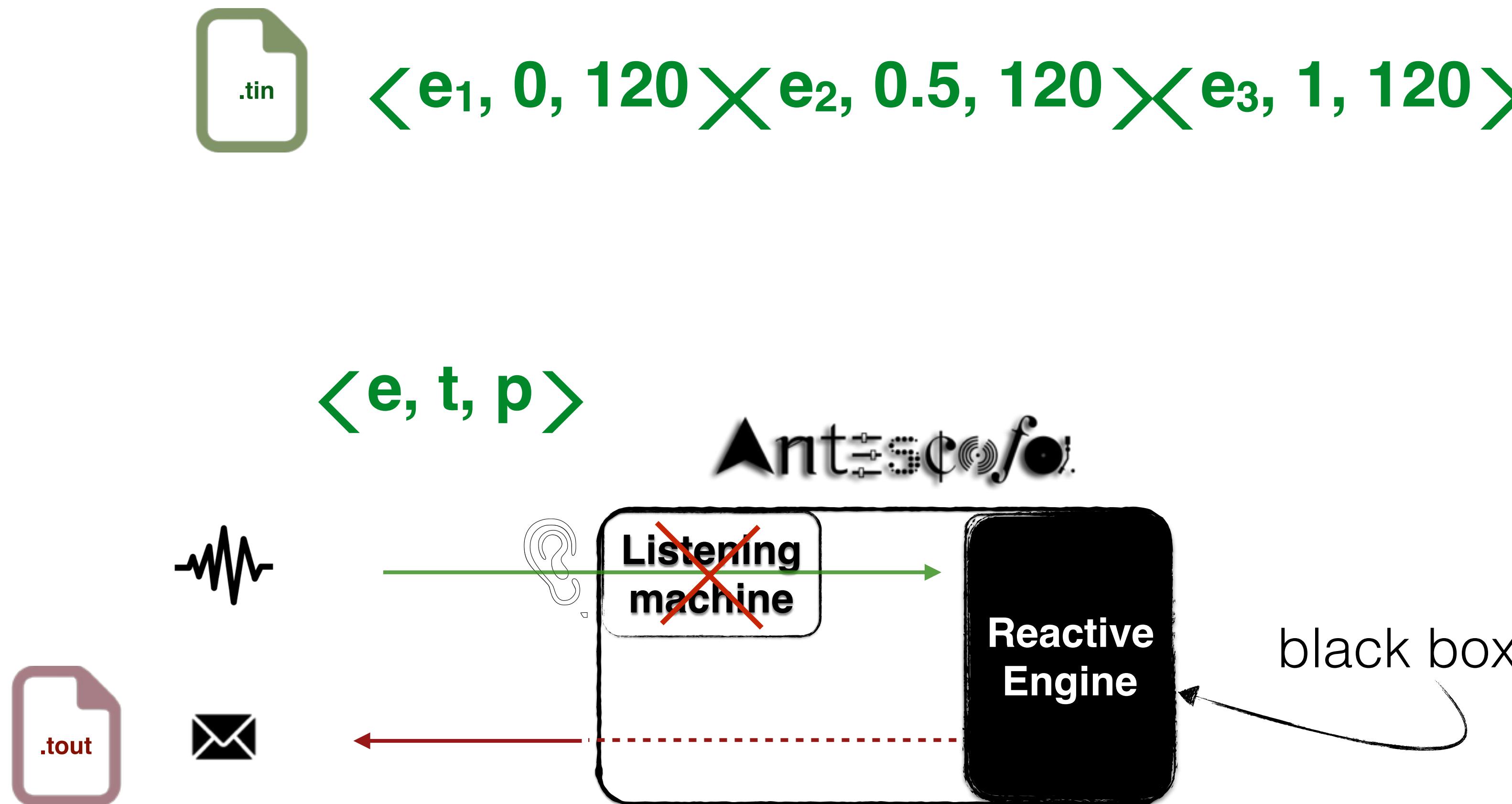
Inference Rules

$$\frac{: ms \vdash_{\text{env}} M_{\text{env}} \quad : ms \vdash_{\text{proxy}} P \quad : ms \vdash_{\text{sys}} A}{: \emptyset \vdash_{\text{all}} A_{\emptyset}}$$

**FSM Parts & Connectors
+ Operators**



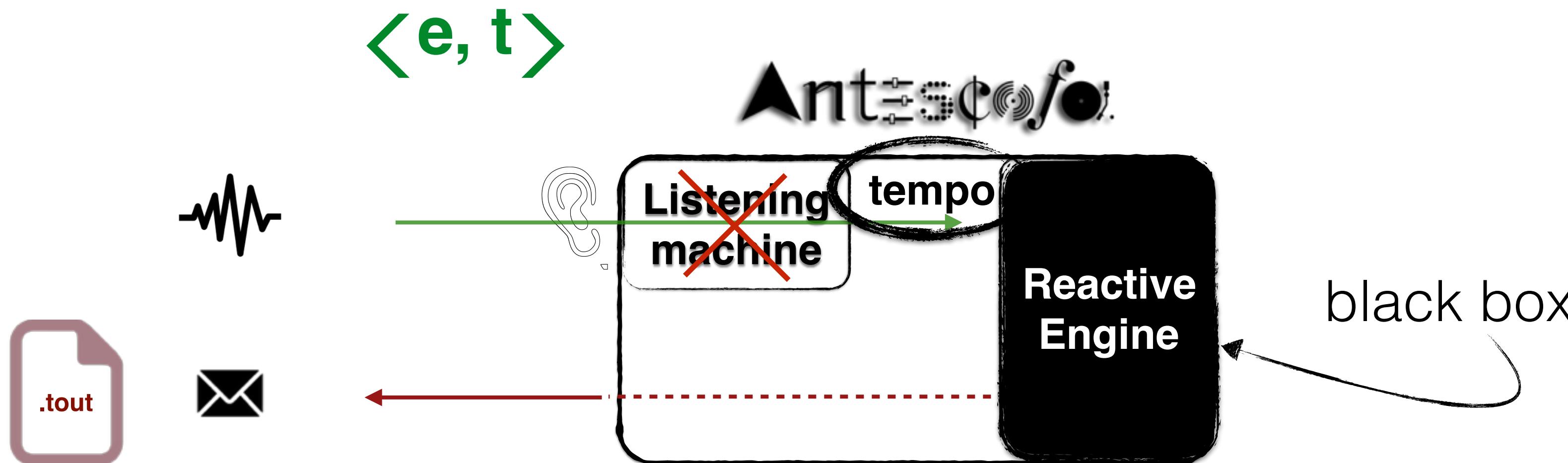
Antescofo Execution



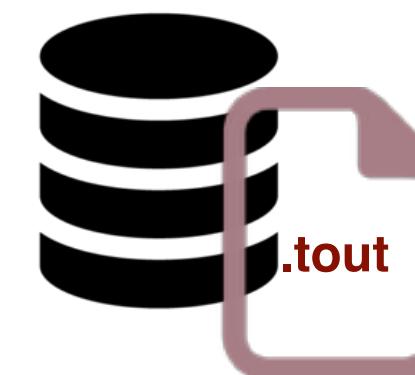
Antescofo Execution



$\langle e_1, 0, - \times e_2, 0.5, - \times e_3, 1, - \rangle$



Verdict



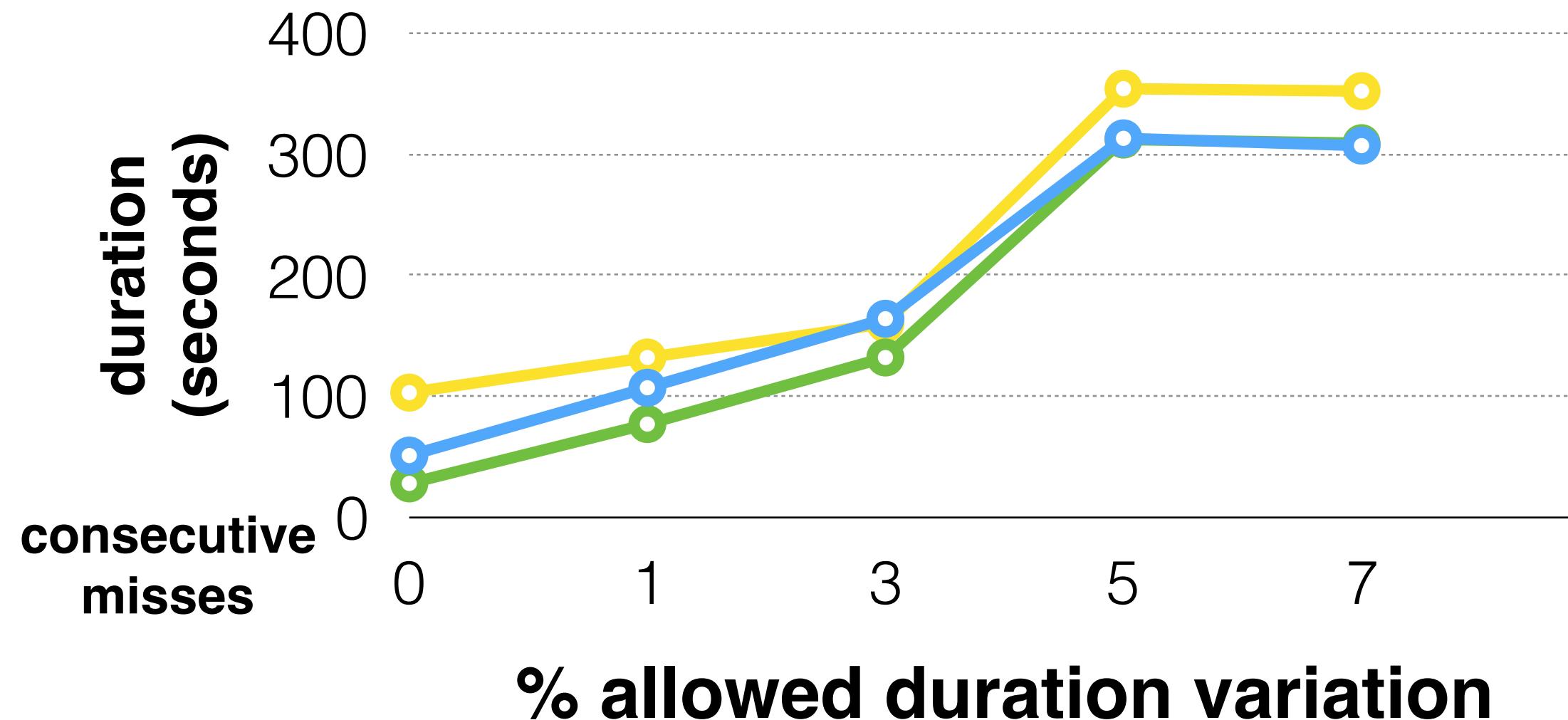
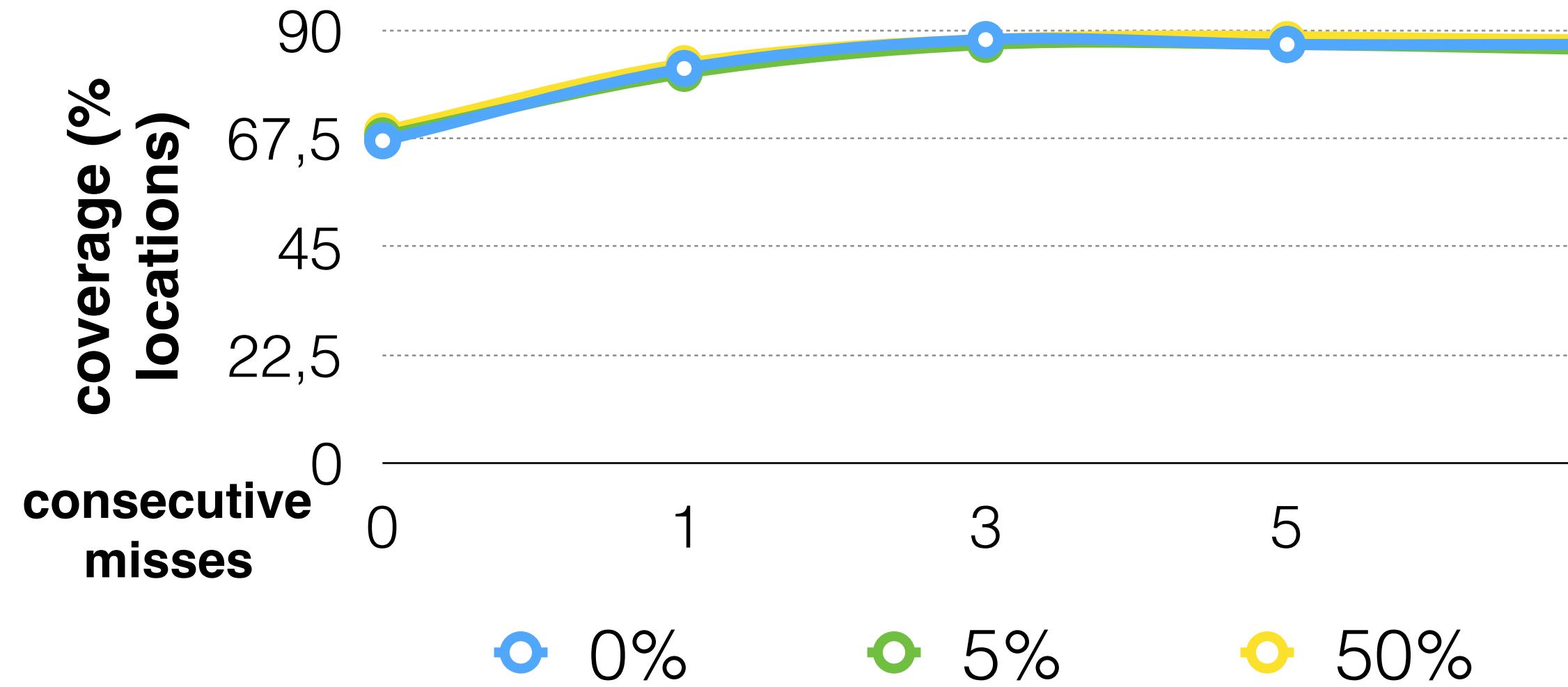
```
start of tests
note0 --> 0.77 --> note1_1.00 --> 0.385 --> note2_1.50 --> 0.1925 --> note3_1.75 --> 0
```

Antescofo Trace			Expected Trace		
	TimeStamp	[Estimate Beat]	TimeStamp	[Beat]	
	a0	0 [0]	a0	0 [0]	
*	note0	0 [0]	e0	0 [0]	* T: 60 BPM
	a1	0.5 [0.5]	a1	0.5 [0.5]	
	a2	0.77 [0.77]	a2	0.77 [0.77]	
*	note1_1.00	0.77 [0.824]	e1	0.77 [0.77]	* T: 64.2 BPM
	a3	0.887 [0.95]	a3	0.887 [1.02]	
*	note2_1.50	0.95047 [1.21]	e2	0.95047 [1.16]	* T: 128 BPM
	a4	0.99 [1.29]	a4	0.95 [1.16]	x delta: 0.04
	a5	1.02 [1.35]	a5	0.985 [1.25]	x delta: 0.0321
	a6	1.02 [1.35]	a6	1.02 [1.35]	
*	note3_1.75	1.0174 [1.4]	e3	1.0174 [1.35]	* T: 173 BPM
*	note4_1.75	1.0174 [1.4]	e4	1.0174 [1.35]	* T: 203 BPM
	a7	1.28 [2.3]	a7	1.28 [2.31]	
*	END	1.2831 [2.38]	e5	1.2831 [2.31]	* T: 220 BPM
Error :: Test K0					
Tinito.					

Experiments

Approach Offline:
CoVer

Benchmark



- Covering generation
- Existing Tools

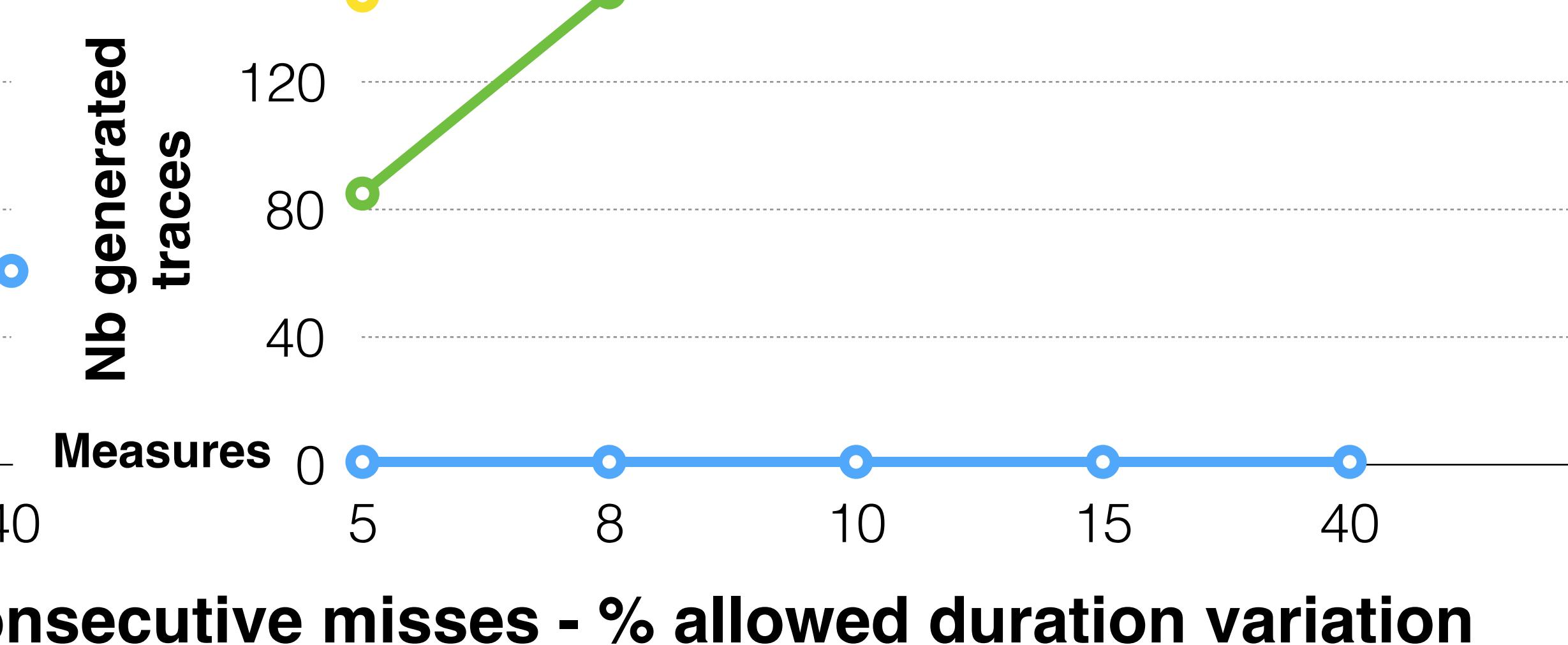
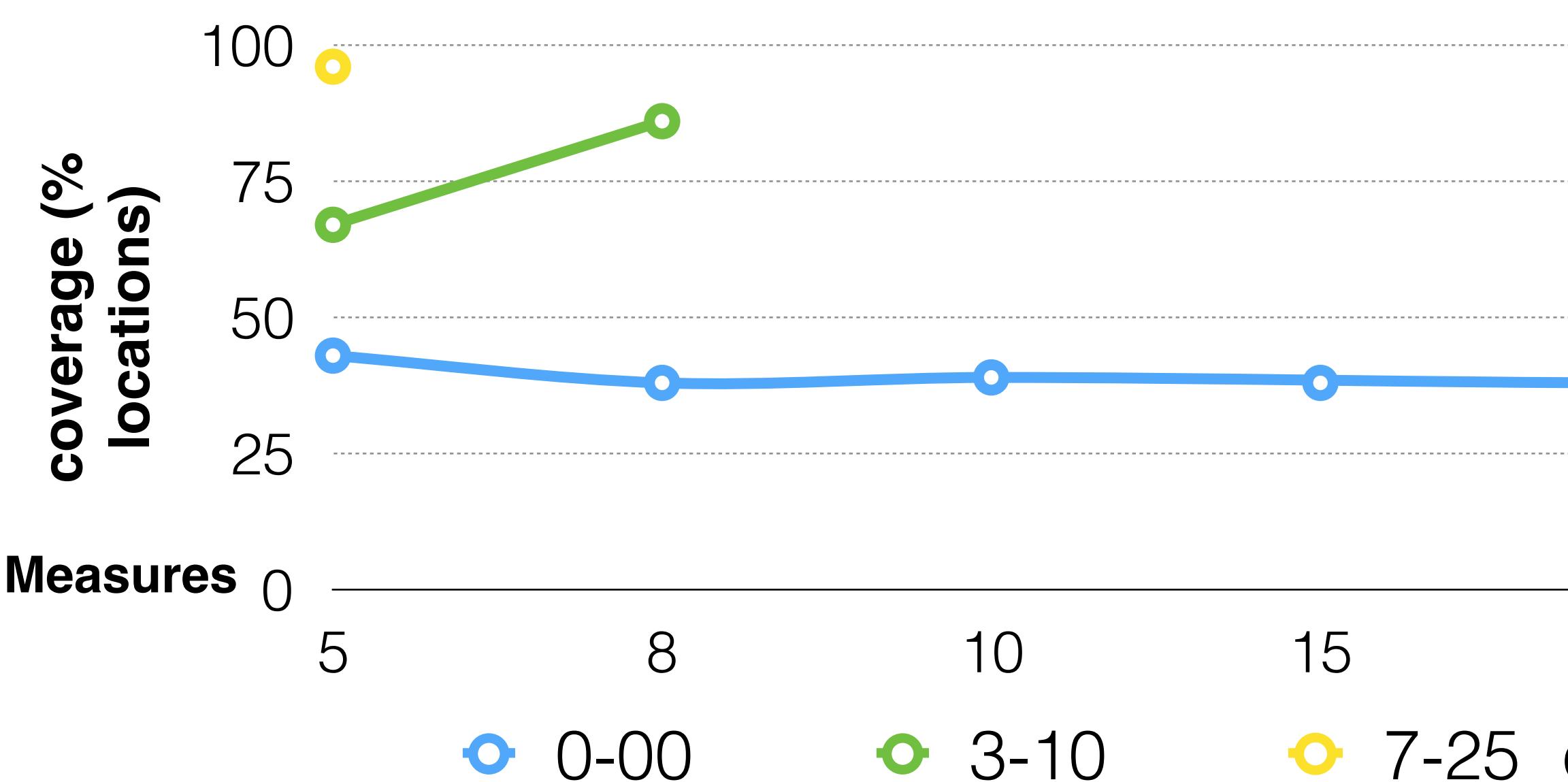
- Translation into Timed Automata
- No musically relevant

Experiments

Approach Offline:
CoVer

Sonata in F major
Georg Friedrich Händel

misses - k



consecutive misses - % allowed duration variation

Measures 5
10s
25 events
84 actions

Measures 8
16s
48 events
185 actions

Measures 10
20s
74 events
264 actions

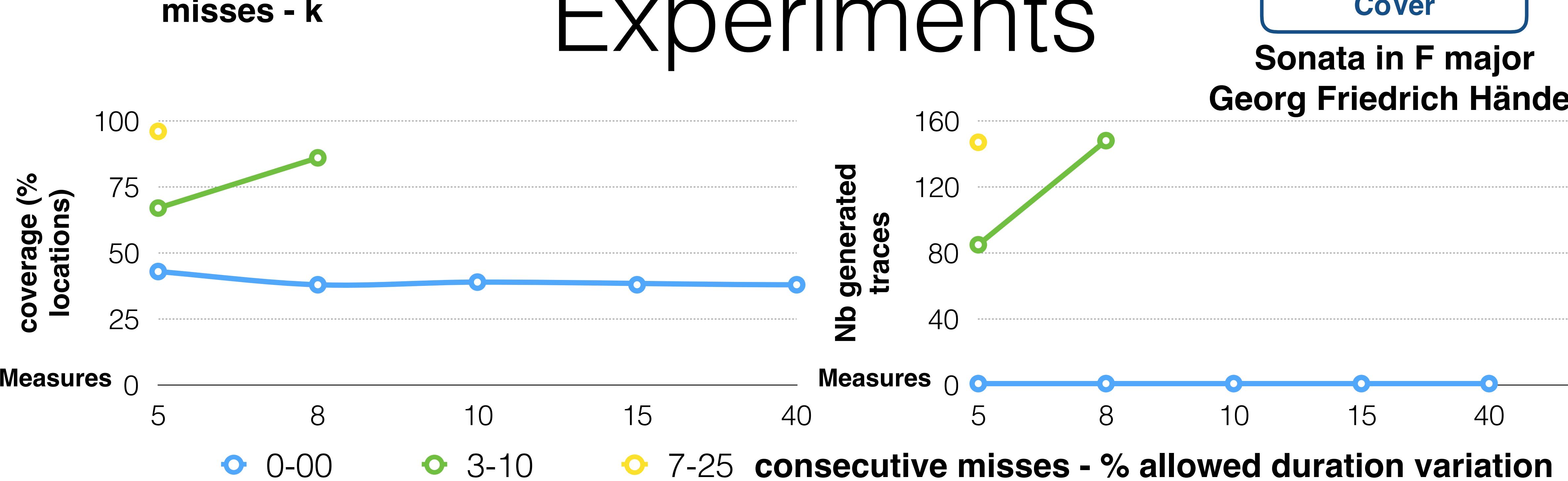
Measures 15
30s
122 events
444 actions

Measures 40
80s
360 events
1218 actions

Approach Offline:
CoVer

Sonata in F major
Georg Friedrich Händel

misses - k



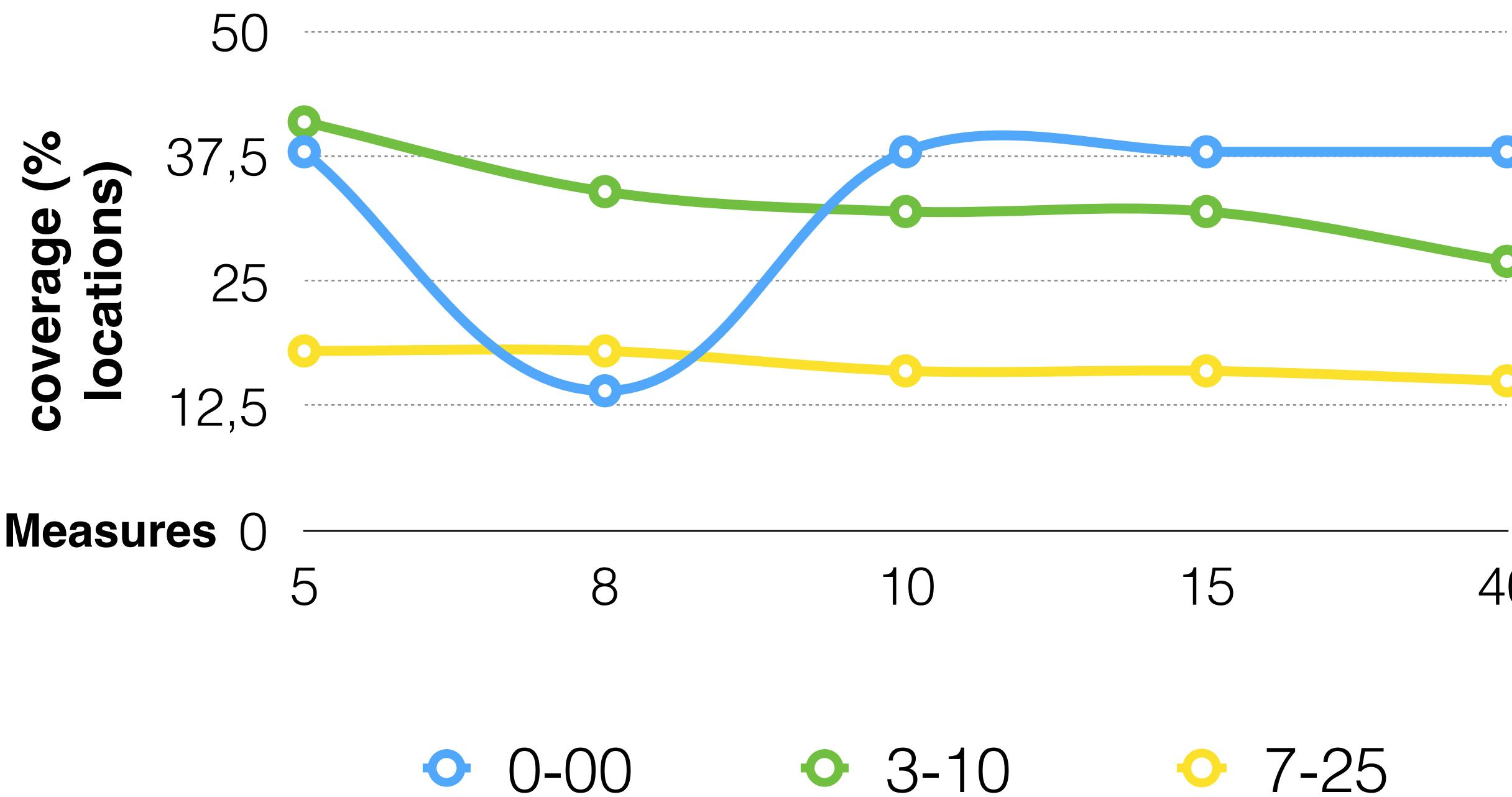
• Not scalable

Experiments

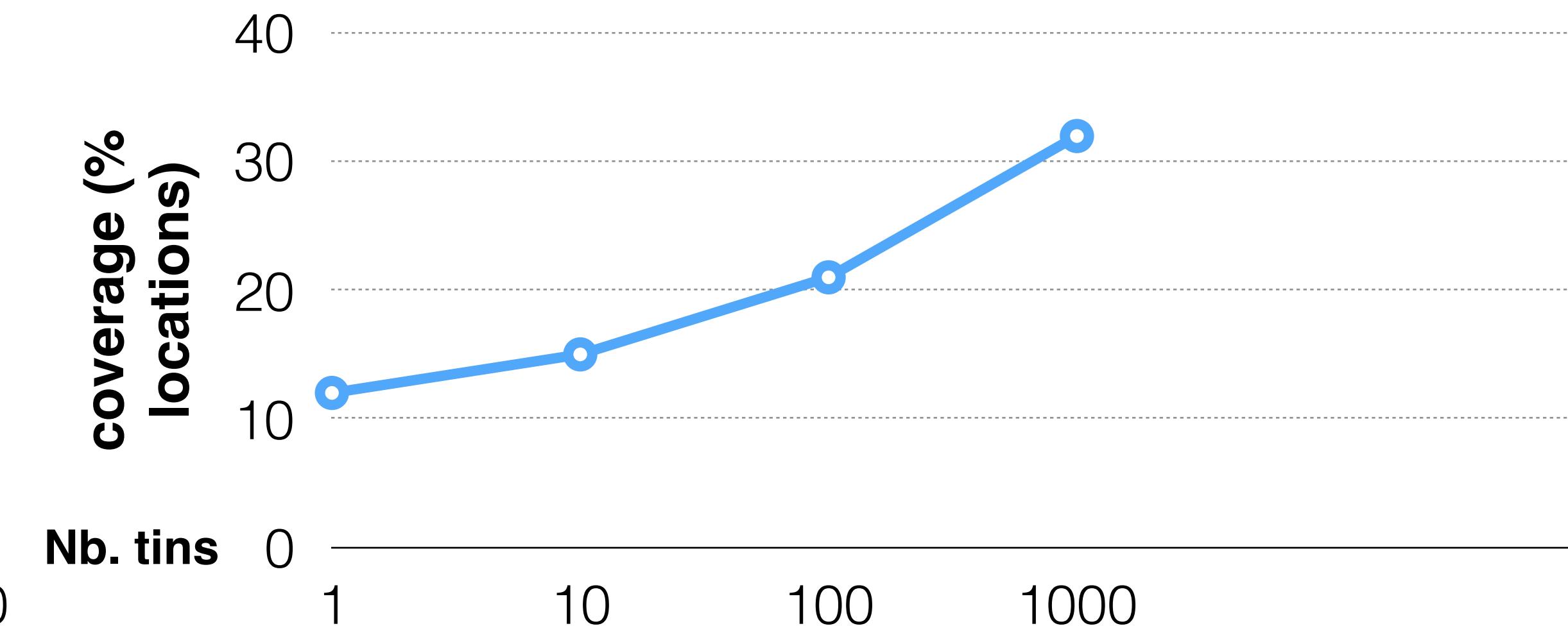
Approach Offline:
Fuzz

Sonata in F major
Georg Friedrich Händel

10 traces



40 measures



consecutive misses - % allowed duration variation

0-00

3-10

7-25

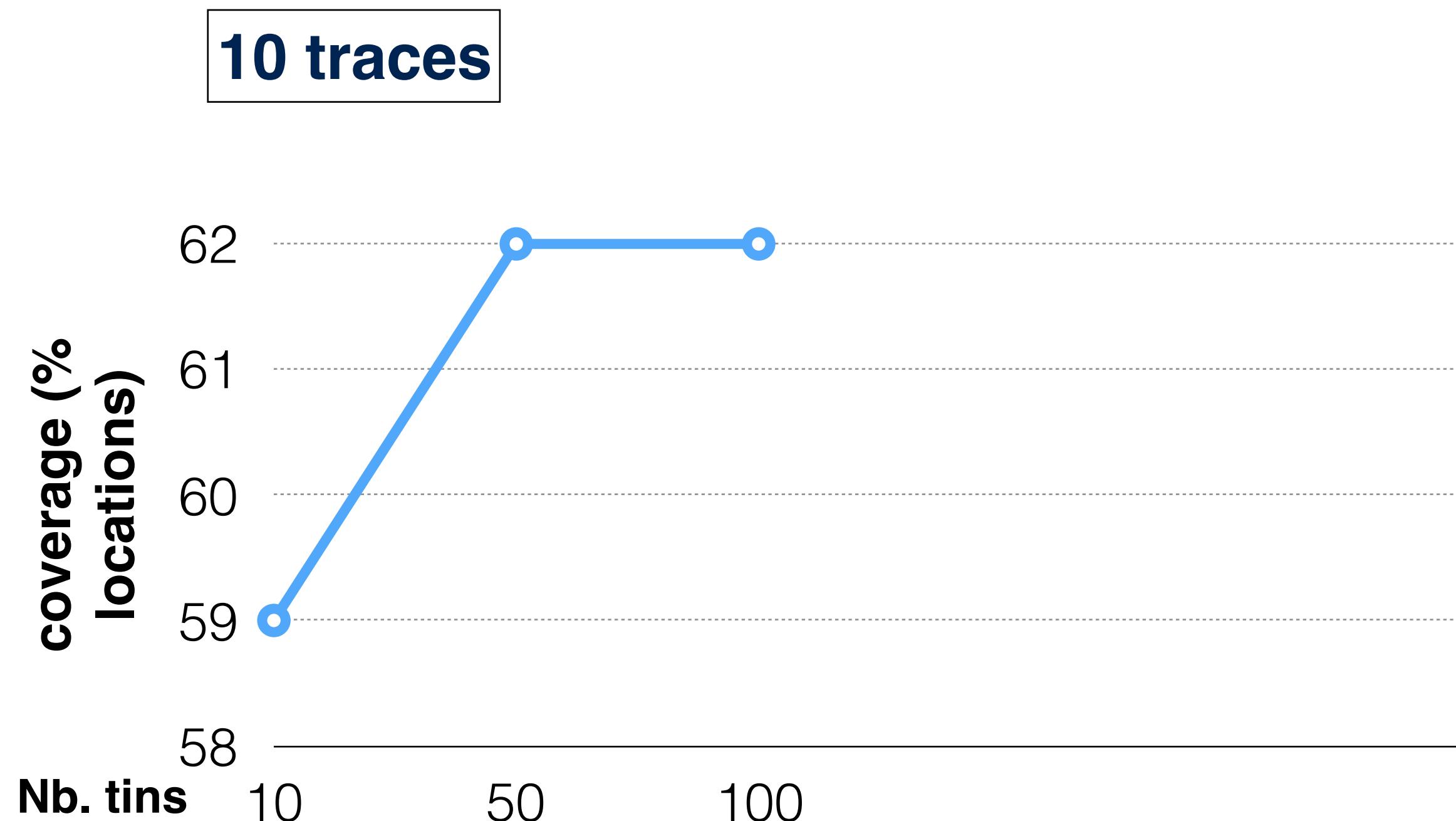
- Musically relevant
- No translation

- No coverage guarantee

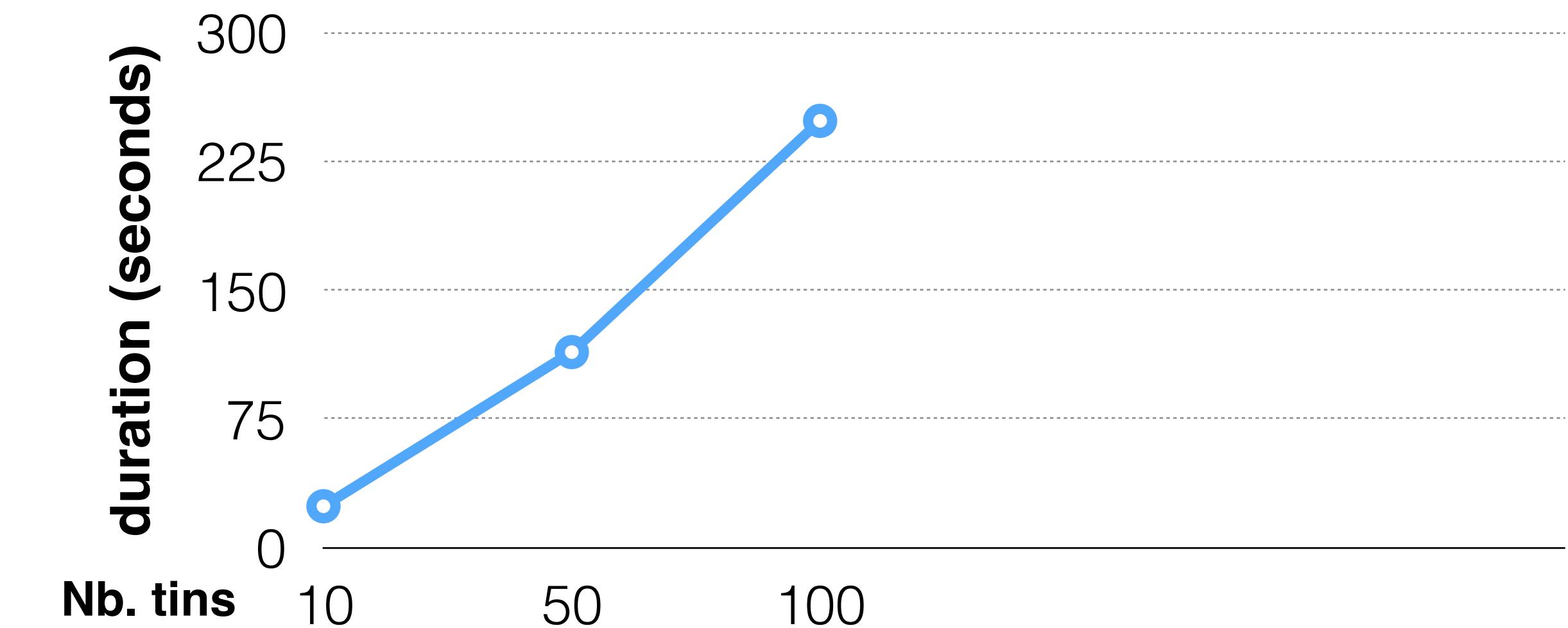
Measures 40
80s
360 events
1218 actions

Experiments

misses - k



Entire measures



Approach Online

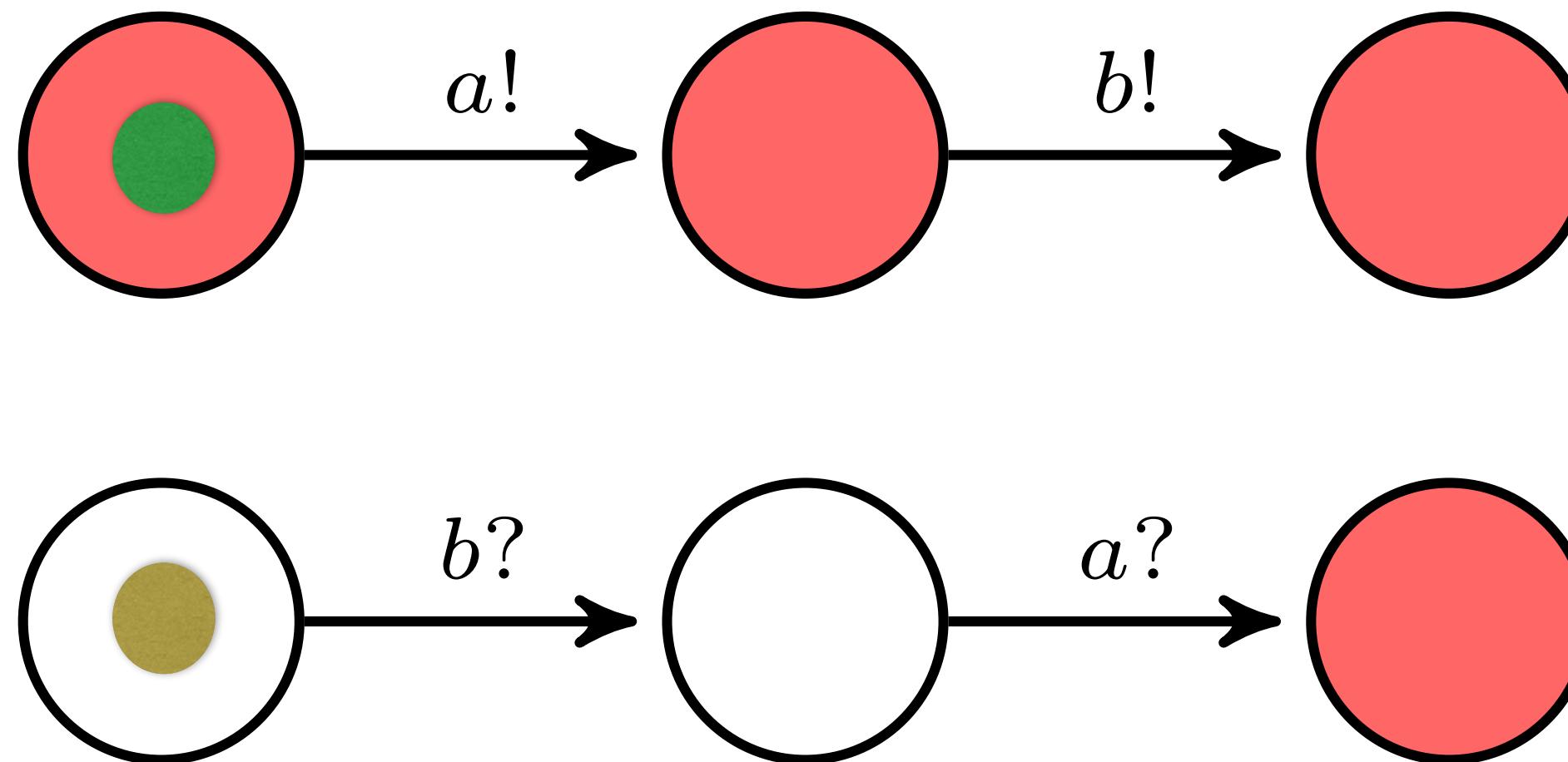
Sonata in F major
Georg Friedrich Händel

- Musically relevant
- No translation

- No coverage guarantee

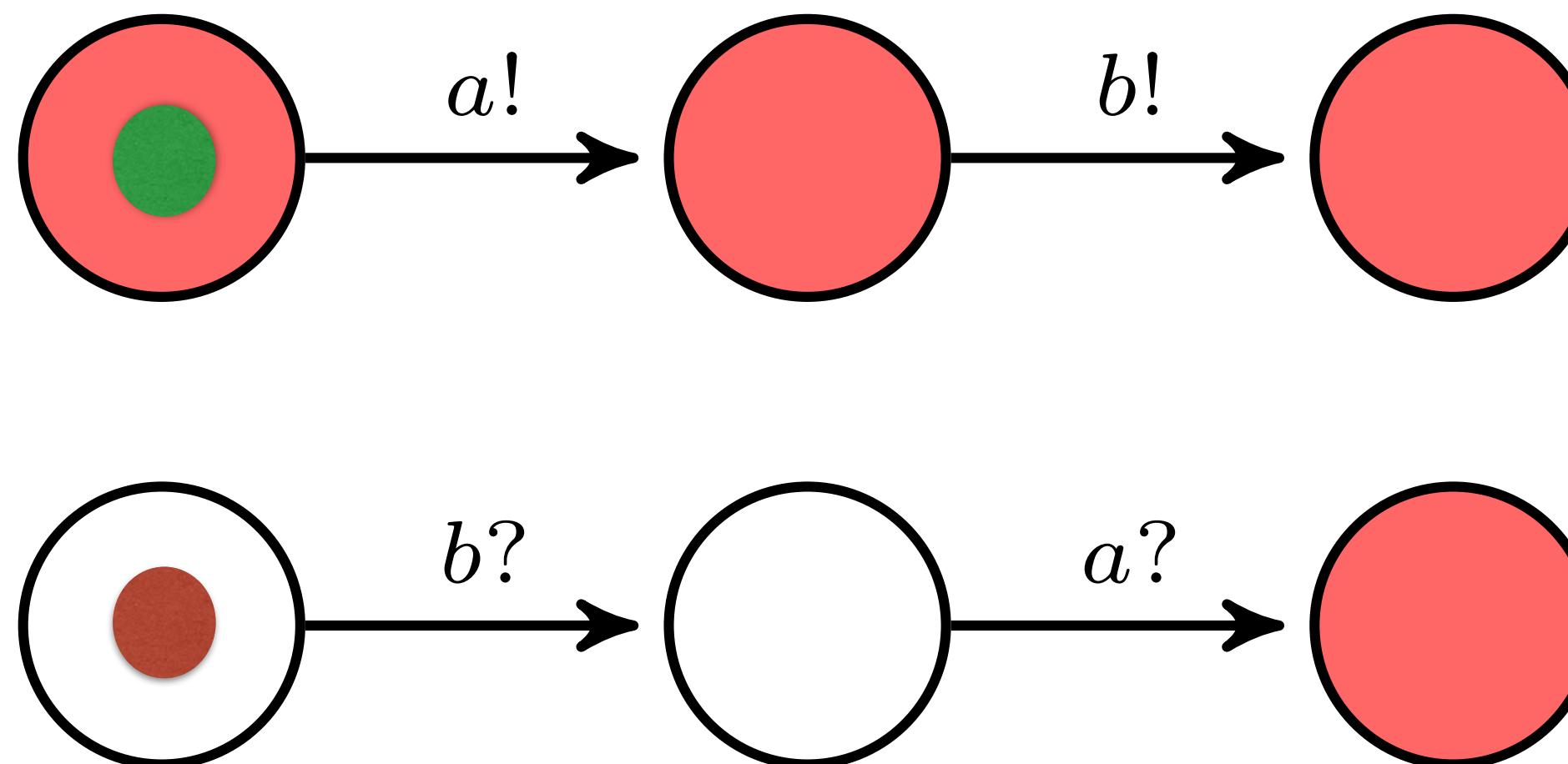
Faster

Appendices



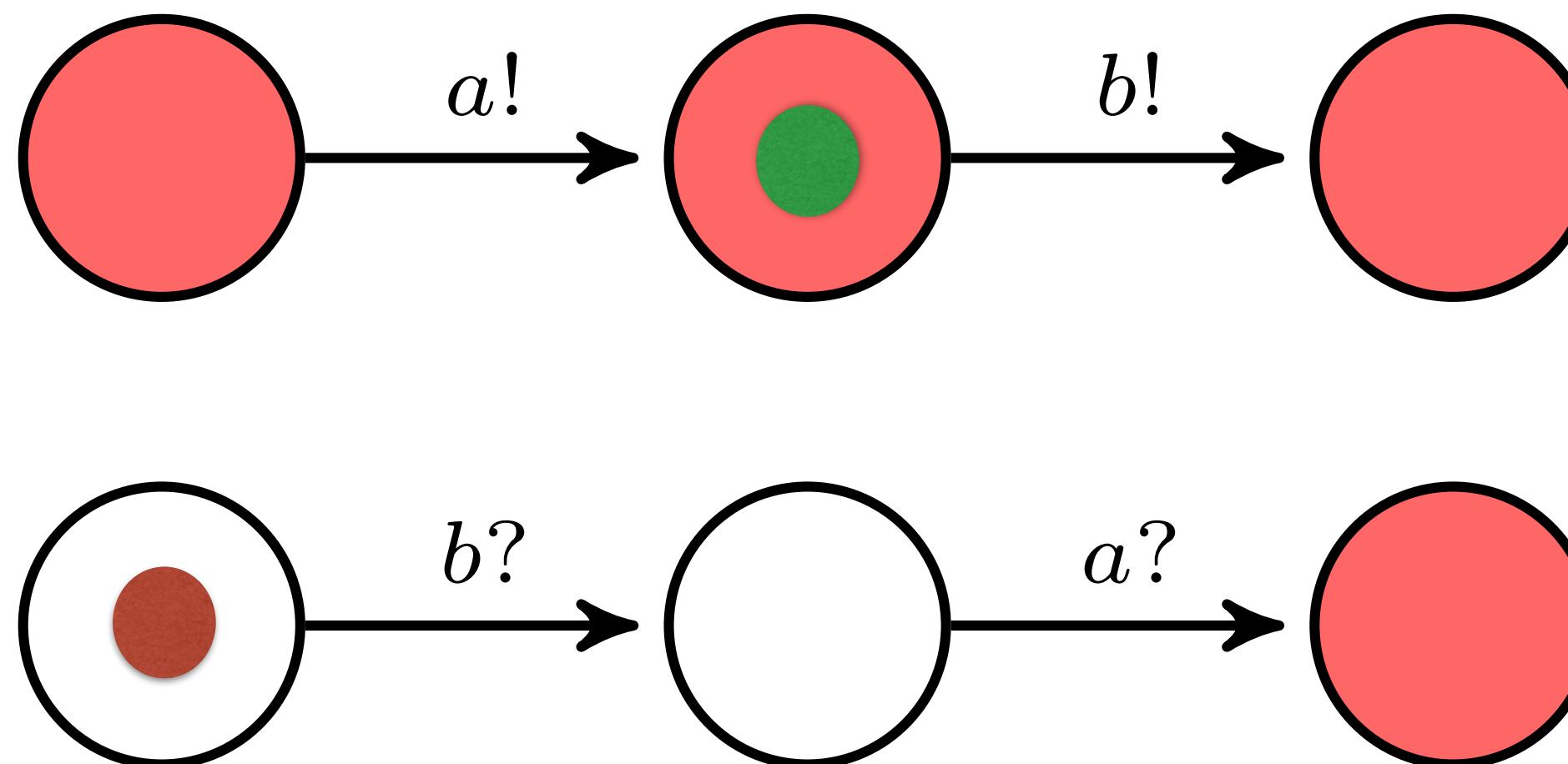
State: $\langle 0, 0 \rangle [c_1=0 :: c_2=0] \{ \}$

Appendices



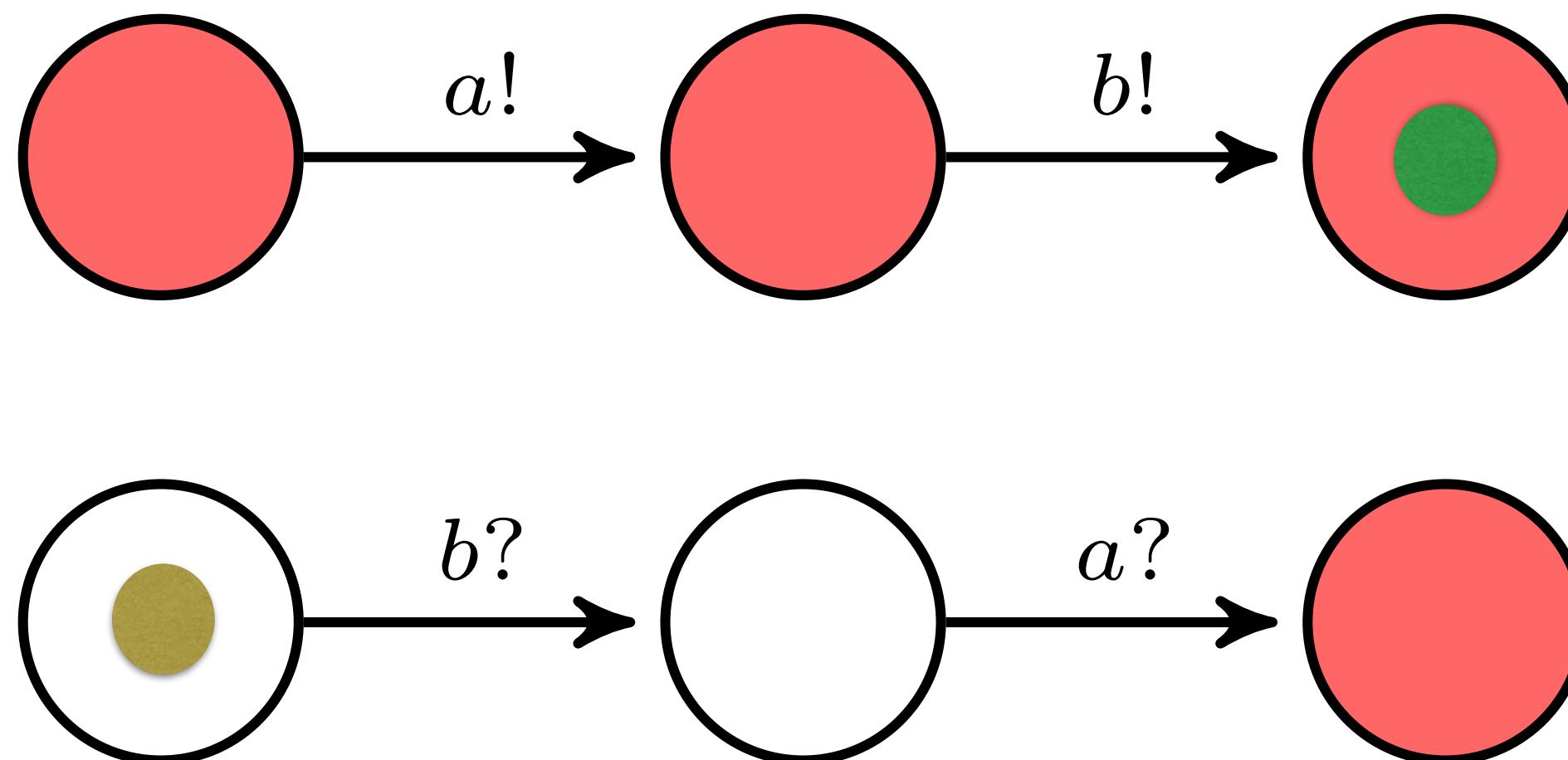
State: $\langle 0, 0 \rangle [\underline{c_1=0} :: c_2=0] \{ \}$

Appendices



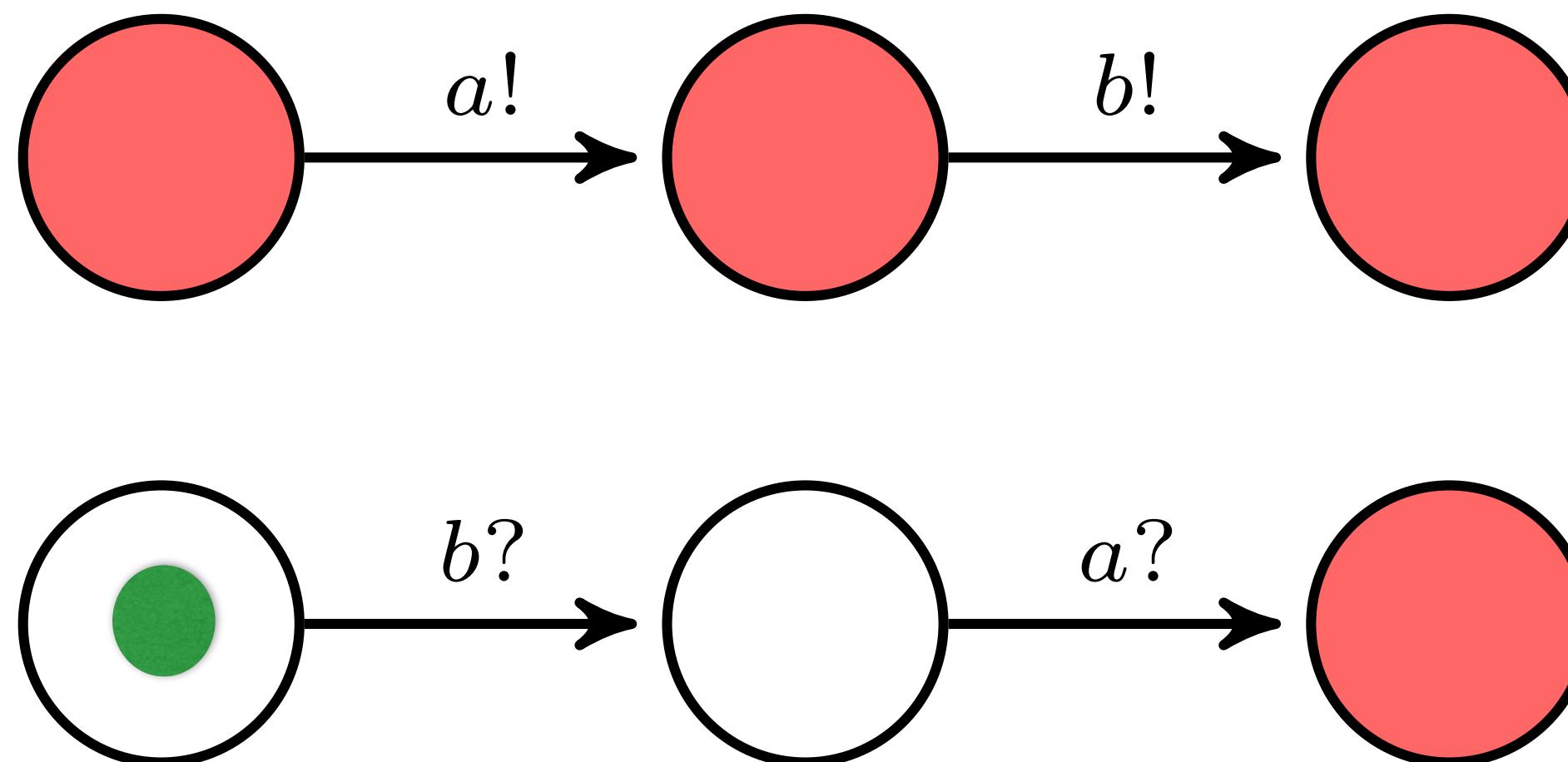
State: $\langle 0, 1 \rangle [\underline{c_1=0} :: c_2=0] \{ a \}$

Appendices



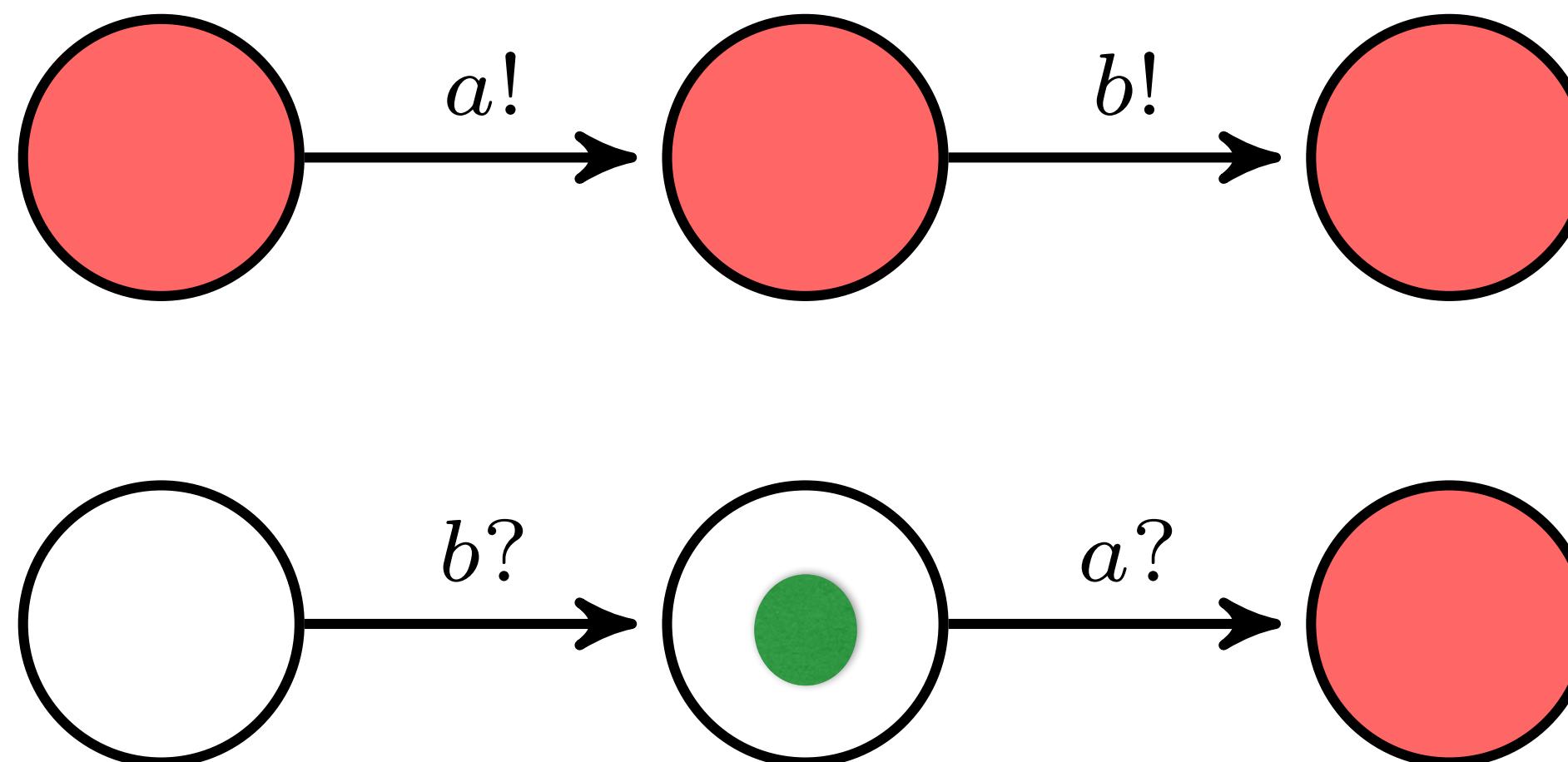
State: $\langle 0, 2 \rangle [c_1=0 :: c_2=0] \{ a, b \}$

Appendices



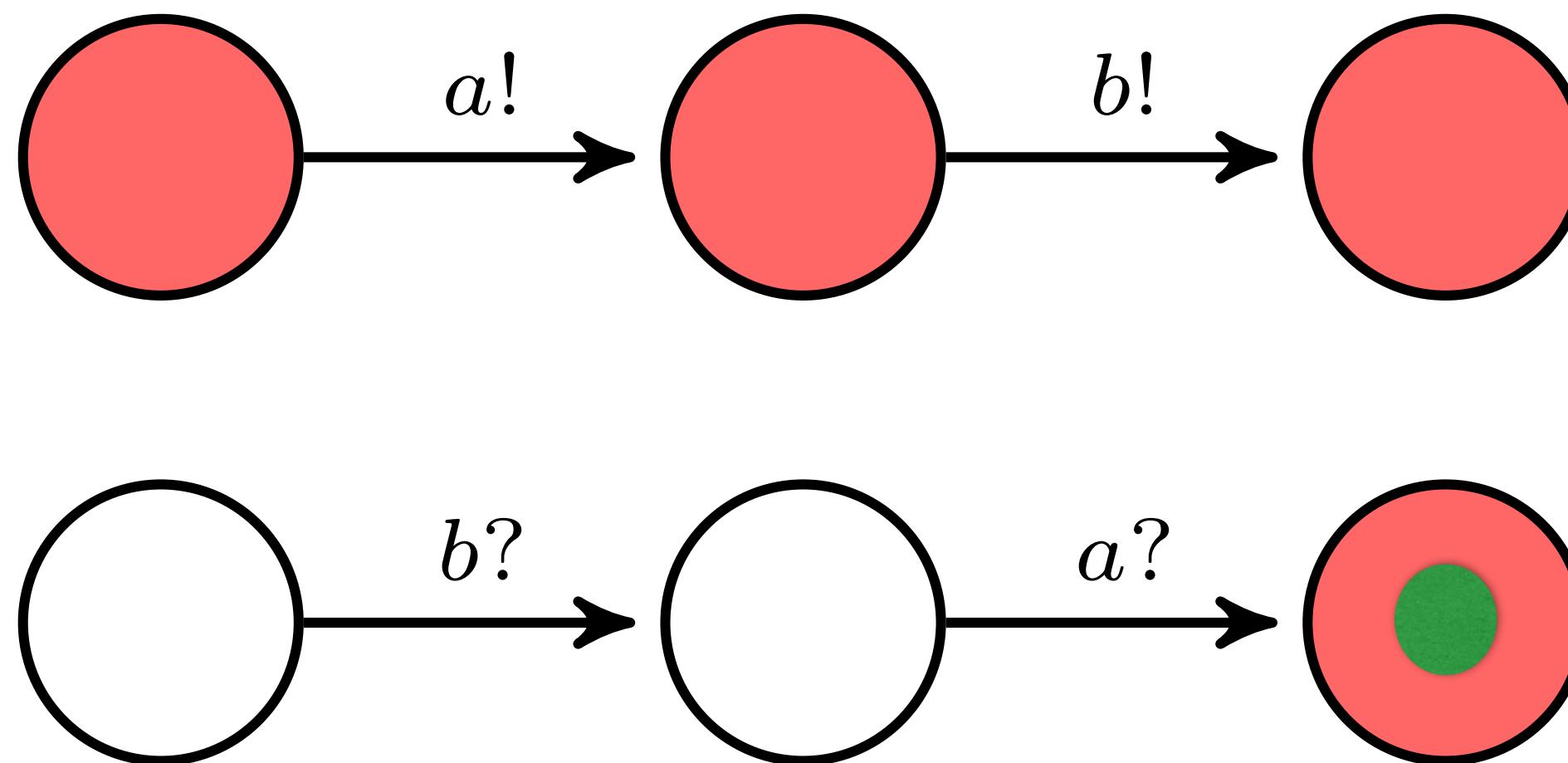
State: $\langle 0, 3 \rangle [\underline{c_2=0}] \{ a, b \}$

Appendices



State: $\langle 0, 4 \rangle [\underline{c_2=0}] \{ a, b \}$

Appendices



State: $\langle 0, 5 \rangle [\underline{c_2=0}] \{ a, b \}$